On the origin and magnitude of surface stresses due to metal nanofilms†

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Metallisation is a vital process for micro- and nanofabrication, allowing the controlled preparation of material surfaces with thin films of a variety of metals. The films are often subjected to further processing, including etching, patterning, chemical modification, and additional lamination. The extensive applications of metallised substrates include chemical sensors and nanoelectronics. Here, we report an experimental study of the metallisation of silicon cantilevers with nano-films of chromium and titanium. Analysis of the stress distribution throughout the cantilever showed that metallisation causes a constant stress along the length of the beam, which can be calculated from interferometric quantification of the beam curvature. The structure of the metal/silicon interface was imaged using electron microscopy in an attempt to ascertain the physical origin of the stress. A theoretical model is constructed for the stressed beam system, and it is shown that there is no single parameter that can describe the change in stress. The resultant structure after deposition varies significantly for each metal, which gives rise to a variety of stress directions and magnitudes.

Introduction

Many silicon based dynamic micro electromechanical systems (MEMS), for instance resonant pressure sensors, require metal deposition in order to be integrated with their control circuitry. These devices frequently comprise of compliant components such as beams or diaphragms. Deposition of metal on these structures affects their mechanical behaviour in a manner that is difficult to predict due to the presence of stresses induced in the system during deposition. Such stresses arise even when the conditions are controlled as to prevent thermal effects. Metallisation is an important intermediate step on the fabrication route to technologies including, but not limited to, microactuators,1 chemical detectors,2 resonators,3 and biosensors.4

Controlling the shape and deflection of high aspect ratio microfabricated structures is of particular importance when considering the design and operation of sensing elements, such as microcantilevers of crystalline materials. Stoney reported the first consideration of stress in deposited films5 and since then studies have evolved to consider static deflections,6–13 dynamic properties,14–21 and thermal noise spectra22 in an effort to incorporate the influence of additional loading on mechanical properties. Additional informative works in this field include a model exploring the evolution of stress during surface oxidation processes23 and an investigation into the change in static deflection in response to an applied temperature change.24

The aim of this work was to study the effect of metallisation on the deflection of flexible Si beams; the variables explored were the metal deposited and the thickness of the metal film. Pre-metallised Si atomic force microscope (AFM) cantilevers were prepared using a focused ion beam (FIB) for transmission electron microscope (TEM) visualisation of the crystal structure at the metal/silicon interface. Cantilevers were metallised with Ti and Cr thin films. These metals are not only important in their own right, but are often used as adhesion promoters for Au films.25 Both metals can form strong bonds between the native silicon oxide and the Au film. Without an adhesive interlayer, Au thin films deposited directly on Si are notoriously fragile. Au surfaces are used for a range of technologies, in particular the deposition of self-assembled monolayers, which are a well-understood and customisable platform for the chemical modification of surfaces.26 Applications involving the deposition and adhesion of 2D nanomaterials such as graphene27 will also benefit from advancements in the understanding and control of thin film stresses. Previous theoretical investigations of surface stress imbalances at Si interfaces have shown promise for the construction of nanomechanical sensors28 and the formation of nanotubes,29 employing...
formulæ based on Stoney\textsuperscript{5} for comparison. However, these studies have not resolved the origin of the surface stress; they have merely considered how the stresses could be exploited usefully. Further, the thickness of Si cantilevers which can be readily manufactured, and are commercially available, are typically much greater than those explored in these studies.

Classical laminated theory generally does not include the effects of interfacial or surface stress; here we report the development and application of a theory for laminated beams that takes into account the effect of this stress. By systematically depositing thin films of Ti and Cr onto one side of Si cantilevers it is shown that the magnitude and direction of this stress vary with the amount and type of metal deposited. We hypothesise that the stress is due to the lattice parameter mismatch between the metal thin film and the underlying Si. Further, the nature of the bonding between Si, native silicon oxide, and metal thin film will likely play an important role.

**Experimental**

**Film deposition**

Commercially available Si atomic force microscope (AFM) cantilevers (CSC12, MikroMasch, Estonia) were coated with thin films of either Cr (99.998\% purity, Kurt J Lesker, USA) or Ti (99.995\% purity, Kurt J Lesker, USA) using an Auto 500 electron beam evaporation system (Edwards, UK). Deposition rates were monitored in situ using a quartz crystal microbalance (QCM) and were in the range 10–100 pm s\(^{-1}\). Samples were held in place using 3M copper tape (RS Components, UK), and a water-cooled target was used to prevent thermal expansion effects.

**Atomic force microscopy (AFM)**

The thickness and spring constants of the unmodified cantilevers were obtained according to the method previously described by Bowen et al.\textsuperscript{30} The frequency of the first resonant mode of each cantilever was measured at 18 °C and 40\% relative humidity, using a NanoWizard II AFM (JPK Instruments, UK).

**Film thickness**

The thickness of the native oxide SiO\(_2\)/Si layer on the Si cantilevers was performed using a UVISEL spectroscopic ellipsometer (Horiba Scientific, UK) operating a Xe light source. The angle of incidence was fixed at 70\(^\circ\), and a wavelength range of 250–800 nm was used. DeltaPsi software was employed to determine the thickness values and the calculations were based on a three-phase ambient/SiO\(_2\)/Si(100) model, in which the SiO\(_2\) was assumed to be isotropic.

**Beam deflection**

Analysis of cantilever shape was performed using a MicroXAM2 white light interferometer (Omniscan, UK) operating a 10× lens (Nikon, UK). Acquired data was processed using SPIP software (Image Metrology, Denmark). Following export as ASCII, data were further analysed using Matlab (MathWorks, UK).

**X-ray photoelectron spectroscopy (XPS)**

XPS analysis of films was performed using a custom-built instrument operating an Al K\(_\alpha\) X-ray source, providing a monochromatic X-ray beam with incident energy of 1486.68 eV and a circular spot of 4 mm\(^2\) area. The region of the cantilever chip adjacent to the fixed end of the cantilever beam was analysed. The measurements were made at a pressure of 1×10\(^{-8}\) mbar, and samples were immobilized onto stainless steel sample holders using double-sided Shintron carbon sticky tape (Agar Scientific, UK). Low resolution survey spectra were obtained using a pass energy of 150 eV over a binding energy range of −10 to 1200 eV with 1 eV increments. High resolution spectra were obtained using a pass energy of 20 eV over a binding energy range of 20–30 eV, centred around a chosen photoelectron binding energy with 0.1 eV increments. A dwell time of 0.5 s was employed when collecting data from each binding energy increment for all measurements.

**Transmission electron microscopy (TEM)**

Cantilever cross-sections were prepared using an Auriga focused ion beam scanning electron microscope (FIB-SEM, Zeiss, Germany). A sacrificial platinum layer was deposited atop the metallised surface of the cantilever, to protect it from the milling beam. The crystal structure of the modified cantilever at the interface between the Si and metal film was then analysed using a Titan 80-30 TEM (FEI, USA). The chemical composition of the metal layer was analysed using energy-dispersive X-ray spectroscopy (EDX) and electron energy loss spectroscopy (EELS).

**Results and discussion**

**Beam shape due to metallisation**

The beam shape post-metallisation exhibits significant curvature in either the tensile or compressive direction (Fig. 1). The convention we employ here is that (i) tensile surface stresses curve the coated side of the beam downwards, whilst (ii) compressive surface stresses curve the coated side of the beam upwards. The beam in the top image is coated with 12 nm Ti, causing a tensile surface stress. The beam in the lower image is coated with 12 nm Cr, causing a compressive surface stress.

Quantification of the curvature was performed using interferometric analysis (Fig. 2). Beams coated with 12 nm Cr (Group 1) exhibit a more pronounced curvature due to compressive surface stress than beams coated with 6 nm Cr (Group 2). Uncoated beams exhibit no curvature (Group 3). Beams coated with 4.5 nm Ti (Group 4) exhibit curvature due to tensile surface stress, the curvature being more pronounced for beams coated with 12 nm Ti (Group 5). The surface stresses generated by the Ti and Cr films are such that a beam of approximate dimensions 100×35×1 μm (length, width, thickness) is curved upwards or downwards by 1 μm due to the
presence of a 12 nm metal film. The radius of curvature of these beams is on the order 10 mm. Classical analysis of cantilever beam deflection under its own weight suggests that unmodified cantilevers would exhibit maximum downward deflections of the order 95 pm. The presence of a Cr or Ti film of 12 nm thickness might be expected to add 3–5 nm of downwards deflection. The metal film masses are in the range 1–4% of the beam mass. These calculations are provided in the ESI.† It is certainly not possible to rationalise an upwards deflection using classical analysis.

Interface structure
Examination of the structure of the interface between the beam surface and metal film was performed using transmission electron microscopy (TEM). For the Ti interface (Fig. 3) the crystalline Si can be clearly seen, with an amorphous 3 nm thickness native oxide (SiO$_x$/SiO$_2$) layer immediately adjacent to the 12 nm Ti film, which exhibits a polycrystalline structure.

Particles of crystalline Ti with diameters ca. 5 nm can be observed throughout the layer; this was confirmed by fast Fourier transform (FFT) analysis of the X-ray scattering exhibiting a cell size of approximately 295 pm, commensurate with the reported 290 pm diameter of Ti atoms in crystalline metal. The amorphous structures can form due to the oxidation of Ti with the small amounts of O$_2$ remaining in the partial vacuum during deposition; the presence of O is confirmed by energy-dispersive X-ray (EDX) analysis (Fig. 3). X-ray photoelectron spectroscopy (XPS) analysis (Fig. 4) further confirms the presence of Ti and O in the 4.5 nm and 12 nm films.

For the Cr interface (Fig. 5) the crystalline Si can be seen, with an amorphous 3 nm thickness native oxide (SiO$_x$/SiO$_2$) layer immediately adjacent to the 12 nm Cr film, in which crystalline regions are visible. FFT confirmed that this layer was metallic Cr. Unlike the Ti film however, the Cr layer terminates with a CrO$_x$ layer, which may form upon exposure of the
freshly deposited Cr to atmospheric oxygen. The presence of O in this amorphous layer is confirmed by EDX analysis (Fig. 5), whilst XPS analysis (Fig. 4) further confirms the presence of Cr and O in the 6 nm and 12 nm films. The XPS results also indicate that there are two distinct binding environments; 2p3/2 photoelectrons from metallic Cr exhibiting a binding energy of 573 eV, whilst 2p3/2 photoelectrons from CrOx exhibiting a binding energy of 575 eV.

Surface stresses

The stress distribution at the silicon/metal interface was calculated by fitting eqn (1) to the vertical curvature of the cantilevers, as measured using white light interferometry (Fig. 6). A two-dimensional beam theory that captures the stress distribution due to a constant shear stress at the surface was developed, in which the axial and vertical displacements of the beam are considered. The full derivation is presented in the ESI.†

The vertical displacement of the beam, \( \nu \), is described by:

\[
\nu = \frac{\tau_1 + \tau_2}{6EI} wb \left( -3L^2x + x^3 + 2L^3 \right) - \frac{\tau_1 + \tau_2}{8G} (x - L) \tag{1}
\]

where, \( \tau_1 \) is the shear stress acting on the upper surface, \( \tau_2 \) is the shear stress acting on the lower surface, \( E \) is the Young’s modulus of the beam material of construction, \( I \) is the second moment of area, \( w \) is the beam width, \( 2b \) is the beam thickness, \( L \) is the beam length, \( G \) is the shear modulus of the beam material of construction, and \( x \) is the axial co-ordinate along the beam length, with the fixed end corresponding to \( x = 0 \).

The shear stress due to metallisation of the upper surface (ESI, Table 1†) is a function of both the beam length and the thickness of the deposited metal film. Cr films and Ti films cause surface stresses which act in opposite directions to each other. Further, for a given film thickness, Cr films cause a surface shear stress of greater magnitude than Ti films. The specific surface stress, \( \beta \), for each beam length and metal film thickness, \( t_{\text{metal}} \), can be calculated using eqn (2).

\[
\tau_1 = \frac{\beta t_{\text{metal}}}{L} \tag{2}
\]

The values of \( \beta \) for Ti films are \(-0.25 \text{ nN nm}^{-2} \) (4.5 nm) and \(-0.56 \text{ nN nm}^{-2} \) (12 nm), whereas for Cr films the values of \( \beta \) are 0.30 nN nm\(^{-2}\) (6 nm) and 1.08 nN nm\(^{-2}\) (12 nm). The relationship between film thickness and surface shear stress is indicative of an as-yet unresolved complex interaction between the metal film and the Si beam. There is an approximate correlation between the magnitude of the shear modulus for the metal film, and the magnitude of the beam deflection. Cr exhibits a shear modulus of 115 GPa, whereas Ti exhibits a shear modulus of 40 GPa. Future work on this topic should seek to explore the possible importance of this parameter.

The geometric arrangement of atoms at and around the beam/film interface should also be considered, particularly the possibility of competition for O atoms from the native silicon oxide layer upon deposition of the metal atoms. Consideration of the atomic diameters and the stoichiometry of the likely metal oxides which could form at the interface suggests that TiO\(_2\) formation could lead to a compressive stress, causing a downwards beam curvature. This is because TiO\(_2\) and SiO\(_2\) exhibit the same stoichiometry, yet Ti atoms exhibit a larger diameter (290 pm) than Si atoms (232 pm).\(^{31}\) Interestingly, with Cr atoms having diameters (250 pm) much closer to Si atoms, and with Cr\(_2\)O\(_3\) exhibiting a stoichiometry with a different metal/oxygen ratio to SiO\(_2\) and TiO\(_2\), the origins of the compressive stress and upwards beam curvature may be partly attributable to space filling effects.

An alternative approach is to consider the dimensions of the unit cells of each material, full details of which can be found in the ESI.† This analysis characterises the strain, \( \epsilon \), due to lattice mismatch between the metal film and the substrate.\(^{32}\) It is shown that both Ti and Cr films should both be in tension, i.e. upwards beam deflection. However, this is clearly not the case for the results obtained in this work, with opposing directions of beam deflection measured for Cr and Ti. It is likely that the structure of the deposited films prevents accurate analysis of crystal orientation effects, such as those performed by Shilo et al.,\(^{33}\) who used X-ray diffraction to...
examine strains in LiNbO₃. Hence, a predictive approach based on unit cell dimensions seems to be inappropriate here.

**Implications for micro/nanomanufacture**

The induced deformation caused by the metallisation can impact compliant micro and nano devices in a number of ways, both beneficial and deleterious. The most obvious repercussion would be a change of stiffness in the cantilever. Standard theory derived from the strength of materials gives the nominal stiffness of a rectangular cantilever as:

\[ k_{\text{nom}} = \frac{3EI}{L^2} \]  \hspace{1cm} (3)

However, from eqn (38) in the ESI† the peak deflection of the cantilever due to a point force acting downwards on the tip can be shown to be:

\[ \nu = -\frac{PL^3}{3EI} + \frac{Pb^2L}{2GI} + \frac{\tau_1 + \tau_2}{3EI} wbL^3 - \frac{\tau_1 + \tau_2}{8G} L \]  \hspace{1cm} (4)

where \( P \) is the magnitude of the point force.

Letting the algebraic sum of the stresses equal \( \tau_0 \), and using the standard definition of the shear stress,

\[ G = \frac{E}{2(1+\mu)} \]  \hspace{1cm} (5)

where \( \mu \) is the Poisson’s ratio of the cantilever substrate, the stiffness of the metallised cantilever, \( k_{\text{mod}} \), becomes:

\[ k_{\text{mod}} = \frac{3EI}{L^3 + 3b^2L(1+\mu)} \]  \hspace{1cm} (6)

The first term in the denominator is the same as given in eqn (3). The second term is due to the shear stresses in the cantilever induced by just the point load and has appeared owing to the higher order derivation used here. Frequently, it is thin cantilevers that are of interest. In this case, the stiffness reduces to the nominal stiffness given by eqn (3). Therefore the surface stress does not affect the stiffness. It does however cause a finite tip deflection, given by eqn (4), even when the point force is zero.

Following Bowen et al.,\(^30\) the resonant frequency of the beam becomes:

\[ f_{\text{res}} = \frac{1}{2\pi} \left( \frac{140Eb^2}{33L^2[2 + 3b^2(1+\mu)]} \right)^{1/2} \]  \hspace{1cm} (7)

Again this is not affected by the surface stress and reduces to the classical expression when the beam is very thin. This result was previously observed by Bowen et al.\(^30\) for coated Si cantilevers with resonant frequencies in the range 80–220 kHz.

When the surface stress is positive, *i.e.* compressive, the beam is curved upwards so that an applied point force acts to straighten the beam. The beam only becomes flat when

\[ P = \tau_0 wb \]  \hspace{1cm} (8)

If the amplitude of oscillations are small, it is possible that the surface stresses preserve the direction of the normal stresses within the beam while it oscillates, *i.e.* a surface in tension may remain in tension, whereas in an unstressed beam the stress will fluctuate between compression and tension. The stresses in this case will also be larger in magnitude (see eqn (14) in section 2 of the ESI†). This will have an impact on the fatigue life of the beam. Traditionally, it was believed that Si was immune to fatigue, however, it was observed recently that micro-scale Si structures may succumb to fatigue failure limiting the useful life of the structure. Normally, fatigue occurs when a structure is exposed to repeated cycles of varying stress. Cracks can form and propagate when a structure is under tension. In Si, this can expose fresh Si which then oxidizes resulting in further stress and crack propagation.\(^34\) This is more likely to be the case if crack initiation sites exist due to prior fabrication processes, such as dry etch and release processes which result in a rough surface finish.\(^35\)

Metallisation of a Si structure can affect the fatigue life in two ways. If the metallised surface results in a tensile surface stress, the opposite surface may remain in compression throughout the entire oscillation cycle preventing cracks from being opened and exposing fresh Si. The metallised surface itself may also hinder further oxidation of the surface in tension. In this way, one would expect the metallisation process to improve the nominal fatigue life of the component. However, the inverse is also true. If the metallised surface results in a compressive stress, the opposite surface may remain in tension and unprotected. In this state, cracks are more likely to open and become oxidized, thus reducing the fatigue life of the component.

Having a curved surface can be advantageous in the field of optoelectronics,\(^36,37\) in particular in the design of optical systems for digital cameras.\(^38\) Metallisation may be a convenient way of controlling the curvature of light focusing arrays, with the added advantage that external forces can be used to modify the curvature further, perhaps to remove aberrations such as astigmatism. The curvature of the beam, \( \kappa \), is defined by:

\[ \kappa = \frac{d^2v}{dx^2} \left[ 1 + \left( \frac{dv}{dx} \right)^2 \right]^{3/2} \]  \hspace{1cm} (9)

where, again derived from eqn (38) in the ESI† and assuming a thin beam:

\[ \frac{dv}{dx} = \frac{(L^2 - x^2)}{2EI} [P - \tau_0 wb], \quad \frac{d^2v}{dx^2} = \frac{-x}{EI} [P - \tau_0 wb] \]  \hspace{1cm} (10)

This means the curvature of the beam varies along its length. This is in contradiction with the classic model by Stoney\(^5\) who assumed perfect bending and hence derived a constant curvature along the beam. As can be seen in Fig. 7, the trend is essentially linear and varies from 0 m⁻¹ at \( x = 0 \) to the peak curvature, \(-L[P - \tau_0 wb]/EI\), at \( x = L \). Therefore, a system which can focus on different parts of the beam can take advantage of the change in the local curvature.

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In situ monitoring of film growth would also be of benefit, particularly when considering the metal/silicon interaction. Cantilevers with a range of lengths have been coated with chromium and titanium with different thicknesses have been analysed using TEM, EDX and EELS in order to ascertain the physical origin of this stress. It was shown that there is no single parameter that can describe the change in stress as a function of the metal or film thickness. This is because the resultant structure after deposition varies significantly for each metal. Analysis of the stress distribution throughout the cantilever showed that metallisation causes a constant stress along the length of the beam, which can be calculated using interferometric data.

The methodology presented here provides a valuable tool for studying this phenomenon in greater detail for a wide range of metals. Extending the methodology further to non-metals could also be of benefit, particularly when considering those materials which readily oxidise upon exposure to O₂. Understanding the magnitude and direction of surface stresses for nanofilms deposited on flexible substrates will be of great benefit to academia and industry, not least those concerned with the design and manufacture of MEMS devices and optoelectronics.

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