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Practical galaxy morphology tools from deep supervised representation learning

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ABSTRACT

Astronomers have typically set out to solve supervised machine learning problems by creating their own representations from scratch. We show that deep learning models trained to answer every Galaxy Zoo DECaLS question learn meaningful semantic representations of galaxies that are useful for new tasks on which the models were never trained. We exploit these representations to outperform several recent approaches at practical tasks crucial for investigating large galaxy samples. The first task is identifying galaxies of similar morphology to a query galaxy. Given a single galaxy assigned a free text tag by humans (e.g. ‘#diffuse’), we can find galaxies matching that tag for most tags. The second task is identifying the most interesting anomalies to a particular researcher. Our approach is 100 per cent accurate at identifying the most interesting 100 anomalies (as judged by Galaxy Zoo 2 volunteers). The third task is adapting a model to solve a new task using only a small number of newly labelled galaxies. Models fine-tuned from our representation are better able to identify ring galaxies than models fine-tuned from terrestrial images (ImageNet) or trained from scratch. We solve each task with very few new labels; either one (for the similarity search) or several hundred (for anomaly detection or fine-tuning). This challenges the longstanding view that deep supervised methods require new large labelled data sets for practical use in astronomy. To help the community benefit from our pretrained models, we release our fine-tuning code zoobot. Zoobot is accessible to researchers with no prior experience in deep learning.

Key words: methods: data analysis – software: data analysis – software: public release – galaxies: evolution – galaxies: general.

1 INTRODUCTION

The core of many machine learning approaches is learning to calculate useful representations, i.e. lower dimensional summaries of images or other data with which a prediction can be made. Learning hierarchical representations, where the representation learned by one layer becomes the input to the next, is the cornerstone of deep learning. Representations are particularly important for words and images, where the input feature space is high dimensional and thus more difficult to make direct predictions with than, for example, typical tabular data (Le-Cun, Bengio & Hinton 2015; Goodfellow, Bengio & Courville 2016).

To date, astronomers have typically set out to solve supervised machine learning problems by creating their own representations from scratch. They often train a randomly initialized model only on the labelled data they are directly interested in. This is often true even for researchers solving similar tasks with similar methods on similar data sets. For example, distinguishing between early- and late-type galaxies in SDSS imaging (Domínguez-Sánchez et al. 2018; Khalifa et al. 2018; Fischer, Domínguez-Sánchez & Bernardi 2019; Khamtsov et al. 2019; Barchi et al. 2020; Variawa, van Zyl & Woolway 2020; Walmsley et al. 2020). The expressivity of each model is limited by the size of the training data (to prevent overfitting) which in turn limits performance on complex tasks requiring such
expressivity. We aim to demonstrate in this paper that, under certain conditions, starting from a representation learned elsewhere is more effective; specifically, that exploiting representations learned while solving a broad set of galaxy morphology tasks can dramatically improve performance on new morphology tasks.

We are primarily motivated by results from the natural language community. Recent empirical research suggests that the performance of deep natural language models with Transformer architectures follows fundamental scaling relations (Vaswani et al. 2017). Broadly speaking, performance increases approximately as a power law with respect to the number of model parameters, the size of the training data set, and the computational budget (Kaplan et al. 2020). For example, increasing the number of model parameters will likely increase performance provided one has access to effectively unlimited data and compute. Most researchers have neither, and so the best-performing models are increasingly created by a few well-resourced groups such as OpenAI (Brown et al. 2020) and Google Brain (Fedus, Zoph & Shazeer 2021). These natural language models are trained to predict masked words in sentences (along with related tasks) and so effectively all digitized writing is useful training data. This style of training is known as ‘self-supervised’ as the model is trained in a supervised manner on labels (masked words) already present in the data itself. Having learned an effective representation of language, the models can then be fine-tuned, i.e. gradually adapted with additional data, on so-called domain tasks: tasks of practical interest such as summarizing news articles, coding websites, or understanding emotion (Kant et al. 2018; Yang et al. 2020b; Austin et al. 2021). Crucially, because the fundamental language representation is already learned, fine-tuning achieves state-of-the-art performance using far more modest data and compute than training from scratch.

Could such an approach work for galaxy morphology? Can we train models on large data sets of galaxy images and then use the learned representations as a starting point to solve new practical morphology tasks? Convolutional neural networks (CNNs), the now-standard approach for classifying galaxy images, likely follow similar scaling laws (Sharma & Kaplan 2020). It is possible to train a CNN on images in an analogous self-supervised manner by predicting pixel values (generative learning, e.g. Van Den Oord et al. 2016) or by enforcing that randomly transformed images retain similar representations (contrastive learning, e.g. Chen et al. 2020). In astronomy, this is typically done in the context of solving a particular task (Sarmiento et al. 2021; Zanisi et al. 2021), though recent work by Hayat et al. (2021) uses self-supervised learning to learn galaxy representations explicitly for generic downstream tasks.

One important drawback to self-supervised methods, and unsupervised methods more broadly, is that the representations must be learned directly from image pixel values and so it is difficult to create representations informed by our physical understanding of the world. We believe this may lead to predictions that do not make physical sense. For example, Buncher, Sharma & Carrasco Kind (2021), aiming to predict how a shallow galaxy image would appear in a deeper survey, found their unsupervised generative model would fill in large artefacts in the original images with a plausible sky background. Spindler, Geach & Smith (2020) found their unsupervised generative model clustered galaxies according to whether they have a background partner galaxy in the top or bottom corner of the image. Contrastive learning allows a degree of physics input through the choice of augmentations, but these are typically limited to basic invariances (e.g. flips, rotations, added noise, etc). We would prefer a representation informed by our human understanding of an image, beyond the raw pixels themselves: a representation that ‘understands’ that a background partner galaxy is not scientifically relevant.

Supervised methods present an alternative way to learn representations. Their representations are optimized for the supervised task and so are more strongly influenced by human labels, which are designed to focus learning on the most scientifically relevant aspects (e.g. bars, arms, etc.). One is then faced with the apparent dilemma of learning a representation using either self-supervised approaches with near-limitless data but limited physical understanding, or supervised approaches with less data but scientifically relevant labels.

To minimize the number of labels required to learn meaningful representations from supervised approaches, one can exploit existing labelled data sets. Pretraining on ImageNet (Russakovsky et al. 2015), a relatively1 diverse benchmark data set containing images of 1000 terrestrial classes, is particularly common in the computer science literature (Marmanis et al. 2016; Tschandl, Sinz & Kittler 2019; Mathis et al. 2020; Ridnik et al. 2021). Astronomers have recently experimented with pretraining on ImageNet to better solve astronomical tasks. Ackermann et al. (2018) and Martinazzo, Espadoto & Hirata (2020) each measured the performance on galaxy-morphology-related tasks of CNNs either initialized randomly or pretrained on ImageNet. In both cases, the ImageNet-pretrained CNN performed significantly better. Additionally, Wu et al. (2018) noted that using frozen ImageNet weights for the first four layers of their CNN improved performance for cross-matching sources given a fixed amount of training time.2 Astronomers have also found success with pretraining CNNs on a previously labelled survey and used them to solve the same task for a new survey: Dominguez Sanchez et al. (2019) pretrained on SDSS and fine-tuned to DES, Pérez-Carrasco et al. (2019) pretrained on CANDELS and fine-tuned to CLASH, and Tang, Scaife & Leahy (2019) pretrained on NVSS and fine-tuned to FIRST (and vice versa).

We hypothesize that ImageNet pretraining works well for new terrestrial tasks because the classification task is broad (i.e. distinguish 1000 classes including ‘toilet paper’ and ‘triceratops’) and so the representation is likely to be appropriate for new terrestrial classes, but will work less well for galaxy morphology tasks because the terrestrial-trained representation is less appropriate. ImageNet classes have dramatically different shapes, textures and signal-to-noise levels than galaxies, and so only the most basic representations (edges, curves, etc., detected by the first convolutional layers, He et al. 2019) are likely to be useful. On the other hand, we believe that while pretraining on other galaxy surveys is helpful because the representations learned will be appropriate for galaxy images, the classification task is narrow (e.g. distinguish mergers from non-mergers) and so the representations are likely to be specific to that task.

The core argument of this paper is that general purpose supervised galaxy morphology representations would be better learned from solving a broad galaxy morphology task. These representations would be both more relevant to galaxy images than are learned from ImageNet (which is comprised of terrestrial images) and more widely applicable to new morphology tasks than

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1 As compared to other benchmark data sets e.g. MNIST, CIFAR10. Diversity in ImageNet is the subject of significant attention (e.g. Recht et al. 2019; Yang et al. 2020a), in part because of its widespread use.

2 This does not necessarily imply improved performance at convergence, however, as pretrained models may converge faster (He, Girshick & Dollár 2019).
representations learned from a single narrow morphology task (as in previous work).

We argue that the models trained by Walmsley et al. (2022) on Galaxy Zoo DECaLS have learned to answer just such a broad task and thus provide ideal cross-task representations. The Galaxy Zoo DECaLS project asked volunteers on www.galaxyzoo.org a diverse set of questions designed to capture the essential phenomenological features of galaxy morphology such as bars (strong and weak), spiral arms (counts, winding), bulge size, inclination, and so forth. Models were then trained to answer these diverse questions. To do so, the models learned to create general representations suitable for morphology tasks beyond the questions themselves, just as ImageNet classifiers learn general representations for terrestrial tasks beyond identifying the ImageNet classes.

We first investigate the DECaLS models’ representations and show that visually similar galaxies are mapped to similar parts of feature space, even for morphology aspects not explicitly measured by the Galaxy Zoo questions (Section 2). We then go on to use that representation to develop and demonstrate practical scientific tools for similarity searches (Section 2.4), anomaly detection (Section 3), and transfer learning (Section 4). We share our code and data in Data Availability Statement Section.

2 REPRESENTATIONS AND VISUAL SIMILARITY

Image representations are crucial for many practical tasks of interest to astronomers. An image representation function maps the information content of a high-dimensional image to a lower dimensional vector. A useful representation should allow for the definition of a meaningful distance metric, i.e. similar images should be closer in representation space than dissimilar images, and small changes to an image should lead to small changes in the representation and vice versa.

In this section, we present evidence that the GZ DECaLS models trained in Walmsley et al. (2022) (hereafter W+22) learn such a representation for galaxies. We then use that representation to introduce a method for identifying objects that are similar to a user-selected query galaxy, and demonstrate the method’s effectiveness on a diverse and independently selected set of galaxies.

2.1 Data

Throughout this paper, we experiment with galaxies sourced from the Dark Energy Camera Legacy Survey (DECaLS) DR5 (Dey et al. 2019). The selection and image acquisition process is described in detail in W+22. Briefly, galaxies are selected from the NASA-Sloan Atlas v1.0.1 (Albareti et al. 2017) if they have an angular radius of petrotheta \( \geq 3 \) arcsec and have been observed by DECaLS in the \( g \), \( r \), and \( i \) bands as of DR5. FITS images are downloaded from the DECaLS cutout service at native telescope resolution with the visible sky area set according to galaxy angular radius, interpolated to 424 \times 424 pixel thumbnails, and finally rescaled and colourised for human viewing on Galaxy Zoo.

Unlike GZ DECaLS, we apply an \( r \)-band magnitude cut of \( 14.0 \leq r \leq 17.77 \). The fainter limit ensures galaxies are within the bulk of the population with SDSS spectroscopy (Albareti et al. 2017) and the brighter limit excludes galaxies with unreliable radii measurements and fields saturated by nearby stars. We also exclude galaxies flagged as likely to be incorrectly sized due to photometric errors in the NASA-Sloan Atlas (see W+22). The resulting catalogue includes 305,657 galaxy images.

For our anomaly detection algorithm (Section 3), to directly compare our performance with that of Astromnomal (Lochner & Bassett 2021), we also experiment with the 60,000 Galaxy Zoo 2 images shared as a public training set for the Kaggle ‘Galaxy Challenge’ competition.4 The construction and selection of these images is described in Willett et al. (2013) and Dieleman, Willett & Dambre (2015), respectively.

2.2 Calculating representations

The trained GZ DECaLS models must internally represent galaxies in a way that is appropriate for predicting the answers to GZ DECaLS questions. Here, we describe how we extract those representations. The procedure is essentially identical to making predictions, except that we save the activation values before the final layer rather than the predictions themselves.

Galaxy images are passed to the model following the same procedure with which the model was trained, described in detail in W+22. Briefly, images are converted to grey-scale, resampled from 424 to 300 pixels on a side, and then cropped about a random centroid to 224 pixels across (effectively zooming the image by 25% per cent). This provides an image with an appropriate field of view and with input dimensions matching those for which our chosen model architecture was designed. Each time an image is loaded into memory, it is uniquely augmented with an aliased rotation through a random angle and randomly selected horizontal and vertical flips.

W+22’s models use the EfficientNetB0 architecture (Tan & Le 2019). EfficientNet is composed of a series of mobile inverted bottleneck blocks (Sandler et al. 2018), comparable to standard convolution and pooling blocks. These stacked blocks are followed by a 1 \( \times \) 1 convolutional layer (Szegedy et al. 2015) with 1280 filters, the output of which is global average-pooled (i.e. each filter is replaced with the mean of that filter’s activations) for a 1280-dimensional vector. This vector is what we refer to throughout as the learned representation. In normal use, this vector would form the input for the final dense layer, and the outputs of that dense layer would be interpreted as the model predictions. Here, however, we remove the final dense layer and directly record the 1280-dimensional internal representation.

Unlike W+22, which was concerned with predicting well-calibrated posteriors for galaxy morphologies, we do not use dropout or model ensembling to marginalize over the network weights. Instead, we use a single forward pass from a single model. Marginalizing might in principle improve performance by removing feature-space noise from the specific weights and augmentations used, but the effect of averaging representations is unclear and so we defer this to future work. We use the weights of a GZ DECaLS model trained on all labelled galaxies (i.e. both training and validation sets) and used by W+22 as part of the ensemble for creating the GZ DECaLS automated catalogue. We refer to this model as ‘the DECaLS model’ in this work.

In this section (for similarity searches) and the following section (Section 3, for anomaly detection), we treat the representation as fixed and therefore precalculate and store the representation for each galaxy. We do not need to make any further CNN predictions

\[^3s = \max(\min(p_{90} \times 0.04, p_{90} \times 0.02), 0.1)\], where petro50 and petro90 are the NSA columns measuring 50 and 90 per cent Petrosian radii.

\[^4https://www.kaggle.com/c/galaxy-zoo-the-galaxy-challenge/data\]
when our methods are applied, removing the significant time and hardware requirements typically associated with applying CNN. In Section 4, we investigate fine-tuning the representation for improved performance.

2.3 Visualizing

We use the dimensionality reduction algorithm umap (McInnes et al. 2018) to visualize the representations learned by the DECaLS model. umap attempts to balance local and global structure (i.e. distances to close neighbours versus far neighbours) when compressing a higher dimensional space. umap is commonly used for visualising high-dimensional spaces in both computer science and astronomy (e.g. Clarke et al. 2020; Reis et al. 2021).

We assume that the 1280-dimensional \( D = 1280 \) representation includes some redundant information because we imposed no independence requirements or weight decay during network training. We therefore first compress the representation space with incremental principal component analysis (Ross et al. 2008) to \( D = 15 \) while preserving 98 per cent of the initial variation. We find this gives more compelling visualizations than using umap directly.

Having compressed the representation from \( D = 1280 \) to \( D = 15 \) with incremental PCA and then to \( D = 2 \) with umap, we can inspect how the representation corresponds to visual appearance by showing galaxy thumbnails located according to their position in the compressed representation. Fig. 1 shows the result for all galaxies. The effect of visual appearance is clear: smooth ellipticals occupy the upper corner, flocculent spirals occupy the lower left, rings and

Figure 1. Visualization of the representation learned by our CNN, showing similar galaxies occupying similar regions of feature space. Created using Incremental PCA and umap to compress the representation to 2D, and then placing galaxy thumbnails at the 2D location of the corresponding galaxy.
diffuse discs occupy the lower centre, and edge-on-discs occupy the right corner. Online Figs A1 and A2 show equivalent plots for galaxies filtered (using the GZ DECaLS automated vote fractions from W + 22) to include only featured or spiral galaxies, respectively, and show similarly striking visual arrangements within each class.

We conclude that even after compression from \( D = 1280 \) to \( D = 2 \), visual similarity strongly affects location in representation space. In the following section, we exploit this representation to identify visually similar galaxies.

2.4 Similarity searches

Automatically quantifying the similarity of two galaxies is a longstanding but elusive goal. The most obvious use for quantified similarity is searching for counterparts to known rare objects. The serendipitous discovery of qualitatively new sources such as Hanny’s Voorwerp (Lintott et al. 2009) raises the inevitable question ‘are there more?’ Effective searches for the most similar galaxies (Ardizzone, Di Gesù & Maccarone 1996; Csillaghy, Hinterberger & Benz 2000; Abd El Aziz, Selim & Xiong 2017) allow us to make the leap from a one-off curiosity to a new class of objects. Quantifying similarity is also foundational to any effort at creating automated clusters or taxonomies of galaxies, a topic of much recent interest (Schutter & Shamir 2015; Hocking et al. 2018; Ralph et al. 2019; Spindler et al. 2020; Cheng et al. 2021). The hope is that automated analysis of large-scale modern surveys will reveal galaxy populations that are more objective, and perhaps better connected to the underlying physics of galaxy formation, than the Hubble sequence and its extensions.

What makes two galaxies similar? Physically meaningful similarity implies not just similar pixels but similar morphology. Our representations provide a new opportunity for measuring morphological similarity. Since galaxies of similar morphology have similar representations, we can use the distance in representation space as an estimate of similarity. We can therefore retrieve the most similar galaxies to a given galaxy simply by listing its nearest neighbours in representation space.

Identifying nearest neighbours in the \( D = 1280 \) CNN representation is computationally expensive, even with efficient algorithms like sklearn’s KDTree. For convenience, we reduce the dimensionality using Incremental PCA (as we did prior to applying \texttt{umap} in Section 2.3 above). Any choice of PCA dimensionality above \( D \geq 10 \) (84 per cent variance preserved) has a minimal effect on the 50 closest neighbours, while reducing the dimensions from \( D = 1280 \) to \( D = O(10) \) reduces the time per search from \( O(h^5) \) to \( O(s) \). We use \( D = 10 \) here.

We choose the Manhattan distance \( \sum |p_i - q_i| \) as our distance metric, implying that similarity is linearly proportional to distance. The Manhattan distance is theoretically preferable to the Euclidean distance for nearest-neighbour searches in high dimensions (Aggarwal, Hinneburg & Keim 2001). We also experimented with the Euclidean distance and could not confidently identify a qualitative difference in the similarity of the galaxies returned using each distance metric.

The Galaxy Zoo Talk forum\(^6\) provides an independent and diverse selection of galaxies with which to test our similarity search. When writing forum posts about galaxies, Galaxy Zoo volunteers can choose to use ‘tag’ phrases prefaced with a hash, e.g. ‘#starforming’, analogously to Twitter hashtags. For each of the most commonly used tags (‘#starforming’, ‘#disturbed’, etc.), we use the galaxy most commonly given that tag as our query galaxy and search for similar galaxies in our compressed \( D = 10 \) representation space.

The results from those similarity searches are shown in Fig. 2. We successfully find similar galaxies in almost all cases. This includes cases like ‘#dustlane’ where the feature in question is highly specific; most of the returned galaxies are not just edge-on-spirals but edge-on-spirals with dust lanes.

These searches are representative of the typical performance of our method. We do not ‘cherry-pick’ the searches with the best outcomes. We only exclude tags for being related to data not in the image (‘#agn’, ‘#decal’, etc.) or being directly equivalent to a decision tree question (‘#spiral’, ‘#merging’, etc.). Tags have also been grouped semantically (e.g. ‘#dust-lane’ to ‘#dustlane’, ‘#ringed’ to ‘#ring’, etc.). Fig. 2 otherwise simply shows searches for the most popular 18 tags.

We emphasize that the DECaLS model was not explicitly trained on any of these tags. The model was only trained to predict volunteer votes to the (different) questions in the GZ decision tree (see W + 22). In these similarity searches, the model is identifying similar objects based on only a single example: the query galaxy itself. In computer science terminology, the model is performing one-shot learning on a fixed embedding (Fei-Fei, Fergus & Perona 2006).

The occasional failures help us understand what the model can and cannot recognize, which speaks to model interpretability. For example, with the ‘#overlapping’ example, the volunteers are likely referring to the small companion galaxy (centre left) but the search returns additional irregular galaxies rather than additional galaxies with small companions. The similarity search is more successful at ‘#diffuse’ where the query image includes a pair of substantially sized galaxies and the search returns similar interacting pairs. We can infer that the DECaLS model likely focuses on the main galaxies in the image and has a lower limit for how small (in angular size) a background galaxy can be to affect the representation.

The ‘#asteroids’ example, where volunteers selected the image due to the small colourful speckle, also illustrates this effect. Further, the model is only provided grey-scale images, and so could not identify similar colourful speckles even without the size issue above. One could address the lack of sensitivity to colour by training on colour images, at the cost of potential bias for users who prefer a colour-insensitive similarity search (e.g. for investigating links between morphology and star formation).

We provide a public interface to our similarity search at https://share.streamlit.io/mwalmsey/decals_similarity/main/similarity.py. Users enter the coordinates of their desired query galaxy which are then matched to the closest-on-sky DECaLS galaxy in our sample. Images and a table of the most similar galaxies are then returned. Code and instructions for a self-hosted version are available at https://github.com/mwalmsey/decals_similarity.

3 FINDING INTERESTING ANOMALIES

3.1 Context

We showed in Section 2.4 that if we have a single example galaxy, we can find similar examples. But what if we don’t know what we are looking for?
Figure 2. Similarity search results for the most common volunteer tags (on which the model was not trained). The query galaxy (left, green border) is the galaxy for which the volunteers most used that tag. The other galaxies on each row are those expected by the DECaLS CNN to be most similar i.e. with the least separation to the query galaxy in representation space. The repeated ‘overlapping’ galaxy is not an error; the background and foreground galaxies are both independently listed in the catalogue and identified as similar. Similarity search results for the most common volunteer tags (on which the model was not trained). The query galaxy (left, green border) is the galaxy for which the volunteers most used that tag. The other galaxies on each row are those expected by the DECaLS CNN to be most similar i.e. with the least separation to the query galaxy in representation space.
Many fundamental insights have been driven by rare objects found serendipitously in ‘big data’ catalogues (Cardamone et al. 2009; Welsh et al. 2011; Boyajian et al. 2016). Such searches may be assisted by machine learning methods aimed at identifying rare objects (e.g. Henrion et al. 2013; Baron & Poznanski 2017; Storey-Fisher et al. 2021). However, not all rare objects are useful. Instrumental artefacts, completely smooth ellipticals, and highly disturbed post-mergers are all ‘anomalous’ in the technical sense of
deviating from the typical distribution of images. Only some of these will be valuable to the user. It is therefore crucial that any automated search for anomalies takes into account the user’s interests.

Finding interesting anomalies guided by user feedback is the focus of the computer science subfield of active anomaly detection (Kong et al. 2020). Previous work has considered various schemes where traditional unsupervised anomaly detectors (e.g. Isolation Forests, Liu, Ting & Zhou 2008) are coupled to user feedback in an active learning loop where the algorithm identifies rare data points, those rare data points are rated for interest, and a supervised algorithm is trained based on those ratings (Pelleg & Moore 2004; Das et al. 2017; Siddiqui et al. 2018). The recently introduced software package Astronomaly (Lochner & Bassett 2021, hereinafter LB21) applies this approach in an astronomical context.

Astronomaly has two parts: the first is a browser interface where users can express their interest in images or 1D data; the second is a set of data processing components which can be configured to extract features, identify rare datapoints, and model user interest. Together, they can be used to apply the active learning loop described above to galaxy images, spectra, light curves etc.

Astronomaly is intended as a general anomaly finding framework which astronomers can extend to suit their specific science goals. Here, we show how several extensions motivated by our new galaxy representations make an Astronomaly style approach significantly better at identifying merging galaxies, as measured on the benchmark task introduced by LB21. We then show how our improved approach can also find mergers, rings and irregular galaxies in the DECaLS survey.

3.2 Method

In this section, we develop a method to search our CNN representation for anomalies likely to be interesting to a specific user. We build a model of interest as a function of representation by intelligently asking that user about their interest in the galaxies which they think will help to identify real detections, and then predict their interest in every galaxy to estimate which galaxies they most care about.

We will contrast our method with the specific method used by LB21 to demonstrate the quantitative performance of Astronomaly on Galaxy Zoo 2 data, which we will simply call ‘Baseline’. We describe the task itself and compare results in Section 3.3.1. Baseline is a particular choice of Astronomaly components designed to work well with this galaxy morphology task while being simple and applicable to other images.

The general approach of Astronomaly (as in LB21) is as follows. Galaxy images are converted to features and ranked by rarity. The rarest galaxies are rated by the user according to personal interest. A regression model is fit to these rare galaxies of known interest to predict interest for all other galaxies. Finally, the predicted user interest is combined with the machine learning rarity scores to find galaxies with both high expected interest and high rarity i.e. interesting anomalies. Those top galaxies themselves can then be rated to continue the active learning cycle of labelling, estimating interest, and choosing new galaxies to label.

LB21’s specific Baseline approach chose ellipse fitting as a feature extractor, an Isolation Forest to rank by rarity, and a Random Forest (Breiman 2001) to model user interest. We replace each of these steps. We also qualitatively change Astronomaly’s novel active learning approach from labelling the galaxies thought to be most interesting to labelling the galaxies which, if labelled, would best help to find those interesting galaxies.

Astronomaly’s ellipse-fitting feature extractor works, in short, by placing a series of ellipses enclosing increasing proportions of flux, and recording the properties of those ellipses (e.g. axial ratio) as tabular features. This was chosen to create features which were sensitive to the shape of galaxies (LB21). In this work, we instead use the DECaLS model as a feature extractor, with the learned representation forming the features for each galaxy. We believe our learned representation is particularly vital for tasks where the interesting morphology (e.g. irregular shapes, rings) cannot be well described as a series of ellipses of increasing flux. More broadly, because the galaxies are arranged in representation space by visual similarity (Section 2), interesting galaxies are likely to have similar representations and so representations are a useful feature for predicting user interest.

Next, we change the regressor modelling user interest. We replace Baseline’s Random Forest with a Gaussian Process (GP; Rasmussen & Williams 2006). Gaussian Processes define a probability distribution over possible functions. The space of possible functions is set by the choice of kernel, \( k(x, x') \). The kernel defines an effective distance between points, with the range of probable values for each point being constrained by the values of known nearby points. The kernel hyperparameters (e.g. the typical distance over which known points have a strong constraining effect) are fit to maximize the likelihood of the observed (training) data. See Murphy (2012) for a concise review and Rasmussen & Williams (2006) for a comprehensive treatment.

GPs are particularly appropriate here for two reasons. First, they can flexibly model smooth distributions; they make no parametric assumptions about the shape of the user interest distribution other than through the kernel itself. We use a rational quadratic kernel assuming user interest is similar for similar galaxies and varies over some typical scale, and add a white component to model intrinsic label uncertainty on user interest and to model noise in the underlying representation. Secondly, through marginalizing over the many possible functions allowed by the kernel, GPs provide relatively reliable uncertainties. Indeed, GP uncertainties are sometimes considered the ‘gold standard’ against which more scalable methods are measured (Houlsby 2014). Knowing the uncertainty of our user interest predictions for each galaxy is critical for applying active learning.

A key part of active learning is the acquisition function i.e. which galaxies to label. Astronomaly selects galaxies to label with a ‘joint’ score based on both expected interest and rarity. For each galaxy, if galaxies with similar features have already been labelled, the regressor is considered more reliable and the joint score is weighted towards the regressor’s predicted interest. If not, the joint score is instead weighted towards the galaxy’s rarity. Users are then asked to label the galaxies with the highest joint score i.e. the galaxies thought most likely to be interesting anomalies. Whilst effective, this algorithmically greedy approach may be inefficient in some cases. We may not yet know which galaxies are likely candidates, and should therefore devote at least some labelling effort to explicitly helping the regressor model user preferences.

Which galaxies would best help model user preferences? Active learning acquisition functions are generally concerned with modelling a function globally; in our case, modelling the user interest on
all galaxies. But here, we are specifically interested in finding the most interesting galaxies, i.e. modelling the function near its maxima. We are not concerned with whether a galaxy is very boring or merely somewhat boring. Modelling maxima is an optimization problem, and we therefore use an acquisition function from the Bayesian optimization literature.

Specifically, we choose to use maximum expected improvement (‘max EI’) as our acquisition function, EI, introduced by Mockus & Mockus (1991) and further developed in Jones, Schonlau & Welch (1998), is calculated as

\[ EI(x) = (\mu(x) - f(x^*) - \epsilon) \Phi \left( \frac{\mu(x) - f(x^*) - \epsilon}{\sigma(x)} \right) + \sigma(x) \phi \left( \frac{\mu(x) - f(x^*) - \epsilon}{\sigma(x)} \right), \]

where \( \mu(x) \) and \( \sigma(x) \) are the mean and variance of the GP modelling user interest, \( f(x^*) \) is the current maximum recorded user interest, and \( \Phi \) and \( \phi \) are the CDF and PDF of a standard normal variable, respectively. Intuitively, EI measures the expected gain in maximum interest from a rating, \( x \), given the current estimate, \( \mu(x) \), and uncertainty, \( \sigma(x) \), for \( x \)’s likely interest. \( \epsilon \) is a hyperparameter balancing exploration and exploitation and is subtracted from the expected improvement, causing the algorithm to ignore gains smaller than \( \epsilon \) (typically in well-explored regions) and instead explore more uncertain regions where the potential gains are still larger than \( \epsilon \). \( \epsilon \) is particularly important for this problem because we potentially aim to find diverse anomalies in many different regions each of high interest, rather than just the anomalies in the single region of highest interest. We find that a non-zero \( \epsilon \) is crucial to avoiding occasional (10–20 per cent) failures where the acquired galaxies fall into a single local maxima. We choose \( \epsilon = 0.5 \) throughout, representing an interest increase of 0.5 on the 0–5 rating scale used by Astronomaly.

3.3 Experiments

3.3.1 Galaxy Zoo 2 ‘Odd’ Galaxies

LB21 primarily demonstrate the performance of Astronomaly through identifying unusual galaxies in Galaxy Zoo 2. Specifically, they aim to identify the rare (approximately 1.5 per cent) subset of galaxies which more than 90 per cent of GZ2 volunteers described as ‘Odd’ in the ‘Is there anything odd?’ task. We repeat this demonstration with the method in this work and compare performance against ‘Baseline’, the specific Astronomaly configuration used by LB21 and summarized in the previous Section.

Starting from the same Galaxy Zoo 2 images as LB21, we calculate representations using our DECaLS-trained CNN following the procedure described in Section 2.2. As in Section 2.2, we further reduce the dimensionality using Incremental PCA, in this case with 40 components preserving 98.1 per cent of the variation. We then use GP-based active learning to model user interest in this reduced representation. As in LB21, we simulate receiver ratings through the Astronomaly interface using the recorded GZ2 ‘Odd’ vote fraction\(^9\) scaled and binned to integers from 0 to 5, and consider anomalies as those galaxies with ‘Odd’ vote fractions above 90 per cent.

\(^9\)We use the vote fraction as released in the ‘Galaxy Challenge’ Kaggle competition, following LB21’s experimental protocol. Note that these vote fractions are not identical to the latest published GZ2 catalogue (Hart et al. 2016), which we suggest for general scientific use.

We acquire (i.e. simulate rating for interest) galaxies in batches of 10, chosen to ensure that it takes no more than a few seconds to retrain the GP and identify the next galaxies to rate. This helps the user rate galaxies quickly and enjoy a responsive experience. Introducing batching did not reduce performance. The first batch of galaxies is chosen randomly.\(^10\) We rate for interest a total of 200 galaxies, matching LB21.

Fig. 3 compares the results of our CNN and GP-based approach with the Baseline. Fig. 3 follows the same format as fig. 5 in LB21, comparing their ‘rank weighted score’ metric against the number of top galaxies, \( N \), to consider when calculating the score. This rank weighted score measures how highly the true interesting anomalies are ranked among the \( N \) galaxies predicted as most likely to be interesting. We also provide conventional accuracy and average precision scores in Fig. 3 and Table 1. All experiments are repeated 15 times to marginalize over stochastic effects.

From Fig. 3 it can be seen that Baseline easily outperforms random selection, with two-thirds of the 50 galaxies predicted as most likely to be interesting anomalies actually being so. Using the method presented in this work, with both CNN representations and GP-based

\(^10\)Experiments with selecting the first batch via Isolation Forest did not show a performance improvement.
active learning, all of the top 50 galaxies and indeed all of the top 100 galaxies are interesting anomalies. Given that interesting anomalies represent only 1.5 per cent of the data set, this improvement is notable. 87 per cent of the top 200 galaxies are interesting anomalies, compared with 40 per cent using Baseline and 1.5 per cent using random selection.

Fig. 4 investigates why the new method is more successful. In this figure, we visualize the representations of both Astronomaly’s ellipse-fitting method and of our CNN using a 2D umap projection, as in Section 2.3. We then colour galaxies according to either Isolation Forest predictions or those of the Gaussian Process interest model. We also show the galaxies considered as anomalies and the galaxies selected for rating by the user, either due to the Isolation Forest ranking or our acquisition function. The CNN representation is far more effective at grouping ‘Odd’ galaxies together than the ellipse representation, and this, in turn, makes user interest easier to model. The interest model matches the density of interesting anomalies well and the user-rated galaxies concentrate along the region of highest interesting anomaly density. In contrast, the ellipse representation places ‘Odd’ galaxies along a distributed border in our visualization. This is crucial for the success of the Isolation Forest in making an initial prioritization (which will prefer border regions). However, the galaxies considered most anomalous by the Isolation Forest, and hence rated by the user, tend to lie only in specific patches on the border and so the user ratings of those galaxies do not efficiently measure user interest along the full anomalous border.

We highlight that our CNN can calculate effective feature vectors from Galaxy Zoo 2 images even though it has never been trained on Galaxy Zoo 2 data. The CNN was only trained on GZ DECaLS images, which are significantly deeper and of higher resolution than the Galaxy Zoo 2 images (W+22). It is well-known that CNNs can suffer from substantial performance drops in the presence of minor domain shifts barely visible to humans (e.g. contrast adjustments, added Gaussian noise, adversarial attacks – see Moosavi-Dezfooli et al. 2017; Hendrycks & Dietterich 2019; Ilyas et al. 2019), and it is therefore encouraging that the CNN representation used here remains useful across different surveys without any need for retraining.

### 3.3.2 DECaLS mergers, rings, and irregular galaxies

The vast majority of ‘Odd’ GZ2 galaxies are major mergers (LB21). While scientifically valuable, major mergers may not be representative of all interesting anomalies and so mergers alone may not provide a comprehensive test of an anomaly finding method. We therefore apply our method to finding irregular galaxies and ring galaxies in DECaLS (along with mergers again for comparison), using the vote fractions reported by GZ DECaLS volunteers.

We use the same DECaLS images previously described and used in Section 2. We select only galaxies with at least 30 total volunteer responses to ensure reliable vote fractions. Of 253 286 volunteer-labelled galaxies, the Astronomaly ellipse method fails for 2112 galaxies, returning nan features; we exclude any galaxies with failed ellipse measurements from the experiment. We filter to relevant galaxies using automated vote fraction prediction cuts of featured fraction > 0.6 and face-on fraction > 0.75, for a final experiment catalogue of 58982 galaxies (56 828 for identifying mergers). For each class of anomaly, we choose the minimum vote fraction to be defined as an interesting anomaly such that the rate of interesting anomalies is 1.5 per cent (matching LB21’s GZ2 experiment above); f > 0.42 for irregular galaxies, f > 0.57 for rings, and f > 0.6 for mergers. As before, we use the binned volunteer vote fraction to emulate user interest responses from 0 to 5.

We follow the same method as for the GZ2 ‘Odd’ experiment, using the CNN representation as galaxy features and acquiring galaxies (in batches of 10) that maximize the expected improvement of our GP user interest model. We compare our results to Baseline in Fig. 5 and Table 1.

Our method again dramatically outperforms both Baseline and random selection. For each anomaly class, we achieve a high fraction of true interesting anomalies in the top 200 galaxies: 88 per cent for mergers, 96 per cent for rings and 91 per cent for irregular galaxies.

13For identifying mergers, where the question was modified during GZ DECaLS (see W+22), we specifically require 30 votes for the latest version of the merger question.

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**Table 1.** Performance metrics for finding each anomaly in each data set with either the Astronomaly configuration used by LB21 on this task (Baseline) or introduced in this work (CNN and GP). ‘Failed’ indicates a failure to find the specified anomalies, indicated by a score comparable to random selection. Errors are (roughly) estimated as the 3σ error on the mean over 15 runs. The best metrics are shown in bold. Our method significantly improves every metric in every case, and avoids failures on some combinations of target anomaly and data set.

<table>
<thead>
<tr>
<th>Data set</th>
<th>Anomaly</th>
<th>Method</th>
<th>Average precision</th>
<th>Accuracy (top 50)</th>
<th>Accuracy (top 200)</th>
</tr>
</thead>
<tbody>
<tr>
<td>GZ2</td>
<td>Odd</td>
<td>Baseline</td>
<td>0.16 ± 0.02</td>
<td>66 per cent ± 16 per cent</td>
<td>40 per cent ± 7 per cent</td>
</tr>
<tr>
<td>GZ2</td>
<td>Odd</td>
<td>Ellipse + GP</td>
<td>0.21 ± 0.10</td>
<td>99 per cent ± 5 per cent</td>
<td>63 per cent ± 22 per cent</td>
</tr>
<tr>
<td>GZ2</td>
<td>Odd</td>
<td>CNN + GP</td>
<td>0.55 ± 0.10</td>
<td>100 per cent</td>
<td>87 per cent ± 11 per cent</td>
</tr>
<tr>
<td>DECaLS</td>
<td>Merger</td>
<td>Baseline</td>
<td>0.12 ± 0.03</td>
<td>25.5 per cent ± 18.6 per cent</td>
<td>24.9 per cent ± 7.7 per cent</td>
</tr>
<tr>
<td>DECaLS</td>
<td>Merger</td>
<td>CNN + GP</td>
<td>0.58 ± 0.20</td>
<td>100 per cent</td>
<td>88 per cent ± 15.4 per cent</td>
</tr>
<tr>
<td>DECaLS</td>
<td>Ring</td>
<td>Baseline</td>
<td>Failed</td>
<td>Failed</td>
<td>Failed</td>
</tr>
<tr>
<td>DECaLS</td>
<td>Ring</td>
<td>CNN + GP</td>
<td>0.63 ± 0.11</td>
<td>99.9 per cent ± 1.5 per cent</td>
<td>95.8 per cent ± 13 per cent</td>
</tr>
<tr>
<td>DECaLS</td>
<td>Irregular</td>
<td>Baseline</td>
<td>Failed</td>
<td>Failed</td>
<td>Failed</td>
</tr>
<tr>
<td>DECaLS</td>
<td>Irregular</td>
<td>CNN + GP</td>
<td>0.58 ± 0.04</td>
<td>100 per cent</td>
<td>91 per cent ± 5.4 per cent</td>
</tr>
</tbody>
</table>
Baseline achieves 25 per cent for mergers and is comparable to random selection for rings and irregular galaxies.

Fig. 6 shows (for each anomaly class) a random selection of the top 200 galaxies identified by our method as having the highest expected interest. These are representative of the galaxies that a user being recommended interesting anomalies might see. Our method successfully presents rings, mergers or irregulars according to the user’s interests.

We have shown how our CNN representations can, when combined with GP-based modelling of user interest, be used to better find interesting optical galaxies than in previous work — even though it was not specifically trained to do so. In the next section, we turn to how to improve the representations themselves.

4 TRANSFER LEARNING AND FINE-TUNING

We have shown that the representations learned by our GZ DECaLS model are useful for tasks on which it was never trained. We used the representations to find similar galaxies (Section 2) and interesting anomalies (Section 3) without any modification. Going further, we can also tailor the representations for a specific task.

One relevant task is to find more of a specific type of galaxy based on a small set of known examples. We can do so better than with a similarity search by learning from multiple examples (not one), and we do not need a blind anomaly search as we know what we are looking for. By starting from our GZ DECaLS representations, we can solve this supervised classification task using far fewer known examples than otherwise required.

In this section, we fine-tune the DECaLS model for finding ring galaxies and find that it outperforms equivalent models trained from scratch, fine-tuned from ImageNet, or fine-tuned from single GZ DECaLS tasks.
4.1 Context

Fine-tuning is a technique where a model is trained on one problem (typically one with plentiful labelled data) and then adapted to a second problem (typically one with less labelled data). Once trained on the first problem, the upper layers of the model (the ‘head’) are removed and the remaining layers frozen (i.e. the weights are fixed). This ‘base’ model simply calculates representations, exactly as we have done in Section 2.2. A new ‘head’ model is added, with outputs appropriate to the new problem and with fewer parameters to avoid overfitting the more limited labels. The new head is trained to predict outputs for the second problem given the frozen representation (from the base model) and the new labels. This allows the new head to benefit from the previously learned representation, as we have been doing throughout this work. Finally, once the new head is trained, some or all of the base model layers may be unfrozen and both head and base model trained together (typically at a low learning rate to avoid overfitting). This gradually adapts the representation to best solve the second problem, starting from the already useful initial representation learned for the first problem. We refer the reader to Goodfellow et al. (2016) for a further introduction to fine-tuning.

What is the best base model to fine-tune for a new galaxy classification problem? In our Section 1, we noted various efforts by astronomers to use fine-tuning to mitigate the lack of available labelled data for their target problem. The base models were trained either on identical narrow questions on comparable surveys (Dominguez Sanchez et al. 2019; Pérez-Carrasco et al. 2019; Tang et al. 2019) or on the broad but terrestrial ImageNet data set (Ackermann et al. 2018; Wu et al. 2018; Martinazzo et al. 2020). Training on identical questions is not possible where we want to answer new questions for which no labels yet exist. We argued that ImageNet is qualitatively different to galaxy images and so pretraining on ImageNet is unlikely to be as helpful as pretraining to answer a broad set of questions on galaxy images. Both approaches would lead to generic representations, but ImageNet would lead to a generic terrestrial representation while galaxy images would lead to a generic galaxy morphology representation. We have shown in the preceding sections that such generic galaxy representations are indeed learned and are immediately useful for diverse tasks beyond classification. We now test if our representations can help astronomers outperform ImageNet pretraining on new classification tasks.
4.2 Experiments

To measure the effectiveness of fine-tuning from our representation to solve new classification tasks, we experiment with identifying ring galaxies.

Rings have long been thought to be typically\(^\text{14}\) caused by resonances in a disc driven by a bar, or, where no bar is present, driven by an oval-shape or spiral potential (Schwarz 1981). More recent theoretical work suggests they may in fact be related to dynamical manifolds (Athanassoula, Romero-Gómez & Masdemont 2009). Both theories predict ring morphologies broadly similar to those observed (Buta 2013). However, each theory makes specific predictions about the nature and frequency of ring subtypes and so it may be possible to distinguish the true cause(s) from a sufficiently large ring sample.

Rings are also useful to measure secular evolution. The slow nature of ring formation (in both theories) suggests a lack of recent major mergers and so any difference in characteristics between rings and standard disc galaxies may help test the effect of major mergers on topics such as quenching (Smethurst et al. 2017) and black hole growth (Simmons et al. 2013). Such an investigation would again likely require a large ring sample in order to control for other variables (mass, redshift, environmental density, etc.)

Existing expert catalogues contain of order tens to hundreds of rings (Buta & Combes 1996; Lavery et al. 2004; Nair & Abraham 2010; Struck 2010; Moisseev et al. 2011; Comerón et al. 2014; Buta et al. 2015, 2019). This is in stark contrast to the size of modern surveys such as DECaLS (Dey et al. 2019), which contain hundreds of thousands to millions of galaxies with imaging appropriate for identifying rings. Even if rings make up only a few percent of galaxies, this suggests that there are thousands to tens of thousands of rings yet to be identified in DECaLS alone.

Efforts at automatic identification are sparse. Our literature search revealed only two papers (Timmis & Shamir 2017; Shamir 2020) automatically identifying 185 and 443 ring candidates in PanSTARRS and SDSS, respectively. The largest ring catalogue, Buta (2017), was created using crowdsourcing. 3692 galaxies were identified by Galaxy Zoo 2 volunteers and then classified by a single expert (R. Buta).

For our experiment in automatically finding rings, we first need to identify large samples of ringed and not-ringed galaxies in DECaLS images. As mentioned in Section 3, Galaxy Zoo DECaLS volunteers were asked if each galaxy had rings via the ‘Are there any of these rare features?’ question (see W+22 for a full schema). We use these votes to identify likely rings and not-rings.

We make initial selection cuts on the DECaLS DR5 catalogue (Section 2.1). For simplicity, we select galaxies with volunteer votes from the GZD-5 campaign (253,286 galaxies). We use the ML-predicted vote fractions of ‘Smooth’ < 0.25 and ‘Not Edge On’ > 0.75 to select a subset of 82,898 candidate ring galaxies.\(^\text{15}\) Note that we use the ML-predicted morphology vote fractions, rather than the volunteer vote fractions, because we ultimately hope to make the same selection cuts on galaxies not previously classified by humans. We then use volunteer ‘ring’ vote fractions to select relatively clean samples of rings and not-rings. Based on inspection by one of the authors (MW) of several hundred random galaxy images selected at various ‘ring’ vote fractions, we choose to consider galaxies with a fraction \(f > 0.25\) as rings (12 per cent, \(N = 9947\); of which we judge approximately 90 per cent are truly ringed based on random inspection) and galaxies with a vote fraction \(f < 0.05\) as ‘not rings’ (61 per cent, \(N = 50,855\)). Galaxies with intermediate vote fractions (27 per cent, \(N = 22,096\)) are discarded. Our priority is to make a simple, reliable test of how different methods perform at finding rings under equivalent conditions rather than finding as many rings as possible. We note that, with approximately 10,000 likely rings, this is the largest ring catalogue to date.

What is the best way to train a model to find these ring galaxies? We test three training methods. First, and most conventionally, training from scratch using a random weight initialization (‘scratch’). Secondly, training a new head on a pretrained base model with frozen weights (‘frozen’). Third, once the new head has been trained, allowing some or all of the base model layers to also be trained (‘fine-tuned’). We test pretraining with either GZ DECaLS (i.e. using our representation as a starting point) or with ImageNet. This allows us to measure whether our GZ DECaLS representation is helpful, whether it is more helpful than the ImageNet representation, and whether further fine-tuning of either representation can improve performance. To investigate whether learning to solve many diverse tasks is important for creating a helpful representations, we also test pretraining with GZ DECaLS labels but only using the labels from a single task (e.g. only training to predict ‘Smooth or Featureless’? votes).

We ensure that, other than the different training methods described above, all other factors are equivalent between tests. Below, we describe the specific details of our architecture, data splits, and training procedure.

4.2.1 Architecture

We use the same EfficientNetB0 architecture and training procedure as previously introduced in Section 2.2. We instantiate the network in three ways: (i) randomly, (ii) with the weights from pretraining on ImageNet as provided by Keras Applications,\(^\text{16}\) or (iii) with the weights from pretraining on GZ DECaLS by W+22 (released with this work, see Data Availability Statement Section), either pretraining to predict all GZ DECaLS tasks (as done throughout this work) or pretraining on only a single GZ DECaLS task (this section only). In all cases, we replace the final dense layer with a new head comprised of two 64-units dense layers, each with dropout probability of \(p = 0.75\) and \(\text{ReLU}\) activations (Agarap 2018), and a final 1-unit dense layer with sigmoid activation. This head design was chosen to have a low capacity to maximize overfitting on small data sets. For pretrained models, the head is trained to convergence on the frozen base model (using the Adam optimizer and an initial learning rate of \(10^{-3}\)) before the base model is unfrozen and allowed to also train (with a lower learning rate of \(10^{-3}\)). Using our chosen head, EfficientNetB0 has approximately 41.1 parameters, comparable to older designs such as VGG16 (Simonyan & Zisserman 2015), and is therefore best viewed as a more advanced network rather than a ‘bigger’ network.

Two elements of EfficientNet are particularly important to this work. First, EfficientNet includes batch normalization layers (Ioffe & Szegedy 2015) which we never unfreeze during fine-tuning (i.e. we preserve the activation statistics from initial training), as is standard practice. Secondly, EfficientNet is divided into a repeating pattern

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\(^{14}\) Some so-called collisional rings are caused by mergers (Lavery et al. 2004). These are thought to be rare and could be an interesting target for the similarity search in Section 2.4.

\(^{15}\) Our volunteer ‘ring’ vote fraction criterion is less reliable for galaxies failing these cuts; galaxies with volunteer ‘ring’ vote fractions \(f > 0.25\) which are also predicted to be extremely smooth or edge-on are often judged to not be rings by the authors.

\(^{16}\) https://keras.io/api/applications/
of mobile inverted bottleneck blocks, just as previous designs tend to include repeating blocks of convolutional layers and a pooling layer. We investigate partially fine-tuning EfficientNet by unfreezing increasing numbers of these blocks, from the output layer down, and measuring how performance varies. We follow the same block naming schema as Tan & Le (2019)’s EfficientNet implementation; the ‘top’ block is the Conv2D and batch normalization block listed as Stage 9 in Tan & Le (2019) table 1, ‘block7’ is the mobile convolutional block listed as Stage 8, ‘block6’ is listed as Stage 7, and so forth.18

4.2.2 Restricting data set size

Not all astronomers have access to tens of thousands of labelled galaxies. It is therefore crucial to measure how the performance of each training method varies with the number of available labels. We expect that starting from the GZ DECaLS representation will be particularly useful for astronomers with fewer labelled galaxies, where training from scratch would be more likely to overfit.

When varying the data set size, the class balance must remain constant regardless of data set size so that the final losses are comparable.19 We choose the balance to be equal. For each experiment run, we first set aside 30 per cent of rings (2984), chosen randomly, and divide them into validation (10 per cent) and test (20 per cent) sets. We then similarly set aside 30 per cent of not-rings and randomly select 2984 not-rings to match each ring. To construct the training set, we oversample (i.e. repeat) the remaining 6962 rings by a factor of 5 such that the number of remaining ringed galaxies is close to, but slightly below, the number of not-ringed galaxies.20 We then cut surplus not-ringed galaxies such that the class balance is exactly equal (6962 rings repeated five times each, and 34 810 unique not-rings). We then artificially reduce the data set size as required for the desired data set size by dropping random galaxies from the training subset. This provides realistic variation in the training class balances while preserving the average balance. We do not drop galaxies from the validation subset; preserving these galaxies drastically reduces the noise in our performance metrics introduced by early stopping (below).

Every model is independently trained with a new train, validation, and test split. This allows us to measure the significant uncertainty in loss caused by the choice of training data, particularly in the low data regime; training on these 10 or those 10 galaxies can dramatically affect model performance.

4.2.3 Training procedure

Models are trained using the binary cross-entropy loss. To efficiently use our limited GPU resources, we use early stopping (i.e. we end training for models with a non-decreasing validation loss). The number of update steps per epoch increases with data set size and so we calculate the patience (i.e. the maximum number of epochs

![Figure 7](https://academic.oup.com/mnras/article/513/2/1581/6539338)

**Figure 7.** Test accuracy as a function of the total number of labelled ring galaxies to train on, split by base model pretraining. Models are pretrained on either all (‘Multi’) GZ DECaLS tasks (i.e. starting from our DECaLS representation), pretrained to solve only the Smooth/Featured/Artifact GZ DECaLS task, pretrained on ImageNet, or trained from scratch. Solid versus dashed lines compare models where only the upper-most layers are allowed to train (‘Frozen’) versus where all layers are allowed to train (‘Finetuned’). Models pretrained on GZ DECaLS are better able to classify rings at all training set sizes.

with no validation loss improvement before cancelling training) on a sliding scale from 10 to 30. Specifically, after some experimentation, we choose the patience as min(max(10, int(epochs/6)), 30) and the total possible epochs21 as 5 × 104/train data set size. We find this ensures that all models are trained to convergence but GPU resources are not unduly wasted past convergence. Training time is strongly dependent on data set size. Training on the full data set takes approximately 6 h on an NVIDIA A100 GPU. As our performance metric, we record the test loss of the weights with the lowest observed validation loss during training (i.e. the best-performing checkpoint as measured on the validation data set).

We experiment with the following training methods. For initial weights pretrained on all GZ DECaLS tasks, on the ‘Smooth or Featured’ task only, or on Imagenet, we test six fine-tuning options (the top block only, blocks 7+, 6+, 5+, 4+, and all blocks), each first training atop a frozen base model before fine-tuning. For initial weights pretrained on the GZ DECaLS ‘Spiral’ task only, ‘Bar’ task only, and ‘Bulge’ task only, we test two fine-tuning options (top block only and all blocks), each first training atop a frozen base model similarly. We also train a model from scratch. All combinations of training method and training data set size are repeated 5 times for each of the 12 data set sizes, for a total of 60 models per training method. We record performance metrics from a total of 2940 models.

4.3 Results

We find that models pretrained with all GZ DECaLS tasks outperform both models pretrained with ImageNet and models trained from scratch for data sets of all available sizes. Fig. 7 reports the mean accuracies.

For very small training data sets (below 10 unique rings), all models struggle similarly but the DECaLS-pretrained models already improve on random chance. With 10–100 rings, the DECaLS-pretrained models vastly outperform all others. With 100–1000 rings, the fine-tuned ImageNet model improves significantly but

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17https://github.com/qubvel/efficientnet
18The blockN and Stage N−1 numbers are offset because the implementation names the first block as ‘stem’ rather than Stage 1.
19Class imbalance makes prediction easier. Consider the limiting case where there is only one class; a toy model predicting only that class would be perfectly accurate.
20This also allows us to train on more non-ringed galaxies than simply picking an equal number of non-ringed galaxies, because each of the 5 repeats of a ring galaxy are matched by a unique non-ring galaxy.
21No model is trained to the maximum number of epochs; this is solely used to calculate the patience for early stopping.
the DECaLS-pretrained models remain firmly ahead. With $10^3 - 10^4$ rings, training from scratch suddenly becomes feasible; the from-scratch model dramatically improves from random chance (i.e. failing to train) to outperform the ImageNet model. The DECaLS-pretrained model remains ahead with our full training data set of 6962 rings, though the from-scratch would likely equal or overtake it with around $10^4 - 10^5$ labelled rings. Since approximately 12 per cent of galaxies in our data set have rings, this would correspond to labelling $10^5 - 10^6$ galaxies.

Two further comparisons suggest that training on multiple tasks is crucial for constructing a useful representation for this new task (identifying rings). Fig. 8 shows that, after fine-tuning all layers to classify rings, models pretrained on all DECaLS tasks significantly outperform equivalent models pretrained on any one of several individual tasks. Fig. 9 compares the final performance of models fine-tuned to increasing depths — from only the top mobile bottleneck block (‘Top’), through the intermediate blocks (Blocks 6 and above, 4 and above) and down to all layers (‘All’). Fine-tuning more layers consistently improves the performance of all models, but the magnitude of this performance improvement is dramatically different. For models pretrained on either ImageNet or on the DECaLS ‘Smooth or Featured’ single task, fine-tuning only the top block has little to no effect on accuracy versus the frozen equivalent (where only the dense layers are trained to classify rings). Fine-tuning the intermediate blocks and above is necessary to achieve good performance, increasing accuracy from approx. 70 per cent to approx. 85 per cent. In contrast, for models pretrained on all DECaLS tasks, even the frozen models outperform the fully fine-tuned ImageNet and single task models, with further fine-tuning providing only a small additional performance improvement. Together, we interpret these comparisons as strong evidence that the representations learned from training on all DECaLS tasks are more immediately appropriate to new tasks than representations learned from single DECaLS tasks or from ImageNet.

Our practical advice is that if you have fewer than $10^4$ labelled galaxies of one class, and the task you are solving is of a similar nature to the Galaxy Zoo questions, you are likely to perform better with our pretrained model than with a comparable model either trained from scratch or pretrained on ImageNet. The further gain from introducing fine-tuning (rather than simply using the frozen pretrained representation) may depend on how similar the task is to the Galaxy Zoo questions.

To help the community benefit from our pretrained models, we release the code as the PYTHON package zoobot at https://github.com/mwalmsley/zoobot. We provide extensive documentation at zoobot.readthedocs.io aimed at researchers (including Masters or PhD students) with a strong interest in deep learning but no prior experience. The package additionally contains simple working examples to extend pretrained models and apply fine-tuning. We hope this will help make deep learning accessible to astronomers working with smaller labelled data sets.

5 DISCUSSION

We have shown that, using our representation, finding a range of interesting anomalous galaxies is straightforward. What should we do with this capability? Specifically, how do we build systems that lead to new scientific insights from those anomalies? First, we would like to make human-in-the-loop anomaly recommendation available to as many interested humans as possible. Citizen scientists have repeatedly driven discoveries of unique objects or new classes (Lintott 2019). We hope to make methods like the one presented here available to them on the Zooniverse citizen science platform. This might also enable us to exploit the shared interests of the crowd through recommendation engines. We could make predictions like ‘people with similar interests to you also liked this galaxy’. We would also like to encourage formal collaboration with observatories for follow-up, which – given the size of new surveys – may become the limiting factor.

The anomalies we find will depend strongly on our choice of representation. Our DECaLS CNN representation is learned directly from data and so might be considered more flexible than handcrafted parametric feature extractors like ellipse fitting, which assume a particular functional form (e.g. that a galaxy can be described as a series of ellipses of increasing total flux). However, our CNN representation will have its own assumptions (from e.g. the choice of convolution sizes) and these are perhaps harder to identify than with parametric feature extractors. There is likely no single ‘best’ representation. Similarly, there is likely no single best active learning strategy. Our GP search and acquisition function assume that the user has degrees of interest (for example, that a user interested in rings will find discs a little interesting, face-on-discs more interesting, and rings most interesting) so that our initially random search can move up the resulting interest gradients to find the target galaxies. A user who only wants to find anomalies which are utterly distinct from other galaxies might be better served by starting from a machine-learning prioritized list of the most quantitatively unusual galaxies, as in e.g. LB21. Frameworks like Astronomaly are therefore important for enabling researchers to choose their own representations and active learning strategies while abstracting away shared technical details such as the browser interface. Our pretrained CNN is publicly available (Data Availability Statement Section) and we plan on incorporating it into future versions of Astronomaly.

Counter-intuitively, our fine-tuning results show that pretraining on ImageNet can actively harm performance. It has been previously assumed (e.g. Dobbels et al. 2019) that pretraining on ImageNet is good practice for astronomers. Evidence for the benefits of ImageNet pretraining was gathered with experiments on relatively small data sets (Ackermann et al. 2018; Martinazzo et al. 2020), where the benefits of pretraining would be expected to be greater. We find that ImageNet pretraining is indeed useful with small data sets
Figure 9. The effect of fine-tuning on ring classification test accuracy, split by base model pretraining. The model layer blocks are named, from the output, ‘Top’, ‘Block7’, ‘Block6’, etc – see main text for details. We show results for fine-tuning the top (Top), blocks six and above (Blocks 6+) blocks four and above (Blocks 4+) and all blocks (All). For models pretrained with either ImageNet (left) or on the GZ DECaLS ‘Smooth or Featured’ task (centre), fine-tuning intermediate layers is crucial to achieve good performance. In contrast, for models pretrained to solve all GZ DECaLS tasks simultaneously (right), performance is high without fine-tuning and fine-tuning provides only a small additional benefit. This suggests the representation learned from all DECaLS tasks is more immediately appropriate to new tasks than representations learned from single DECaLS tasks or from ImageNet.

(consistent with previous experiments) but that as the data set size increases, ImageNet pretraining may eventually lead to worse performance than training from scratch. Recent computer science results show that the network initialization can dramatically change the minima found at convergence (Fort, Hu & Lakshminarayanan 2019). It may be that, beyond a certain data set size, the ImageNet initialization sets the network on a path to learn features which are ultimately less helpful than those that would otherwise be learned directly. We encourage researchers to experiment with both our galaxy-appropriate pretrained weights and with training from scratch.

When aiming to solve a new task on galaxy images, it may seem self-evident, in retrospect, that pretraining on galaxy images is more effective than pretraining on terrestrial images. Doing so is not standard practice. We are the first to do this in a supervised context. It remains to be seen whether pretraining on large supervised data sets or on even larger self-supervised data sets will be more effective for astronomers. Self-supervised contrastive learning in particular continues to advance (Grill et al. 2020; Caron et al. 2021) and has found very recent practical applications in astronomy (Hayat et al. 2021; Sarmiento et al. 2021; Stein et al. 2021). One key benefit in our context is the opportunity to distinguish classes where broad supervised labels are unhelpful (for example, we note that the similarity search returns two ‘wrong size’ images under the ‘star’ search, perhaps because the GZ decision tree labels are not useful in distinguishing these two cases). The best approach may ultimately be a combination of the two, with self-supervised ‘pre-pretraining’ followed by supervised pretraining and finally fine-tuning to the task at hand. As the complexity grows, we may see some ML-centric researchers specialize in this process while others focus on carrying out specific applications and drawing scientific conclusions.

Bias propagation is a potential concern. The initial representation could include subtle unwanted correlations from the initial data set, which could then be inherited by the fine-tuned model and affect the downstream predictions even if the downstream data set is itself unbiased. Detecting such biases is itself an active field of computer science research and so this, again, would likely benefit from specialized attention. We note that only a small minority of recent deep learning applications in the astronomical literature include experiments to check for biases or to understand why specific predictions are made (e.g. Ghosh et al. 2020). This might either make inherited bias more of a concern, in that such biases are unlikely to be detected without a change in culture within the field, or less of a concern, in that the field currently broadly accepts models with a potential direct bias and so inherited bias is merely a second-order effect on an existing issue.

The question of how best to classify a new survey with no labels comes increasingly pressing as we approach first light for the Vera Rubin Observatory (LSST Science Collaboration 2009) and Euclid (Laureijs et al. 2011). We noted (Section 3) that our model was able to identify ‘Odd’ galaxies in Galaxy Zoo 2 despite only being trained on DECaLS. It is plausible (see e.g. Dominguez Sanchez et al. 2019) that retraining on a few hundred survey-specific labels might have further improved performance. If, as our results suggest, CNN trained on broad tasks are relatively transferable between galaxy surveys, we may be able to use these pretrained models to rapidly classify entirely new surveys like LSST. A short citizen science campaign answering a Galaxy-Zoo-like task on an active-learning-selected subset could provide enough new labels to adapt our representations. The adapted representations could then be used for time-sensitive downstream tasks like finding difference-image transients for which one cannot afford to wait several years to build the data sets that traditional ‘from scratch’ approaches require.

If large data sets become central to deep learning in astronomy, as they have in the natural language community, it is crucial that we allow fair access for researchers at less well-resourced institutions. The data, code, and trained models from this work are all publicly available (Data Availability Statement Section).

6 CONCLUSION

Representations are the core of many machine learning methods. We have shown that, when trained on the broad task of answering every Galaxy Zoo DECaLS question, our convolutional neural network learns an internal representation of galaxies arranged by morphological similarity. This general representation is directly useful for new practical tasks on which the network was never trained.

The first practical task we showed was a similarity search method. Similarity searches aim to return the most similar galaxies to a query galaxy. To do so, they require a quantified measurement of the similarity between two galaxies – a problem underlying the search for automatic taxonomies of galaxies. Because our representation arranges galaxies by similarity, our measurement of similarity is simply estimated as the distance in representation space between
galaxies. The most similar galaxies are the galaxy galaxy’s nearest neighbours. We tested our search method using free text hashtags (e.g. ‘#starforming’, ‘#disturbed’, etc.) from the Galaxy Zoo forum. For each common hashtag, we searched for the galaxies most similar to the galaxy most frequently given that tag. Our searches were successful in a clear majority of cases, even where the hashtag was highly specific (e.g. ‘#dustlane’) and even though none of the tags corresponded to the original training labels (Galaxy Zoo vote fractions).

The second practical task was finding rare galaxies that were personally interesting to a given user. We used GP regression to model user interest, and our uncertainty about that interest, for each galaxy. We selected which galaxies to be rated for interest by our user with active learning and a Bayesian optimization acquisition function. We simulated a user expressing their interest through the Astronomaly interface (Lochner & Bassett 2021) with Galaxy Zoo vote fractions as a ground truth for interest values. We carefully replicated the test originally used to demonstrate a specific Astronomaly configuration and achieved a significant improvement in performance. All of the top 100 galaxies predicted by our method to be most interesting were voted ‘Odd’ by Galaxy Zoo 2 volunteers. We then carried out comparable tests to identify mergers, rings and irregular galaxies in the DECaLS survey and found similarly improved results. Our method successfully identified each class of anomaly for our simulated user.

The third practical task was fine-tuning a convolutional neural network to solve a new galaxy classification task; specifically, to find ringed galaxies in DECaLS. We experimented with training the same architecture (EfficientNetB0) in three ways: from scratch, fine-tuned from ImageNet, and fine-tuned from Galaxy Zoo DECaLS (i.e. from our representations). In each case, we measured how the test loss varied with training data set size. We found that fine-tuning from Galaxy Zoo DECaLS performed best, especially when few labelled rings were available (as would typically be the case for a new task). We therefore suggest that researchers use our pretrained weights rather than ImageNet weights for models aiming to solve new galaxy classification tasks.

Together, solving these tasks demonstrates the utility that an appropriate representation can have. We believe the future of machine learning for galaxy morphology lies in the thoughtful creation and sharing of representations, so that researchers can build on top of one another’s models rather than creating them from scratch for each new problem.

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This research made use of the open-source PYTHON scientific computing ecosystem, including SCIPY (Jones et al. 2001), MATPLOTLIB (Hunter 2007), scikit-learn (Pedregosa et al. 2012), scikit-image (van der Walt et al. 2014), and PANDAS (McKinney 2010). We also used the active learning library ModAL (Danka & Horvath 2018) for our expected improvement acquisition function. This research made use of Astropy, a community-developed core python package for Astronomy (The Astropy Collaboration 2018). This research made use of TensorFlow (Abadi et al. 2016).

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DATA AVAILABILITY STATEMENT

To help the community benefit from our pretrained models, we release much of the code from this work as the documented Python package ‘zoobot’ at https://github.com/mwalmsley/zoobot. This includes code for training the Galaxy Zoo DECaLS models from scratch, calculating the representations of new galaxies, and fine-tuning the trained model to new classification problems. The repository also includes the weights of the trained model used in this work.

We release the remaining code for this work at https://github.com/mwalmsley/morphology-tools for reproducibility and future extension. This includes code for our similarity searches, our human-in-the-loop anomaly detection method, and our fine-tuning experiments.

The Galaxy DECaLS images and Galaxy Zoo DECaLS volunteer votes (with the exception of votes to the final multiple-choice question) were previously made available by Walmsley et al. (2022). The ‘ring’ multiple-choice answers are currently being used as part of a rigorous follow-up search for ringed galaxies in the DESI Legacy Surveys, powered by a combination of citizen science and deep learning. The complete ring catalogue will be publicly available.

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SUPPORTING INFORMATION

Supplementary data are available at MNRAS online.

Practical Morphology_Tools_Appendix

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