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# Observational detection of eight mutual eclipses and occultations between the satellites of Uranus

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## ABSTRACT

**Aims.** We carried out observations, with five different instruments ranging in aperture from 0.4 m to 10 m, of the satellites of Uranus during that planet’s 2007 Equinox. Our observations covered specific intervals of time when mutual eclipses and occultations were predicted.

**Methods.** The observations were carried out in the near-infrared part of the spectrum to mitigate the glare from the planet. Frames were acquired at rates  $>1$ /min. Following modelling and subtraction of the planetary source from these frames, differential aperture photometry was carried out on the satellite pairs involved in the predicted events. In all cases but one, nearby bright satellites were used as reference sources.

**Results.** We have obtained fifteen individual lightcurves, eight of which show a clear drop in the flux from the satellite pair, indicating that a mutual event took place. Three of these involve the faint satellite Miranda. All eight lightcurves were model-fitted to yield best estimates of the time of maximum flux drop and the impact parameter. In three cases best-fit albedo ratios were also derived. We used these estimates to generate intersatellite astrometric positions with typical formal uncertainties of  $<0.01$ , several times better than conventional astrometry of these satellites. The statistics of our estimated event midtimes show a systematic lag, with the observations later than predictions. In addition, lightcurves of two partial eclipses of Miranda show no statistically significant evidence of a light drop, at variance with the predictions. These indicate that new information about the Uranian satellite system is contained in observations of mutual events acquired here and by other groups.

**Key words.** eclipses – occultations – planets and satellites: individual: Uranus – planets and satellites: general – methods: observational – techniques: photometric

## 1. Introduction

The satellites of the planets Jupiter, Saturn and Uranus undergo seasons of mutual eclipses and occultations at equinox when the Sun and the Earth respectively pass through the planet’s equatorial plane. These so-called “mutual events” yield very precise positional measurements of the satellites (Vasundhara et al. 2003; Noyelles et al. 2003; Emelyanov & Gilbert 2006).

The 2007 Uranian equinox presented the first opportunity to observe mutual events between the classical Uranian satellites: Miranda (V), Ariel (I), Umbriel (II), Titania (III) and Oberon (IV) (Christou 2005; Arlot et al. 2006). These

observations can potentially lead to the greatest incremental improvement of the satellite ephemerides and system constants since the Voyager 2 flyby of the Uranian system in 1986.

In the present study, we report on the outcome of an observational programme of these mutual events using five different instruments with 0.4 m, 2 m and 10 m apertures during 2007. Analysis of one of these observations, which to our knowledge was also the first of a mutual event between two Uranian satellites, was reported in Hidas et al. (2008) hereafter referred to as HCB08. In the following section we describe our observational strategy and circumstances for the observed events. In Sect. 3 we explain the methods we employed for data reduction,

**Table 1.** Instruments and detectors used in acquiring the observations reported in this paper.

Site Abbr	FTN (F65)	FTS (E10)	ATH1	ATH2	SALT (A60)
Location	Haleakala, Maui	Siding Spring, Australia	Athens, Greece	Athens, Greece	Sutherland, South Africa
Lat (N)	20 <sup>d</sup> 42 <sup>m</sup> 27 <sup>s</sup>	-31 <sup>d</sup> 16 <sup>m</sup> 22 <sup>s</sup>	37 <sup>d</sup> 59 <sup>m</sup> 52 <sup>s</sup>	37 <sup>d</sup> 58 <sup>m</sup> 07 <sup>s</sup>	-32 <sup>d</sup> 22 <sup>m</sup> 46 <sup>s</sup>
Lon (E)	203 <sup>d</sup> 44 <sup>m</sup> 38 <sup>s</sup>	149 <sup>d</sup> 04 <sup>m</sup> 14 <sup>s</sup>	23 <sup>d</sup> 53 <sup>m</sup> 36 <sup>s</sup>	23 <sup>d</sup> 47 <sup>m</sup> 00 <sup>s</sup>	20 <sup>d</sup> 48 <sup>m</sup> 30 <sup>s</sup>
Aper	200 cm	200 cm	40 cm	40 cm	1000 cm
CCD	2k × 2k EEV CCD42-40	2k × 2k EEV CCD42-40	1392 × 1040 ATIK 16HR	1530 × 1020 SBIG ST-8 XMEI	2 2k × 4k EEV CCD44-82 frame xfer
Binning	2 × 2	2 × 2	NO	2 × 2	2 × 2
Img scale "/pxl <sup>a</sup>	0.28	0.28	0.31	1.03	0.28

<sup>a</sup> Image scale is after binning, where applicable.

**Table 2.** Summary of observational circumstances and results for the mutual event observations attempted in this work.

Date (DDMMYY)	Event type <sup>a</sup>	Obs. site <sup>b</sup>	Exp. time (s)	Filter	Number of frames	UT of first exp.	UT of last exp.	Ref. sat.	Obs. result <sup>c</sup>	Seeing (")	Airmass
040507	4O2P	FTS	3	sdss <i>i'</i>	150	19:02:01.3	19:32:02.1	Titania	POS	2.25	1.62
260707	1E5P	FTS	2	sdss <i>i'</i>	43	18:56:21.6	19:22:21.8	Titania	NEG	1.18	1.28
050807	4O2P	FTN	2	sdss <i>i'</i>	53	13:32:12.2	14:12:08.0	Titania	POS	1.39	1.15
060807	1O5P	FTN	2	sdss <i>i'</i>	14	10:32:57.4	10:41:53.4	Titania	NEG	0.82	1.32
140807	2O4P	ATH1	30	IR72	34	01:09:39	01:46:14	Titania	POS	4.35	1.46
200807	5O2P	FTN	2	sdss <i>i'</i>	51	13:34:07.0	14:01:11.7	Ariel	NEG	3.68	1.30
220807	2E5T	FTN	2	sdss <i>i'</i>	100	14:35:06.4	15:15:24.0	Titania	POS	1.55	1.74
240807	1O2P	FTN	2	sdss <i>i'</i>	150	12:02:13.8	13:00:10.1	Oberon	POS	1.11	1.16
220907	1E5P	ATH2	10	Bessell I	260	18:01:26	18:57:35	Titania	NEG	4.26	2.08
051007	1O5P	FTS	2	sdss <i>i'</i>	36	08:55:33.3	09:29:28.7	Oberon	NEG	1.77	1.55
121007	4E5T	FTN	2	sdss <i>i'</i>	75	09:32:47.3	09:59:52.7	Titania	POS	2.35	1.23
211007	1E2P	FTS	2	sdss <i>i'</i>	100	13:53:06.3	14:30:07.2	Titania	NEG	1.52	1.51
221007	1E2C	FTS	2	sdss <i>i'</i>	100	13:22:23.7	14:00:09.8	Titania	NEG	1.34	1.38
291107	2E4P	SALT	0.7, 1, 2	Bessell I	–	19:00:44	19:42:05	–	NEG	–	1.26
301107	3E4P	SALT	0.7	Bessell I	4299	18:34:47	19:28:27	Star	POS	–	1.22
301107	1E5T	FTN	2	sdss <i>i'</i>	38	08:32:56.0	08:57:37.9	Titania	POS	1.58	2.18

<sup>a</sup> We use the event type notation of [Arlot et al. \(2006\)](#). <sup>b</sup> Observatory abbreviations are given in Table 1. <sup>c</sup> Each observation results in either POS(itive) or NEG(ative) detection of a lightcurve.

particularly where these differ from the approach used in HCB08. In Sect. 4 we present our results in the form of lightcurves, model-fitted parameter estimates and astrometric offsets for the satellite pairs involved in each event. In addition, we show that a significant offset exists between predicted and observed event midtimes. In Sect. 5 we present our conclusions.

## 2. Observations

Our programme of observations spanned the period 04/05/2007–30/11/2007 and employed the instruments and facilities listed in Table 1. The majority of the observations were carried out with the Faulkes Telescopes North (FTN) and South (FTS) on the island of Maui, Hawaii and at Siding Spring, Australia respectively. Two events were observed from Athens, Greece: one from the Ellinogermaniki Agogi School Observatory (ATH1) and one from the Gerostathopoulion Observatory of the University of Athens (ATH2). Finally, two events were attempted with the Southern African Large Telescope (SALT) in Sutherland, South Africa. Our observations are summarised in Table 2.

To facilitate the observational campaign, predictions were tabulated in advance by the models of [Christou \(2005\)](#) and [Arlot et al. \(2006\)](#). Christou based his predictions on the Voyager-era GUST86 analytical ephemeris ([Laskar & Jacobson 1987](#)) which is available in binary format through NASA's Navigation and Ancillary Information Facility (NAIF) ftp site (<ftp://naif.jpl.nasa.gov/pub/naif/>) as SPICE kernel URA027. Arlot et al reproduced the results by Christou based on this ephemeris

and, in addition, generated a different set of predictions using the recently developed numerical ephemeris LA06 ([Lainey 2008](#)).

To ensure that each mutual event would be captured in its entirety (if it occurred) and to satisfy the requirement, imposed by scheduling restrictions, that the total duration of each observation is kept to a minimum, we adopted the following strategy: for each event, the published start and end times according to the predictions by [Christou \(2005\)](#) and [Arlot et al. \(2006\)](#) were compared. The start (end) times of our observations were then determined by choosing the earlier (later) of the two start (end) times and subtracting (adding) a time interval equal to three times the difference between the two sets of predictions.

During the course of these observations, [Rush & Jacobson \(2007, hereafter RJ07\)](#) published a new numerical ephemeris for these satellites, available through NAIF as SPICE kernel URA083. By incorporating this new kernel into the prediction model by Christou, we generated a new set of predictions specifically for the events discussed in this paper. This was done partly to refine our choice of observing interval for those events that were yet to be observed but also to enable comparisons between GUST86, LA06 and the new ephemeris.

We also strove to maximise the contrast between the faint satellites and the bright planet while, at the same time, sampling the planet at a good signal-to-noise. The latter would allow a posteriori modelling and subtraction from each frame in order to facilitate satellite photometry. For FTN and FTS, this meant that our implementation was very similar to that used in HCB08, namely short exposures using a Sloan Digital Sky

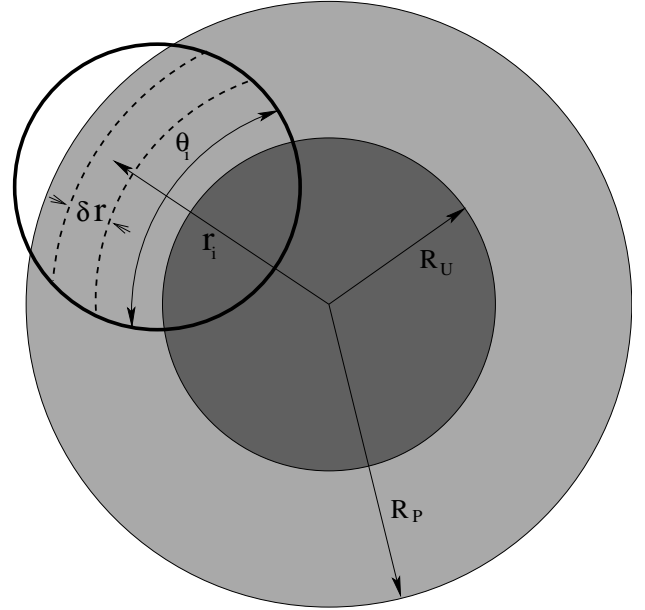
Survey (SDSS)  $i'$  filter at a relatively high cadence ( $<1$  min). We used 2-s exposures as opposed to the 3-s used in HCB08 since the new observations were generally acquired at lower airmass. The cadence was lower in the new observations (ranging between 30 and 40 s as opposed to  $\sim 14$  s in HCB08) due to the non-availability of a certain mode in the instrument control software. The two observations carried out from Athens used a similar strategy, utilising longer exposures in order to reach a satisfactory level of signal with these smaller apertures. During the observations on 22/09/07, we attempted  $2 \times 2$  binning in order to improve the cadence to  $\sim 10$  s and acquire more measurements during the critical period. However, this resulted in under-sampling the planet and complicated the process of extracting it from the images. Combined with the relatively high airmass, it introduced a high level of noise in the reduced data.

The SALT observations were carried out in Slot Mode, where a mask is advanced over the entire chips except for a slot just above the frame transfer boundary. Instead of half frame transfers at the end of each exposure, 144 rows are moved (the “slot”). This allowed exposure times as short as 0.7 s. In addition, the slot field of view was aligned with the satellite orbital plane projected on the sky. The image of Uranus was placed in the 1.5 mm (equivalent to 100 pixels) gap between the two chips in order to minimise the effects of planetary glare on the satellites. Observations on the first night (29/11/07) were carried out through cloud and, although the satellites were detectable on the images, the signal-to-noise ratio was too low and the sky conditions too variable to allow useful photometry of the event. On the second night, the telescope enclosure was buffeted by wind and this resulted in the light from the satellites spreading over a relatively large area of the CCD during the exposures. A nearby star was used as a reference source as all the other satellites were on the other chip. A mutual eclipse was successfully detected in this case.

### 3. Data reduction

The images were reduced using the same method as in HCB08, namely subtraction of the planetary source followed by differential photometry between the satellite pair involved in the occultation or eclipse relative to a bright reference satellite, usually Titania. At the end of this process, the lightcurves were visually inspected to reveal whether a mutual event, as indicated by a dip, actually took place. Eight of our lightcurves showed convincing evidence of such a dip and were chosen for further analysis. These data are available from the authors upon request. It is worth noting at this point that, since we cannot separate the signal from the two satellites involved in an eclipse, we need to model their combined brightness. Hence, unlike the case in Arlot et al. (2008), our eclipse modelling, to be discussed shortly, depends on their albedo ratio.

The next stage in the analysis requires a model to estimate the time  $t_{\min}$  and distance  $b$  of closest approach between the two satellites on the impact plane as well as the ratio  $A$  of their albedos. We define the impact plane as the plane that (a) is perpendicular to the line connecting the Sun/Earth with the eclipsing/occulting satellite and (b) contains the uranicentric position of the eclipsed/occulted satellite at maximum eclipse/occultation respectively. Our occultation model is the same as the one used in HCB08; here we adopt the new terminology  $t_{\min}$ ,  $b$  and  $A$  instead of  $t_0$ ,  $x$  and  $a$  used in that paper. For the eclipses the same terminology is used, with the difference that now the eclipsing satellite is replaced by the intersection of its shadow cone with the impact plane. For the purposes of this work, the part of the



**Fig. 1.** Representation, on the impact plane (see text), of the model used to fit our mutual satellite eclipse data. The light lost from the eclipsed satellite (bold circle) is composed of the invisible part of the satellite in the umbra (circle of radius  $R_U$ ) and the fraction of light lost from each sector  $i$  of thickness  $\delta r$  and angular width  $\theta_i$  in the penumbra (ring of radius  $R_P - R_U$ ) at a distance  $r_i$  from the centre of the umbral cone. For clarity, the penumbra is depicted here as uniformly bright whereas in the model it is of radially-increasing brightness. The index  $i$  spans the area fraction of the satellite in the penumbra.

eclipsed satellite in the penumbra is divided into steps of thickness  $\Delta r$  and angular size  $\theta_i$  residing at a distance  $r_i$  from the centre of the shadow cone (see Fig. 1).

Solar illumination within each one of these steps is considered to be constant and equal to  $L_i$ , the fraction of the “virtual” or “reduced” sun (Aksnes 1974; Aksnes & Franklin 1976) that is not obstructed by the eclipsing satellite as seen from the eclipsed satellite. The “darkness” contributions  $1 - L_i$  from each step are then multiplied by the step areas  $r_i \delta r \theta_i$  and the (assumed uniform) satellite albedo to estimate the penumbral contribution to the loss of light. It is then added to the umbral contribution (equal to the satellite area within the umbral cone) to estimate the total dimming of the eclipsed satellite at a given instant in time.

For eclipses as well as for occultations, we do not take into account surface scattering (“limb darkening”) or phase effects. The latter is less than  $3^\circ$  in all cases and affects principally the determination of the impact parameter by a few tens of km or less (Arlot et al. 2008). Similarly, we do not take into account the light travel time between the two satellites which affects the determination of  $t_{\min}$  by a few seconds (see e.g. Noyelles et al. 2003).

## 4. Results

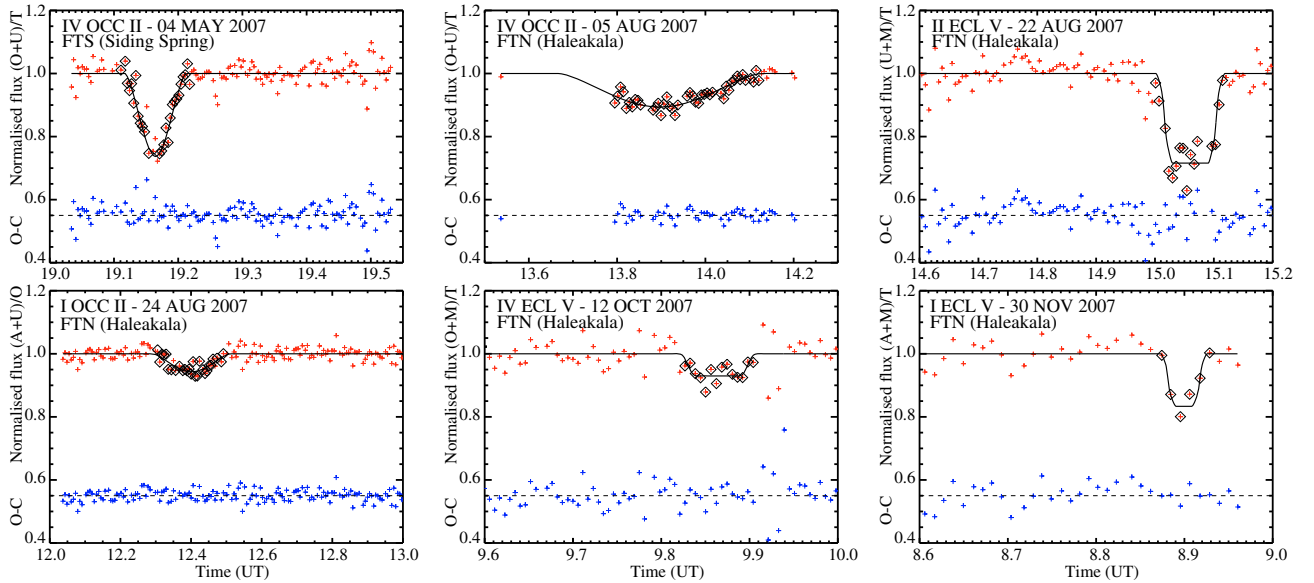
### 4.1. Positive observations

During model fitting we considered the relative satellite velocity on the sky plane to be fixed and equal to the one given by RJ07 (available through the HORIZONS ephemeris service; Giorgini et al. 1996). Initial estimates for the ratio  $A$  of the satellite albedos were calculated from Table V of Karkoschka (2001) by linear interpolation among the values nearest to the phase angles and wavelengths applicable to each event. This wavelength

**Table 3.** Best-fit estimates of the parameters of the mutual events successfully observed in this work.

Date (DDMMYY)	Event type	Obs. site	Midtime (UT)	Impact parameter (km)	Albedo ratio	Relative speed on impact plane (km s <sup>-1</sup> )	Mean rms of fit
040507	4O2P	FTS	19:09:53 ± 3	400 ± 70	1.229 <sup>a</sup> ± 0.1	7.078 <sup>a</sup>	0.031
050807	4O2P	FTN	13:53:49 ± 30	850 ± 30	1.238 <sup>a</sup> ± 0.1	1.225 <sup>a</sup>	0.019
140807	2O4P	ATH1	01:34:25 ± 28	750 ± 160	0.813 <sup>a</sup> ± 0.1	5.765 <sup>a</sup>	0.083
220807	2E5T	FTN	15:03:37 ± 5	0 ± 60	0.410 ± 0.025 (0.617)	3.647 <sup>a</sup>	0.039
240807	1O2P	FTN	12:24:04 ± 30	840 ± 30	1.833 <sup>a</sup> ± 0.1	2.210 <sup>a</sup>	0.018
121007	4E5T	FTN	09:51:53 ± 2	410 <sup>+150</sup> <sub>-410</sub>	1.271 <sup>+0.55</sup> <sub>-0.28</sub> (0.759)	5.179 <sup>a</sup>	0.042
301107	1E5T	FTN	08:53:58 ± 2	310 <sup>+90</sup> <sub>-130</sub>	0.830 <sup>+0.22</sup> <sub>-0.14</sub> (1.216)	7.403 <sup>a</sup>	0.040
301107	3E4P	SALT	18:47:36 ± 5	260 ± 150	1.113 <sup>a</sup> ± 0.1	1.992 <sup>a</sup>	0.032

<sup>a</sup> These parameters have been assumed and kept fixed during the fitting process.

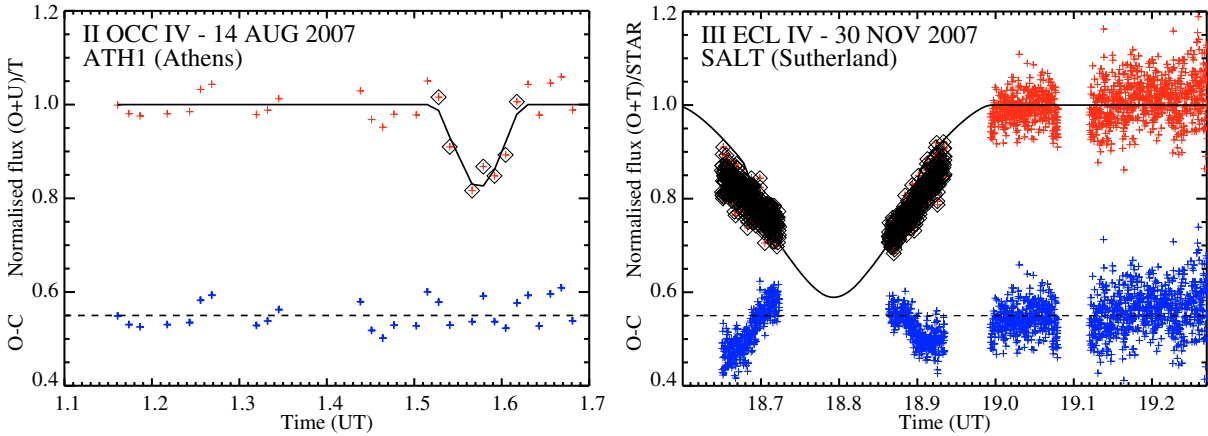


**Fig. 2.** Model fit (black curve) to observations (red “+” signs) acquired from Faulkes Telescopes North (FTN) and South (FTS). Diamonds indicate the data points used in the fit. Residuals (blue “+” signs) are referenced to the datum provided by the dashed horizontal line.

of “peak sensitivity” was assumed to be 770 nm (the same of that of the sds *i'* filter used by FTN and FTS) in all cases. Due to the high degree of correlation between the albedo ratio and impact parameter in fitting occultations (see HCB08), the albedo ratio *A* was kept fixed at its initial value and only  $t_{\min}$  and *b* were allowed to vary. On the other hand, simultaneous fitting of  $t_{\min}$ , *b* and *A* was possible for three out of the four eclipse lightcurves. To maintain consistency, we also re-reduced the 4th May event reported in HCB08 with an updated set of a priori parameters. The fit results for all eight events are shown in Table 3. Numbers shown in brackets are albedo ratio estimates from Karkoschka (2001) used here as starting values for the fit. All estimated errors are formal 1- $\sigma$  uncertainties. Associated lightcurves and best-fit models are shown separately for the FTN/FTS (Fig. 2) and SALT/Athens (Fig. 3) observations. Typical root-mean-square (rms) of the modelled vs. observed data points ranged from 2% to 4% with the exception of the 2O4P event on 14/08/2007 for which a fit rms of 8% was obtained. The SALT data of 30/11/2007 show evidence of significant systematic errors, likely due to marginal observing conditions and the lack of a bright reference source on the chip that contained the Oberon/Titania pair. Hence we have kept *A* fixed and only allowed particular segments of the data to be considered in the fitting process in order to enable an acceptable fit.

Some interesting features appear in this set of estimates, particularly those for the eclipses. A central (i.e.  $b = 0$ ) configuration for the 4E5T event observed on 12/10/2007 cannot be rejected at the 1- $\sigma$  level. The initial estimate of *A* for that event is just outside the 3- $\sigma$  contour around the best-fit value in the *A* vs. *b* plot of the  $\chi^2$  goodness-of-fit statistic (see HCB08 for details). It is well outside the 3- $\sigma$  contour for the 2E5T event observed on the 22/08/2007 and lies on the 2- $\sigma$  contour for the 1E5T event observed on the 30/11/2007. One explanation for this discrepancy between predictions and observations could be that, since the satellite hemispheres visible to the Earth at the time of the observations contained areas not in view during the 1997 observations used by Karkoschka (2001), we are seeing the effects of albedo variations that have only recently been illuminated by the Sun. Alternatively, our formal uncertainties may have underestimated the actual photometric errors, for example if the proximity of Miranda to Uranus somehow introduced systematics in our measurements.

These data can be used to gauge the precision of the available ephemerides of the satellites. Although definitive statements on this issue must await future analysis of the complete set of observations acquired by various groups in the course of this international campaign, we can take advantage of the relatively large number of events reported in this work by looking at



**Fig. 3.** Model fit to observations acquired from Athens (ATH1; left panel) and Sutherland (SALT; right panel). Notation is as in Fig. 2.

**Table 4.** Calculated vs. observed (C–O) midtime residuals for the ephemerides considered in this paper.

Date (DDMMYY)	Event type	Obs. site	Fitted midtime (UT)	C–O sec (km) (GUST86)	C–O sec (km) (LA06)	C–O sec (km) (RJ07)
040507	4O2P	FTS	19:09:53	–142 (–1010)	–16 (–110)	–34 (–240)
050807	4O2P	FTN	13:53:49	–149 (–180)	+137 (+170)	+19 (+20)
140807	2O4P	ATH1	01:34:25	–177 (–1020)	–40 (–230)	–77 (–440)
220807	2E5T	FTN	15:03:37	–148 (–540)	–47 (–170)	–33 (–120)
240807	1O2P	FTN	12:24:04	–197 (–440)	–81 (–180)	–57 (–130)
121007	4E5T	FTN	09:51:53	–117 (–610)	–42 (–220)	–77 (–400)
301107	1E5T	FTN	08:53:58	–24 (–180)	–35 (–260)	–31 (–230)
301107	3E4P	SALT	18:47:36	–124 (–250)	+69 (+140)	–34 (–70)
Median C–O				–145 (–480)	–38 (–180)	–34 (–180)

the statistics of the best-determined parameter, namely the midtime  $t_{\min}$ . In Table 4 we present the offsets between the observed midtimes and those predicted by models using GUST86, LA06 and RJ07. The numbers in brackets provide the same quantities in km using the speeds from Table 3. It is evident that the two latter ephemerides performed a factor of 3–4 better than the Voyager-era GUST86 in reproducing the satellite-to-satellite positions (along their relative sky velocity vector) to 180 km or 0.013 arcsec. It is also apparent that the LA06 and RJ07 offsets are not randomly distributed between positive and negative values but instead indicate that the observations lag behind the predictions by a few hundred km. This finding is in accordance with the observations of a single eclipse of Titania by Umbriel reported by Arlot et al. (2008) and four events involving Ariel, Umbriel, Titania and Oberon reported by Miller & Chanover (2008). We view this as evidence that new information about the Uranian satellite system is contained in the acquired measurements, in accordance with the expectations of Christou (2005) and Arlot et al. (2006).

The final step in our analysis is the conversion of our fitted set of parameters to satellite positions in a celestial coordinate system. For these purposes the necessary frame rotations were calculated using vectors from RJ07 available through HORIZONS. In Table 5 we provide the results in the form of (a) intersatellite positions – occulted (eclipsed) satellite relative to the occulting (eclipsing) satellite – in the J2000 Earth Equatorial frame at time  $t_{\min}$  (Cols. 4 and 5); and (b) offsets between these positions and those generated by RJ07 at the same time as  $t_{\min}$  (Cols. 6 and 7). It is important to note that these are impact plane coordinates; in other words, while the positions derived for occultations are Earth-centred, those derived from eclipses are Sun-centred with  $t_{\min}$  referring to the moment of

maximum eclipse as observed from the Sun. Hence these times are different than those given in Tables 3 and 4.

#### 4.2. Negative observations

Seven of our observations resulted in lightcurves that did not show obvious signs of a photometric dip. In the case of the 051007 observation, image acquisition began too late to cover the main interval of interest fully or partially. For the remaining six, a dip was expected to occur at various degrees of confidence. These are summarised in Table 6. Column 4 gives the fraction of the event, as predicted by RJ07, that overlapped with the time interval covered by our observations. Column 5 gives the statistical variation of our photometric measurements about the mean, normalised to 1, for each observation. The three last columns give the expected *R*-band flux drop according to GUST86, LA06 and RJ07 respectively.

We can gauge the significance of those negatives by using the criterion of Birlan et al. (2008). Those authors concluded that a brightness drop of a magnitude similar to the measurement uncertainty cannot be reliably established from the data. In Table 6 we see that the predicted flux drop was smaller than, or equal to, the measurement uncertainty for the events 200807, 220907 and 211007. In contrast, the measurement uncertainties were 40% and 20% of the smallest predicted drop in the 260707 and 060807 events respectively. Hence, those last two events do contain information on the satellites' position and future ephemerides of the satellites must be able to reproduce these negative results.

It is interesting that these two cases are partial events involving Miranda. Taking our positive observations of total eclipses

**Table 5.** Satellite-satellite relative positions and O–C residuals on the impact plane as determined from our observations in equatorial J2000 coordinates.

Date (DDMMYY)	Event type	Fitted midtime (UT)	Relative position (″)		O–C (″)	
			$\Delta\alpha \cos \delta$	$\Delta\delta$	$\Delta\alpha \cos \delta$	$\Delta\delta$
040507	4O2P	19:09:53	−0.0256 (±0.0037)	−0.0069 (±0.0015)	+0.0042	+0.0181
050807	4O2P	13:53:49	−0.0587 (±0.0024)	−0.0167 (±0.0026)	+0.0070	+0.0003
140807	2O4P	01:34:25	−0.0517 (±0.0112)	−0.0141 (±0.0116)	+0.0070	−0.0319
220807	2E5T	15:11:37*	0.0000 (±0.0031)	0.0000 (±0.0013)	−0.0149	+0.0030
240807	1O2P	12:24:04	+0.0585 (±0.0019)	+0.0157 (±0.0041)	−0.0012	+0.0097
121007	4E5T	09:58:53*	+0.0280 ( <sup>+0.0052</sup> <sub>−0.0059</sub> )	−0.0025 (±0.0005)	+0.0012	+0.0205
301107	1E5T	08:55:10*	−0.0208 ( <sup>+0.0036</sup> <sub>−0.0033</sub> )	+0.0044 (±0.0008)	−0.0044	+0.0244
301107	3E4P	18:48:44*	+0.0178 (±0.0046)	−0.0026 (±0.0007)	−0.0106	−0.0046

\* Midtime of the event as observed from the centre of the Sun. Earth midtimes for these events are given in Table 3.

**Table 6.** Circumstances of those observations which gave negative results.

Date (DDMMYY)	Event type	Obs. site	Cov.	Meas. rms	Predicted flux drop		
					(GUST86)	(LA06)	(RJ07)
260707	1E5P	FTS	1.0	0.021	0.111	0.048	0.050
060807	1O5P	FTN	1.0	0.022	0.126	0.130	0.154
200807	5O2P	FTN	0.7	0.130	0.050	0.103	0.087
220907	1E5P	ATH2	1.0	0.224	0.130	0.080	0.086
211007	1E2P	FTS	1.0	0.030	0.033	—	0.007
221007	1E2C	FTS	—	0.043	—	—	—

Dashes (“—”) indicate that the event was expected to be a miss by the respective model.

into account, a possible interpretation is that Miranda is out of position by an amount sufficient to cause a miss of a partial event, but not of a total one. Such an effect may, for example, be caused by an offset in the inclination and longitude of the ascending node of that satellite. Future processing of all the mutual event data amassed during the past Uranian equinox should determine if this is indeed the case.

## 5. Conclusions

In this paper we have presented the results of a multi-instrument, multi-group effort as part of a broader international campaign to capture the never-before-observed mutual events between the satellites of the planet Uranus. Eight such events, four eclipses and four occultations, were successfully detected and reduced to precise intersatellite positions. Three of the eclipses reported involve the faint satellite Miranda, traditionally a difficult target for conventional astrometry due to its proximity to Uranus. Two additional observations yielded negative results above the noise, at variance with the predictions. The result of our data reduction procedure is a set of high-precision intersatellite positions. Our formal uncertainties are several times smaller than typical values for post-Voyager ground-based satellite-satellite astrometry (Jones et al. 1998; Veiga & Vieira Martins 1999; Shen et al. 2002). It is also noteworthy that, within the limitations of small number statistics, our rate of success was largely independent of the aperture used, 50% in all cases. In our opinion, thorough planning (e.g. matching specific events to individual instrument capabilities) and instrument/detector operational flexibility were the main contributing factors to the successful outcome of this programme. In particular, it highlights the ability of moderate aperture instruments to carry out challenging observations.

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