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The dust-to-ices ratio in comets and Kuiper belt objects

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ABSTRACT
Comet 67P/Churyumov-Gerasimenko (67P hereinafter) is characterised by a dust transfer from the southern hemi-nucleus to the night-side northern dust deposits, which constrains the dust-to-ices mass ratio inside the nucleus to values a factor two larger than that provided by the lost mass of gas and non-volatiles. This applies to all comets, because the gas density in all night comae cannot prevent the dust fall-back. Taking into account GIADA data collected during the entire Rosetta mission, we update the average dust bulk density to $\rho_D = 785^{+520}_{-115}$ kg m$^{-3}$ that, coupled to the 67P nucleus bulk density, confirms an average dust-to-ices mass ratio $\delta = 7.5$ inside 67P. The improved dust densities are consistent with a mixture of (20 ± 8)% of ices, (4 ± 1)% of Fe-sulphides, (22 ± 2)% of silicates, and (54 ± 5)% of hydrocarbons, on average volume abundances. These values correspond to solar chemical abundances, as suggested by the elemental C/Fe ratio observed in 67P. The ice content in 67P matches that inferred in Kuiper Belt Objects (KBOs hereinafter), (20 ± 12)% on average volume abundance, and suggests a water content in all Trans-Neptunian Objects (TNOs hereinafter) lower than in CI-chondrites. The 67P icy pebbles and the dust collected by GIADA have a microporosity of (49 ± 5)% and (59 ± 8)%. 

Key words: comets: general – comets: individual: 67P/Churyumov–Gerasimenko – Kuiper belt: general – Kuiper belt objects: individual: Pluto, Charon, Triton – protoplanetary discs – space vehicles

1 INTRODUCTION
While ground-based coma observations provide reliable measurements of the water loss rate, unrealistic assumptions of the dust size distribution have often provided strong underestimates of the dust loss rate from comets (Newburn & Spinrad 1985), with the consequence that the dust-to-ices mass ratio $\delta$ has been often assumed $< 1$. Here with dust we refer to the total non-volatile component of a comet nucleus. Often, the dust size distribution was assumed very steep, with both the dust mass and optical brightness dependent on micron-sized particles, opposite to what has been observed with Rosetta, with the 67P dust mass dependent on the largest ejected chunks, and the optical brightness on mm-sized particles (Rotundi et al. 2015; Fulle et al. 2016a). For example, Kresak & Kresakova (1987) provided the loss rates from most Jupiter Family Comets (JFCs hereinafter) assuming $\delta = 1/3$. In 67P, Kresak & Kresakova (1987) estimated a water loss rate per orbit about 20% larger than actual measurements (Bertaux 2015; Shinnaka et al. 2017). The Giotto mission to comet 1P/Halley showed that $\delta > 1$ and a more recent analysis of the Giotto dust data provided $3 < \delta < 40$ (Fulle et al. 2000). This result confirmed the $\delta$ estimates for JFCs (Sykes & Walker 1992a) based on the first ground-based observations able to infer reliable dust mass loss rates, derived by models of the IRAS dust trails (Sykes & Walker 1992b). Regarding 67P, Sykes & Walker (1992a) found $\delta = 4.6$, a good prediction of the values later confirmed by the Rosetta mission in the material lost by the comet, $\delta = 4 \pm 2$

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(Rotundi et al. 2015). In the same paper, Sykes & Walker (1992a) showed that the low bulk density of Pluto and Triton is consistent with the same volume abundances of dust and ices (of bulk density of 3000 and 1000 kg m\(^{-3}\), respectively) in these bodies. This implies \(\delta \approx 3\) and a common origin of all TNOs. This approach neglects the presence of hydrocarbons in the non-volatile mass of TNOs, although the CHON particles observed in 1P/Halley are mostly hydrocarbons (Jessberger et al. 1989). Best terrestrial analogues of hydrocarbons in the protoplanetary disc are soft hydrogenated carbon alloys (Robertson 2002), with a bulk density close to that of ices and a hardness up to 10 GPa, a factor ten larger than the central pressure of Pluto and Triton. The bulk density of TNOs may be due either to abundant ices or to hydrocarbons (Fulle et al. 2017). Models of Pluto and Charon assume a hydrocarbons-to-silicates mass ratio \(h/s = 0.2\), which implies \(\delta = 1.5\) (McKinnon et al. 1997). In 1P/Halley, the elemental abundances provide \(h/s > 0.9\) and a ratio \(C/Mg = 8\) (Jessberger et al. 1989), which is larger than the solar ratio \(C/Mg = 7\) (Lodders 2003) and cannot constrain \(\delta\). All these facts indicate that we cannot infer the real structure of comets and KBOs without fixing the ratios \(\delta\) and \(h/s\) (Fulle 2017), which is the aim of this paper.

2 67P DUST DEPOSITS PROVIDE \(\delta\)

The Rosetta mission has observed dust deposits many metres thick and mostly composed of particles of mass \(> 1\) mg (Fulle et al. 2016b), which cover about 80% of the 67P northern hemisphere (Keller et al. 2015b). The coheren orientation of tail-like features around boulders embedded in the dust deposits indicates a dust flow from south to north (Mottola et al. 2015). This implies that the deposits are built-up by a dust transfer occurring mainly at perihelion, when the comet activity is at its maximum, and most of the southern hemisphere is in a seasonal polar summer and eroded of many metres (Keller et al. 2015b). At the same time, most northern hemisphere is in a seasonal polar night: the very low gas pressure above that surface (and possibly the recondensation of some water from the coma back to the surface) makes the deposition on the northern hemisphere. On the contrary, the process of dust transfer from the sunlit nucleus surface to the night side one is independent of the duration of the polar night, because the physics of the night coma is independent of the spin stability. The day-to-night dust transfer is probably very similar in all comets, because the nucleus surface temperature on the night side, and therefore the gas outflow, is similarly low in all comets. Thus, the cut-off dust mass, below which the fall-back on the nucleus becomes less and less efficient, depends mainly on the nucleus mass. In 67P, the dust fall-back is efficient at masses \(> 1\) mg (Fulle et al. 2016b). This cut-off dust mass becomes even lower for comet nuclei of mass larger than that of 67P, and larger for the few comets with a lighter nucleus, e.g. 103P/Hartley 2. In this comet, dust deposits are further thinned by its unstable spin, with a fast and large precession excited by the gas torque on the light nucleus, so that the day-to-night dust transfer has no time to build-up thick deposits, which are eroded once the night surface is exposed to the sun.

The 67P dust deposits offer us a unique opportunity to measure the dust mass involved in the day-to-night dust transfer. The dust in the coma and the deposits have the same water mass fraction \(Z\), because the sublimation lifetime of dust is much longer than the day-to-night dust transfer, as shown below. The water mass fraction \(X \approx 6\%\) which is sublimating from the nucleus surface has been evaluated by thermo-physical models of the nucleus surface (Keller et al. 2015b; Blum et al. 2017). It is linked to the water mass fraction \(Y\) of the pristine terrains and to \(Z\) by means of two equations for the northern and the southern hemi-nuclei, respectively

\[
(1 - b) \ Y + b \ Z = a X \quad (1)
\]

\[
X + Z = Y \quad (2)
\]

where \(Y\) provides the dust-to-water mass fraction \(\delta_{\text{water}} = Y^{-1} - 1\) inside the nucleus, \(b \approx 0.8\) is the fraction of the northern nucleus surface covered by dust deposits (Keller et al. 2015b) and \(a \approx 1.05\) takes into account an active spot in Hapi (Fulle et al. 2016b), with an area about 1/20 of the northern hemisphere and with \(X\) a factor about ten larger than the average on the nucleus surface (Fougere et al. 2016). Eq. (2) describes a pristine surface exposed by the erosion of many metres (Keller et al. 2015b), with a water mass fraction \(Y\) partly released by water sublimation (\(X\)) and partly trapped in the ejected dust (\(Z\)). Eqs. (1) and (2) provide \(Y = (a + b) \ X \approx 11\%\), \(Z = (a + b - 1) \ X \approx 5\%\) and \(\delta_{\text{water}} \approx 8\), which is larger than \(\delta_{\text{water}} \approx 5\) provided by the dust and gas loss rates from 2 au to perihelion (Fulle et al. 2016a). 3D coma models constrain the gas loss rate from the coma dust to a fraction \(c < 5\%\) of that coming from the nucleus (Fulle et al. 2016b), so that the dust particles in the coma release a water loss rate \(c Q_w\) from their total water mass \(Z M_d\), where \(Q_w = 400 \pm 50 \ \text{kg s}^{-1}\) is the 67P perihelion water loss rate (Shinnaka et al. 2017) and \(M_d \approx 3 \times 10^8\) kg is the dust mass in particles of mass \(> 1\) mg. \(M_d\) has been computed inside the Rosetta orbit of radius \(R \approx 400\) km, where the mass in dust particles is \(R Q_w / \nu\) in the case of a spherical expansion at constant speed \(\nu\). The mass loss rate \(Q_m\) and \(\nu\) are provided by OSIRIS data (Fulle et al. 2016a). Actually, the mass in particles is larger, due to the dust acceleration from the nucleus to the distance \(R\). Particles reaching a nucleus distance larger than \(R\) have a negligible probability to fall back into the deposits. The day-to-night transfer lasts much less than \(Z M_d/(c Q_w) > 8\) days on average, supporting the assumption of the same \(Z\) in the dust deposits and in the coma dust.

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RSI (Radio Science Investigation) onboard Rosetta measured a total mass loss from 67P nucleus of \((1.1\pm0.3) \times 10^{10}\) kg from 2014, August, to 2016, September (Pätzold et al. 2016). During the same period, Hansen et al. (2016) estimated a water loss of \(6.4 \times 10^9\) kg by modeling Rosetta in-situ data, with a maximum water loss rate of \((3.5\pm0.5) \times 10^{28} \text{ mol s}^{-1}\), a factor 3 larger than provided by Earth-orbiting satellites, \((1.3 \pm 0.15) \times 10^{28} \text{ mol s}^{-1}\) (Shinnaka et al. 2017). This is inconsistent with e.g. water distributed sources, which imply in-situ measurements of the water loss rate lower than Earth-based ones. Such a systematic error of the water loss rate estimated by Hansen et al. (2016) at perihelion is confirmed by the overestimate by a factor 4 of the IR water flux modeled by Hansen et al. (2016) and Fougere et al. (2016) with respect to that measured by VIRTIS (Visible and Infrared Thermal Imaging Spectrometer, Bockelée-Morvan et al. (2016)), which makes VIRTIS water data consistent with Earth-based ones (Bertaux 2015; Shinnaka et al. 2017) and with the water loss rate fitting the acceleration of the 67P nucleus spin (Keller et al. 2015a). Taking into account the systematic correction of the total water loss provided by Hansen et al. (2016), it becomes consistent with previous estimates of \(2.7 \times 10^9\) kg (Bertaux 2015; Keller et al. 2015b), so that the RSI measurements provide \(\delta_{\text{water}} = 3 \pm 1\), again significantly lower than \(\delta_{\text{water}} \approx 8\) provided by Eqs. (1) and (2). This difference measures the dust mass involved in the day-to-night transfer. If \(\delta_{\text{water}}\) inside the nucleus were exactly that inferred for the lost material, the dust mass deposited on the night side would be exactly zero, according to the assumption that all the dust is lost in space. Instead, to obtain dust deposits, \(\delta_{\text{water}}\) inside the nucleus has to be significantly larger than the values observed in the lost material. In 67P, if the lost material has \(\delta_{\text{water}} = 3\) and the nucleus pristine material has \(\delta_{\text{water}} = 8\), i.e. 16 dust unit masses and 2 water unit masses, then 1 water unit mass is lost in space and another remains on the surface, together with 13 dust unit masses, so that the dehydrated material remaining on the nucleus surface has a water mass fraction of 7%, in good agreement with the water mass fraction \(Z = 5\%\) of the deposits. We infer that probably in all comets \(\delta_{\text{water}}\) inside the nucleus is about twice that measured in the lost material (e.g. by RSI or by means of JFC trail models).

3 GIADA DATA PROVIDE \(\delta\) AND \(H/S\)

GIADA (Grain Impact Analyser and Dust Accumulator) onboard Rosetta measured the speed, the scattered light and the momentum of individual dust particles by means of two subsystems (Della Corte et al. 2014): a laser curtain plus photodiodes (GDS, Grain Detection System) and a plate
connected to piezoelectric sensors (IS, Impact Sensor). Here we consider the complete set of 271 coupled GDS+IS detections during the entire mission, from August 2014 to September 2016. Ongoing calibrations performed on the GIADA spare model with cometary dust analogues (Ferrari et al. 2014) allowed us to refine the mass and the geometrical cross section of the GDS+IS detections (Fig. 1) with respect to those reported in Fulle et al. (2016c). The new calibrations shifted four of the five data-points with bulk density $> 4000 \text{ kg m}^{-3}$ to the area between the dotted lines in Fig. 1, and increased the data uncertainty close to the saturation of the GDS signal. We follow here the procedure described by Fulle et al. (2016c) to compute the average dust bulk density in 67P by means of the dust masses and cross sections measured by GIADA (Della Corte et al. 2015). (Della Corte et al. 2016). The data in Fig. 1 provide the weighted average dust bulk density $\rho_D = 785^{+250}_{-115}$ kg m$^{-3}$, where the weights are the inverse of the bulk density error derived from each error pair in Fig. 1. $\rho_D$ is linked to the non-volatiles-to-ices mass ratio inside the nucleus

$$\delta = \left[ \frac{\rho_N}{\phi_C \rho_D} - 1 \right]^{-1}$$

where $\rho_N = 533$ kg m$^{-3}$ is the 67P nucleus bulk density and $1 - \phi_C = 0.4$ is the nucleus macro-porosity (Fulle et al. 2016c). With $\rho_D = 785$ kg m$^{-3}$, we get $\delta = 7.5$ on average, consistent with $\delta_{\text{water}} \approx 8$ discussed in the previous section because at least 10% of 67P ices are composed of CO, CO$_2$ and O$_2$ (Fulle et al. 2016b). The lower and upper limits $\rho_D = 670$ kg m$^{-3}$ and $\rho_D = 1300$ kg m$^{-3}$ provide $\delta = 3.1$ and $\delta = \infty$, respectively. The 67P C/Fe ratio (Fray et al. 2016) is close to the solar end-case (Lodders 2003), so that the updated $\delta = 7.5$ and the solar elemental abundances constrain the free parameters of the structural equations of the 67P nucleus plotted in Figs. 2 and 3 of Fulle et al. (2016c), namely the micro-porosity and the volume abundances $c_1 = (4 \pm 1\%)$ of Fe-sulphides (bulk density $\rho_1 = 4000$ kg m$^{-3}$), $c_2 = (22 \pm 2\%)$ of silicates ($\rho_2 = 3200$ kg m$^{-3}$ for Mg,Fe-olivines and pyroxenes, $\rho_2 = 2600$ kg m$^{-3}$ for amorphous silicates (Fulle et al. 2016c)), and $c_3 = (54 \pm 5\%)$ of hydrocarbons ($\rho_3 = 1200$ kg m$^{-3}$). The upper limits are obtained for compact ices and the lower limits for porous ices. The volume abundance of ices in 67P is $c_2 = (20 \pm 8\%)$, with the upper limit corresponding to porous ices. This value matches the volume abundances of ices found in ten parameter combinations valid for KBOs (between the end-cases of solar and CI-chondritic compositions), $c_4 = (20 \pm 12\%)$ (Fulle 2017). The updated micro-porosity of the pebbles, i.e. the icy building-blocks of the 67P nucleus, is $1 - \phi_p = (49 \pm 5\%)$. The dust micro-porosity is $1 - (1 - c_4) \phi_p = (59 \pm 8\%)$, where the factor $(1 - c_4)$ takes into account the voids left in the dust by the ices after sublimation. The bulk density of compacted dust becomes $\rho_D/[(1 - c_4) \phi_p] = 1925^{+2000}_{-1250}$ kg m$^{-3}$. The upper limits of the micro-porosities and of the compacted bulk density are obtained for crystalline silicates and compact ices, the lower limits for amorphous silicates and porous ices.

5 CONCLUSIONS

For the first time, Rosetta data allowed us to constrain the dust-to-ices mass ratio in a Jupiter Family Comet by means of independent techniques. Also, thick dust deposits ubiquitous on 67P northern terrains allow us to infer that probably in all comets the dust-to-ices mass ratio inside the nucleus is about twice that most often measured in the lost material, e.g. by the RSI experiment and by trail observations. The water mass fraction of the dust deposits is $\approx 5\%$, very close to the water mass fraction sublimating from the average nucleus surface, thus making similar the activity from pristine terrains and that coming from the deposits. We obtain a pristine ice volume fraction of the 67P nucleus close to 20%, matching that directly provided by the bulk

4 DISCUSSION

Both 67P and KBOs contain only 1/5 of their volume as ice, thus less water than CI-chondrites (McKinnon et al. 1997). This suggests that bodies born close to the water snowline contain more water than TNOs. This is consistent with the D/H ratios in 67P (Allweg 2015) and 103P/Hartley 2 (Hartogh et al. 2011), which imply that 103P (apparently more water-rich than 67P) was born closer to the asteroidal belt than 67P (Fulle et al. 2016b). We have no data determining if the C/Fe ratio in 103P is lower than in 67P, i.e. closer to the CI-chondritic end-case, C/Fe $< 1$, than to the solar end-case, C/Fe $= 8.5$ (Lodders 2003). Although 1P/Halley shows a ratio C/Fe $= 16$ (Jessberger et al. 1989), even larger than the solar one, comets may also have a CI-chondritic C/Fe ratio, as it is confirmed by Stardust data and by KBOs. The composition of dust from comet 81P/Wild 2 is CI-chondritic, although the actual carbon bias on the data is unknown (Brownlee 2014). Fulle (2017) showed that Triton’s bulk density is consistent with a CI-chondritic composition, not with a solar one. Fray et al. (2016) find that the 67P C/Fe ratio is close to the solar end-case, although the bias in the detections of 67P’s C, Si and Fe remains unknown. In this case, the 67P ratios $h/s = (c_3/c_1)/(c_2/c_3)$, $c_2/c_1 = 5$, $c_3/c_1 = 12$ for porous ices and $c_3/c_1 = 14$ for compact ices match the values assumed to compute the KBO composition (Fulle 2017), and fix the largest possible KBO bulk density $c_3\rho_3$, where $c_3 = (1 + c_2/c_1 + c_3/c_1)^{-1}$ and $\rho_3 = c_3\rho_3 + 520(c_3/c_1)\rho_3$ (Fulle 2017). Porous ices and crystalline silicates provide $h/s = 0.9$ and $c_3\rho_3 = 1944$ kg m$^{-3}$, which implies an ice surface layer on Pluto with a thickness of $c_3 R/3 = 30$ km only, where $R$ is Pluto’s radius. Compact ices and amorphous silicates provide $h/s = 1.2$ and $c_3\rho_3 = 1720$ kg m$^{-3}$, which would make the bulk density of Pluto and Charon too inconsistent with a solar composition. The 67P $h/s$ ratios match the value measured in 1P/Halley (Jessberger et al. 1989) and are much larger than $h/s = 0.2$ assumed so far in models of Pluto and Charon (McKinnon et al. 1997). Impacts, tidal stress and the decay of radionucleides may decrease the pristine ice content during KBO lifetimes, implying that the pristine KBO bulk density may increase in time, without in any way overcoming the upper limit $c_3\rho_3$. 

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density of Pluto, Charon and Triton, just assuming that the composition of their non-volatile material is that measured in comets (Fulle 2017). The possible highly variable content in carbon, and the ice volume fraction in comets and KBOs, lower than in CI-chondrites, suggest multiple scenarios of their formation. Icy objects in the protoplanetary disc may have formed everywhere outside the water snow-line, with a composition of non-volatiles apparently independent of the solar distance during accretion, thus confirming a fast mixing of non-volatiles in the protoplanetary disc (Ciesla 2011). This is further confirmed by the sub-mm aggregates of minerals of bulk density $> 4000$ kg m$^{-3}$ observed by GIADA in 67P (Fig. 1). These minerals can have been formed only in the inner solar protoplanetary disc (Brownlee 2014). The variable ice content in KBOs suggests important migrations of the most icy objects (possibly comets and KBOs with a CI-chondritic composition of non-volatiles) outside the water snow-line, where they may have accreted. Memory of the accretion sun-distance may be preserved by the ratios D/H, O$_2$/H$_2$O and N$_2$/H$_2$O (Fulle et al. 2016b).

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