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THE ENVIRONMENTAL DEPENDENCE OF GALAXY COLORS IN INTERMEDIATE-REDSHIFT X-RAY–SELECTED CLUSTERS

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ABSTRACT

We present a wide-field imaging study of the colors of bright galaxies (\( <M^* + 2 \)) in a sample of 12 X-ray–selected clusters and groups of galaxies at \( z \sim 0.3 \). The systems cover one of the largest ranges in X-ray luminosity (\( L_X \sim 10^{38} - 10^{45} \text{ ergs s}^{-1} \)), and hence mass, of any sample studied at this redshift. We find that the “red” galaxies form a tight color–magnitude relation (CMR) and that neither the slope nor zero point of this relation changes significantly over the factor of 100 in X-ray luminosity covered by our sample. Using stellar population synthesis models, we find that our data allow a maximum possible change of 2 Gyr in the typical age of the “red” galaxies on the CMR over the range of \( L_X \) of our sample. We also measure the fraction of blue galaxies (\( f_b \)) relative to the CMR in our clusters and find a low value of \( f_b \sim 0.1 \) consistent with other X-ray–selected cluster samples. We find that there is no correlation between \( f_b \) and \( L_X \) over our large \( L_X \) range. However, we do find that both the CMR and \( f_b \) depend significantly on cluster radius, with the zero point of the CMR shifting blueward in \( B - R \) by 0.10 ± 0.036 mag out to a radius of 0.75 times the virial radius. This color change is equivalent to a luminosity-weighted age gradient of \( \sim 2.5 \text{ Gyr per log (radius)} \) and is consistent with previous studies of the radial change in the zero point of the CMR. It thus appears that the global cluster environment, in the form of cluster mass (\( L_X \)), has little influence on the properties of the bright cluster galaxies, whereas the local environment, in the form of galaxy density (radius), has a strong effect. The range of \( \sim 100 \) in \( L_X \) corresponds to a factor of \( \sim 40 \) in ram pressure efficiency, thus suggesting that ram pressure stripping or other mechanisms that depend on cluster mass, like tidal stripping or harassment, are unlikely to be solely responsible for changing the galaxy population from the “blue” star-forming galaxies, which dominate low-density environments, to the “red” passive galaxies, which dominate cluster cores.

Subject headings: galaxies: clusters: general — galaxies: elliptical and lenticular, cD — galaxies: evolution — galaxies: fundamental parameters

1. INTRODUCTION

The first clear evidence for galaxy evolution in clusters was presented by Butcher and Oemler (BO) in a series of papers in the late 1970s and early 1980s. Initially, they demonstrated that the fraction of blue galaxies (\( f_b \)) in two high-redshift centrally concentrated clusters (Butcher & Oemler 1978a) was significantly higher than that found in similar local clusters (Butcher & Oemler 1978b). This suggests that unlike the cores of local compact clusters, which contain almost exclusively quiescent early-type galaxies, similar clusters at high redshift contain many star-forming galaxies in addition to the early-type galaxies. This result was subject to significant scrutiny, particularly the required statistical removal of foreground and background galaxies (Mathieu & Spinrad 1981; Dressler & Gunn 1982; Koo 1981). In an attempt to resolve this, Butcher & Oemler (1984) studied 33 galaxy clusters up to a redshift of 0.5. This showed an increasing trend of blue fraction with redshift, but with a large scatter. Several other studies have reported similar trends. For instance, Roskos & Schombert (1995) find an even faster increase but do not limit their clusters to centrally concentrated ones, and Margoniner et al. (2001) also confirm a similar trend using a large sample of Abell clusters.

Follow-up observations of the BO blue galaxies showed spectroscopic signatures of galaxies with either ongoing or recently truncated star formation (Couch & Sharples 1987; Dressler & Gunn 1983; Lavery & Henry 1986), and morphological studies have shown most of these galaxies to be late-type spirals but with an increased incidence of a disturbed or interacting appearance (Dressler et al. 1994; Oemler et al. 1997; Couch et al. 1994, 1998; Lavery & Henry 1988).

However, it is not clear that the increased blue fraction is universal. Smail et al. (1998), using 10 bright X-ray clusters at \( z \sim 0.25 \), have found no significant evidence for an increase in the blue fraction, and Allington-Smith et al. (1993) showed no increase in radio-selected groups. It has also been suggested that the clusters studied at high redshift are not similar to those that were observed locally. For example, Andreon & Ettori (1999) have shown that the Butcher and Oemler clusters have increasing X-ray luminosities with redshift.

While evidence exists for strong evolution in the late-type population of clusters, the early-type galaxies have shown very little evidence of evolution beyond the passive aging of their stellar populations. In particular, studies of the correlation between the colors and magnitudes of early-type galaxies (Sандage & Visvanathan 1978a, 1978b) in clusters (Bower et al. 1992a, 1992b; Terlevich et al. 2001) have shown that this relation has a small scatter and evolves very little to high redshift (Ellis et al. 1997; Stanford et al. 1998). This slow evolution in the slope, zero point, and scatter of the color–magnitude relation (CMR) suggests that the stellar populations of early-type galaxies were formed at high redshift (\( z \gtrsim 2 \)), evolving purely passively since,
with the slope being consistent with a metallicity sequence rather than an age sequence (Kodama & Arimoto 1997; Kodama et al. 1998).

The only evolution in the early-type population in clusters appears to be in the number of S0 galaxies. A spectroscopic and Hubble Space Telescope study (MORPHS) of 10 rich galaxy clusters (0.37 < z < 0.56) found that the fraction of elliptical galaxies remained constant, but that the fraction of S0 galaxies decreased with redshift (Dressler et al. 1997). Further, they found an increase in both the star formation rate and the number of galaxies showing evidence of recent star formation (Poggianti et al. 1999) with redshift. However, a similar spectroscopic study of high-redshift rich clusters, this time X-ray selected, found a very weak redshift dependence of the star formation rate with redshift (e.g., CNOC; Balogh et al. 1999).

The decrease in S0 galaxies and the increase in blue star-forming galaxies and galaxies with recently truncated star formation with redshift have often been linked. It has been suggested that spiral galaxies falling into the cluster environment may be halting their star formation followed by a rapid truncation of their star formation. This results in the fading of the disk and the formation of an S0 galaxy. Several mechanisms that can occur in the cluster environment may be driving this transformation. These include ram pressure stripping (Gunn & Gott 1972; Fujita 1998, 2001; Fujita & Nagashima 1999; Abadi et al. 1999; Quilis et al. 2000), galaxy harassment (Moore et al. 1996, 1998, 1999), tidal effects (Byrd & Valentijn 1990; Henriksen & Byrd 1996; Fujita 1998), and strangulation (Larson et al. 1980; Balogh et al. 2000; Dienerio et al. 2001). These processes have the effect of removing an infalling galaxy’s gas supply and thus halting ongoing star formation. This idea has been further reinforced by the change in galaxy properties with cluster radius. The morphology-radius/density relation (Oemler 1974; Dressler 1980) at low redshift is an excellent example of this and first inspired the idea that a galaxy’s star formation may be halted by the cluster environment, resulting in a morphological transformation (Gunn & Gott 1972; Oemler 1974). This relation was further shown to exist at high redshift (Dressler et al. 1997; Treu et al. 2003).

Similarly, Butcher & Oemler (1984) showed that the blue fraction increased with radius in their clusters, and this trend has generally been confirmed by other studies (e.g., Abraham et al. 1996; Kodama & Bower 2001; Fairley et al. 2002). Balogh et al. (1997) that the star formation rate depends strongly on cluster radius in the CNOC sample. In the same sample, they find no radial dependence of the fraction of post-starburst/star-forming galaxies, unlike the MORPHS clusters (Poggianti et al. 1999).

Both, however, conclude that the truncation of star formation is independent of the morphology-density relation. Recently, two large studies using the latest galaxy redshift surveys (2dF, Lewis et al. 2002; SDSS, Gómez et al. 2003) have found very clear relationships between star formation and density in the vicinity of clusters. Both studies find a characteristic density (radius) at which the average star formation rate rapidly drops.

Some observational evidence also exists for an environmental dependence of the properties of elliptical galaxies in clusters. Abraham et al. (1996) find that the galaxies on the CMR become bluer as a function of cluster radius in A2390 at a redshift of 0.23. Terlevich et al. (2001) find a similar trend in the Coma Cluster, as do Pimbblet et al. (2002) in a combined sample of 11 rich clusters at z ~ 0.1.

When trying to draw general conclusions regarding the evolution of cluster galaxies as discussed above, one particular concern is how cluster selection may have affected the results. It has already been noted that the BO sample has systematic differences as a function of redshift. A further concern comes from the fact that the clusters used were those that already had available data. This meant that they were often unusual objects (Sandage et al. 1995), which was the reason they had been studied originally. This type of selection has often occurred (e.g., MORPHS; Stanford et al. 1998), and when other more careful selection criteria are used, differing results are found (e.g., CNOC; Smail et al. 1998). It should also be noted that the clusters studied have mainly been massive rich clusters, as they provide the best statistics and are easiest to locate at high redshift. This may be of particular concern as they are very rare objects and are unlikely to be the evolutionary predecessors of the clusters with which they are compared locally (Kauffmann 1995). Galaxy properties clearly depend on environment, and it may be that by studying only the most massive clusters a nonrepresentative picture of galaxy evolution has been generated.

This paper presents further results from a comprehensive study of galaxy populations in X-ray–selected clusters at both intermediate and high redshift. The clusters were selected to cover a wide range in X-ray luminosity (L_X), and all were imaged over a wide field in three bands. The wide range in X-ray luminosity and hence mass and the wide-field imaging allows us to simultaneously investigate how the cluster galaxy population depends on both cluster mass and cluster radius. In Fairley et al. (2002) we presented measurements of the blue fraction in an initial sample of eight clusters over a large redshift range. In this paper 12 intermediate-redshift clusters from the sample are used to investigate how the blue fraction and CMR depend on both X-ray luminosity and cluster radius.

Throughout this paper a cosmology with Ω_m = 0.3, Ω_Λ = 0.7, and H_0 = 70 km s^{-1} Mpc^{-1} is assumed.

2. CLUSTER SELECTION AND DATA

The 12 clusters presented here are selected to cover a large range of X-ray luminosities and hence cluster masses over a small redshift interval at z ~ 0.3. Because they are all selected using their X-ray emission and are at similar redshifts, comparison of their galaxy populations should be free of any selection effects driven by the cluster selection technique. The clusters were drawn from four X-ray–selected cluster samples: the Extended Medium Sensitivity Survey (EMSS; Gioia et al. 1990), the Southern Serendipitous High-Redshift Archival ROSAT Cluster (SSHARC; Collins et al. 1997; Burke et al. 2003), the Bright Serendipitous High-Redshift Archival ROSAT Cluster (BSHARC; Nichol et al. 1999; Romer et al. 2000), and the Wide Angle ROSAT Pointed Survey (WARPS; Scharf et al. 1997; Perlman et al. 2002). The low flux limits of SHARC and WARPs allow the selection of clusters with low L_X, whereas the large area of the EMSS allows the selection of rarer high-L_X clusters. Table 1 lists the name, original catalog, coordinates of the center, redshift, X-ray luminosity, and telescope (with which the observations were made) of the cluster sample.

2.1. Observations

Each cluster was imaged over a wide field of view through three filters, B, V, and R, in the Johnson-Cousins system. These filters correspond approximately to U, B, and V at rest at the cluster redshift, minimizing any K-corrections required. The imaging was undertaken using two telescopes: the Isaac Newton Telescope (INT) at the Roque de los Muchachos Observatory on the Island of La Palma and the Blanco Telescope at the Cerro Tololo Inter-American Observatory (CTIO), Chile. Each telescope was
equipped with a wide-field mosaic CCD camera. The INT Wide Field Camera (Ives et al. 1996) consists of four thinned EEV 2k × 4k CCDs mounted at the INT prime focus in an “L” configuration. Each CCD has a pixel size of 13.5 μm corresponding to 0′′33 on the sky. There are 2048 × 4100 pixels in the useful imaging area of each CCD, giving a field of view of 22′8 × 11′4. The four CCDs together give a total imaging area of ∼0.29 deg². The CTIO MOSAIC II camera consists of eight 2048 × 4096 SITE CCDs mounted in two rows of four. Each pixel is 15 μm corresponding to 0′′27 on the sky, giving each CCD dimensions of 9′2 × 18′4 and a total imaging area of ∼0.38 deg². The gaps between the CCDs are ∼40 pixels or 11″.

The INT data were acquired on four nights from 1999 June 17 to 20. The observing conditions were generally good through the four nights, except for the first night during which light cirrus cloud was present. Despite this, the observations were still made using slightly longer exposure times with calibration images of the same fields taken on the following night. It was also noted that Saharan dust was present in the upper atmosphere throughout the observations. This is a common feature at the Roque de Los Muchachos Observatory and is known to show “gray” absorption, increasing the atmospheric extinction equally over all wavelengths (King 1985). The CTIO data were taken on the nights of 2000 September 26 and 27. The observing conditions were good on both nights with no cloud cover. Tables 2 and 3 give details of the observations.
By a constant pixel scale. Before rebinning, the pixel scale was determined for each image, which was then used to rebin the image point. To correct for this, an accurate astrometric solution was derived using all pixels having the same sky level, which is incorrect for fields where there is significant variation of the pixel size across the CCD array. After flat-fielding the images, the curvature of the focal plane causes a significant error in the pixel size. Apertures with a physical diameter of 20 kpc were used to calculate the magnitudes. Apertures near very bright sources were also masked as these can affect the photometric errors. It is known that SExtractor’s total photometry estimate suffers from a decrease in the included flux with decreasing total flux. In order to calculate a correction to the total magnitude, isolated galaxies were identified on each image. Using the IRAF task PHOT, the magnitudes of these isolated galaxies within a large aperture were calculated in order to estimate the true total magnitude. For bright objects, the difference between the SExtractor’s total photometry and true total magnitude is approximately constant at ~0.04 mag or ~2%. This rose to ~0.2 mag for the faintest objects. These corrections were applied to all the total magnitudes. Apertures with a physical diameter of 20 kpc were used to calculate the colors, representing a minimum size of at least twice the seeing, thus ensuring that the small seeing variations between images do not affect the colors. The observed colors of each object were used to apply the color corrections determined from the standard solutions giving the final magnitudes for each object. In order to remove any spurious detections, objects that were not detected in at least two bands were removed from the catalog. Finally, the number of bad pixels present in an object was calculated from the exposure masks and added to the catalog. Any object with more than 10% bad pixels in a band had the magnitude in that band flagged. The final catalogs of all measured objects in a field contained between 15,433 and 39,977 objects.

2.4. Star-Galaxy Separation

In order to differentiate stars from galaxies, a method similar to that presented in Metcalfe et al. (1991) was used. A concentration parameter was defined as the magnitude within 4 pixels divided by the total magnitude. Figure 1 shows the concentration parameter as a function of magnitude for two example cluster fields. The stars are visible as the horizontal linear feature in the plots and are clearly separated from the galaxies at bright magnitudes. The solid lines define the region chosen to represent the mean extinction and color terms. Again they were found to be sufficiently consistent (rms < 0.01) to combine and use as one term for the whole mosaic. Although using one photometric solution for the whole array may slightly increase the photometric errors, it greatly simplifies the photometric measurements for the stacked images since spatial offsets between the individual images mean that a single patch of the stacked image can have contributions from several CCDs.

The INT calibration proceeded in a similar manner. However, fewer images of standard fields were observed over too low a range in air mass, preventing an accurate determination of the extinction. Instead, extinction coefficients were used from the Carlsberg Meridian Telescope, a photometric monitoring telescope on the observatory site. As for the CTIO, data zero points and color terms were first determined for each individual CCD to ensure that they were consistent and then combined to determine zero points for the whole array.

2.3. Constructing Galaxy Catalogs

Object detection and photometry were performed using the Source Extractor package (SExtractor; Bertin & Arnouts 1996). Objects were detected on the $R$-band images only, with photometry then being performed on all three images using the objects from the $R$ detection. A Gaussian filter of size equal to the image seeing was used during the detection process to better differentiate between faint sources and noise peaks. The areas around very bright sources were also masked as these can affect the galaxy’s background determination, leading to poor photometry. Both total photometry, using a modified Kron aperture (Kron 1980), and aperture photometry were performed.

It is known that SExtractor’s total photometry estimate suffers from a decrease in the included flux with decreasing total flux. In order to calculate a correction to the total magnitude, isolated galaxies were identified on each image. Using the IRAF task PHOT, the magnitudes of these isolated galaxies within a large aperture were calculated in order to estimate the true total magnitude. For bright objects, the difference between the SExtractor’s total photometry and true total magnitude was approximately constant at ~0.04 mag or ~2%. This rose to ~0.2 mag for the faintest objects. These corrections were applied to all the total magnitudes. Apertures with a physical diameter of 20 kpc were used to calculate the colors, representing a minimum size of at least twice the seeing, thus ensuring that the small seeing variations between images do not affect the colors. The observed colors of each object were used to apply the color corrections determined from the standard solutions giving the final magnitudes for each object. In order to remove any spurious detections, objects that were not detected in at least two bands were removed from the catalog. Finally, the number of bad pixels present in an object was calculated from the exposure masks and added to the catalog. Any object with more than 10% bad pixels in a band had the magnitude in that band flagged. The final catalogs of all measured objects in a field contained between 15,433 and 39,977 objects.

### Table 3

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Notes.—Summary of the cluster observations made at the CTIO from 2000 September 26 to 27. For each cluster the filter, the night, the total exposure time, the number of exposures, and the mean seeing are listed.

CTIO MOSAIC camera, and a model has been developed to correct the data.

Wide-field imaging requires a step not normally necessary in CCD data reduction. The curvature of the focal plane causes a significant variation to the pixel size across the CCD array. After flat-fielding all pixels have the same sky level, which is incorrect for pixels of different sizes and leads to a varying photometric zero point. To correct for this, an accurate astrometric solution was determined for each image, which was then used to rebin the image to a constant pixel scale. Before rebinning, the pixel scale changed by ~4% in the INT WFC and ~8% in the CTIO MOSAIC II camera from the center to the edge of the array and would thus cause a significant error in the photometry across the field.

Before combining the individual images into final stacked images of each cluster in each band, the photometric scales were matched, correcting for variations in the sky level, extinction, and exposure times. This was done by comparing the flux of a number of stars that appear on each image. The corrected images are then stacked using a mean, excluding pixels in the bad pixel mask.

The photometric calibration was achieved using images of standard-star fields (Landolt 1992) taken throughout each night. Fields covering a large area were chosen so that it was possible to place standard stars on every CCD with one pointing. For the CTIO data there were sufficient standards to fit for a zero point, an extinction, and a color correction term on each CCD on each night. As would be expected, the extinction terms were all equivalent within the errors and so a weighted mean was taken. The zero point and color terms were then refitted. Although the color terms may be expected to vary slightly between CCDs, the small size of these corrections meant that they were equivalent within their errors and a weighted mean was again used to give a final color term for each CCD. The zero points were then refitted using
stars in each plot. These criteria had to be selected for each cluster individually as this parameter is dependent on the image seeing, with increasing seeing moving the locus of stars to higher values and greater width. The seeing was observed to vary across the wide field of our images, up to 10% in the CTIO images and 20% in the INT images. The effect of this radial variation in the seeing is to just broaden the stellar locus, reducing the magnitude with which the separation can occur, but not causing any systematic change in the separation with radius. The B-band data were not used for the final separation as they displayed a larger scatter in the stellar locus. The separation was typically effective to an R magnitude of ~22. Fainter than this, the number counts are dominated by galaxies. Any remaining stars will be included in the field region in equal proportions as in the cluster regions and thus will be removed by the statistical background subtraction (see § 3.2).

To confirm the reliability of this method, the star and galaxy classifications in the field of RX J0256.5 were compared to those of the Sloan Digital Sky Survey (SDSS; York et al. 2000), which also images this field. The SDSS star-galaxy separation is reliable to $m_R \approx 22$, comparable to the magnitude at which the separation was possible here. Of the 2558 galaxies, 52 were classified as stars by the SDSS, and of the 1155 stars, 87 were classified as galaxies by SDSS. The SDSS star-galaxy separation is approximately 95% accurate at these depths (Lupton et al. 2001), suggesting that the separation here is at least as accurate.

The final step in the construction of the galaxy catalogs is to correct for galactic extinction. To apply the required corrections, the maps of Schlegel et al. (1998) were used. Typically, one extinction correction is applied per field. However, the resolution of these maps is sufficient to map variations over the wide fields of the images used here. Investigation showed that the extinction could vary by up to 25% across a field. Therefore, the extinction was calculated for each galaxy individually by using the interpolation options available in the codes provided with the Schlegel et al. (1998) maps.

2.5. Photometric Checks and Completeness

Before using the photometry for our scientific investigation, it is reassuring to check its accuracy against external sources and to determine if the observations have achieved the desired depth and accuracy. Fortunately, two of the fields imaged here have existing photometry from other sources that may be used to check the reliability of the photometry presented here.

Tyson et al. (1998) measured Johnson B and $B-R$ photometry for 99 stellar objects in the field of RX J1418.5. Sixty-five of these objects have photometry measured by SExtractor, of which 41 are stars. Comparing with our B and R photometry for these 41 stars shows a median difference of less than 0.03 and an rms $\approx 0.1$, showing a good consistency between the data sets to $m_R = 22$.

The field of RX J0256.5 has photometry available from the SDSS in the Sloan filters ($u, g, r, i, z$). Using the conversions from Smith et al. (2002) and the Sloan point-spread function (PSF) magnitudes, the equivalent total $B, V$, and $R$ magnitudes were calculated for all of the stars present in both data sets. The conversions were found to be less reliable at either end of the $g - r$ color range and so the sample was restricted to $0.5 \leq g - r \leq 1.2$, leaving 1076 stars in common. The median offset was found to be $< 0.03$ in all of the filters with an rms $< 0.09$ to $m_R = 22$, showing excellent agreement between the two data sets.

Figure 2 shows the number-magnitude relations (NMRs) in the $R$ band using the SExtractor total magnitudes. Reassuringly, the relations are similar for all of the cluster fields but do show some scatter as would be expected from cosmic variance. The mean density can vary by almost a factor of 2 between cluster fields. This illustrates the importance of individual estimates of the background density when correcting cluster galaxy counts (see § 3.2). Plotted on the $R$-band NMR are the relations derived by Metcalfe et al. (1991) and Smail et al. (1995). These are consistent with the NMRs of the cluster fields, providing another confirmation of the photometry.

These relations can be used to estimate the completeness of the galaxy catalogs. The NMRs clearly begin to turn over as the number of galaxies falls off. Table 4 lists the estimated completeness in the detection bands and the original target equivalent to $M_F = -19$ for an elliptical galaxy at redshift zero. These values were estimated by observing the position at which the NMR appears to turn over. This level of precision was adequate, as the questions considered in this paper typically use galaxies at least ~1 mag brighter than these limits.

3. ANALYSIS AND RESULTS

3.1. Defining a Characteristic Radius

The variation in the mass of our cluster sample means that each cluster has a different physical size. In order to compare the
galaxy populations between clusters, we must define some characteristic radius that is equivalent for all of the clusters. If we just use a fixed physical scale, it may include just the core of the most massive clusters and substantially beyond the core of the least massive. To this end, Butcher & Oemler (1978b) defined a characteristic radius, $R_{30}$, within which they measured the blue fraction. $R_{30}$ is defined as the radius containing 30% of the total number of galaxies in a cluster. To calculate this, it is necessary to integrate the cluster density profile up to the edge of the cluster ($R_{100}$) after subtracting the background galaxy density. Most other studies of the Butcher-Oemler effect have attempted to calculate $R_{30}$ for their clusters (e.g., Smail et al. 1998; Kodama & Bower 2001; Fairley et al. 2002; Pimbblet et al. 2002). Apart from the original Butcher and Oemler papers, details of the calculation of $R_{30}$ are scarce, particularly as $R_{100}$ and the background level were determined (although see Andreon et al. 2004).

Here we attempted to determine $R_{30}$ by the following procedure. For each cluster, the density profile was calculated in 0.25 bins, by counting all galaxies whose centers lay in each bin up to a limiting $R$ magnitude of 22.5. The area in each radial bin was then calculated using the exposure masks of each image. Only the areas that had maximum exposure in all three bands and the galaxies within those areas were included. A further correction to the area was required to take into account the effects of large objects and crowding. Large objects potentially obscure galaxies in front of or behind them. This can be a problem, particularly in the cores of dense clusters where many bright elliptical galaxies lie. For all objects larger than 900 pixels, an estimate was made of the area brighter than the deblending threshold. These estimates were then summed and subtracted from the previously calculated area.

Figure 3 shows the integrated number of galaxies as a function of radius for four example clusters. The integrated number was calculated by subtracting a background density typically calculated as the mean density in the region 11′–17′ from the cluster center. In some instances, this was adjusted to avoid obvious overdensities in the background.

In order to calculate $R_{30}$, it was necessary to first determine the cluster “edge,” $R_{100}$. This was difficult, as the edge was lost in the variations of the background density. In most clusters, a number of radii seemed applicable as a possible $R_{100}$, and it was unclear which, if any, represents the “real” cluster edge.

The profiles in Figure 3 illustrate the difficulty in calculating $R_{30}$ particularly for the low-$L_X$ clusters. Aside from determining the cluster edge, the choice of background density can also have a large effect on $R_{30}$. The unphysical nature of the very rapidly rising or falling total number–radius plots for some clusters (e.g., RX J0054.1) demonstrates this sensitivity. To further highlight this problem, Figure 4 shows how the total number of galaxies as a function of radius varies when the background density is changed. The background level is changed by its ±1 σ error, resulting in wild variations in the total number profiles. This may be a particular problem for previous studies that have used a small field of view to image the clusters and then a separate global background estimate. The difficulty in determining $R_{30}$ is further illustrated using the cluster MS 1455.0. Smail et al. (1998) calculated an $R_{30}$ of 2.2 for this cluster, whereas Fairley et al. (2002) found 3.75, and this study either 1.56 or 3.07 depending on the choice of the cluster edge. This could potentially be a significant problem for blue fraction studies, particularly when comparing samples from different authors, considering that the blue fraction has been shown to depend on radius (Butcher & Oemler 1984; Abraham et al. 1996; Kodama & Bower 2001; Ellingson et al. 2001).

In an attempt to reduce some of the systematic uncertainties in calculating $R_{30}$, it was decided to define another characteristic radius using the X-ray properties of this cluster sample. Assuming that the cluster core is virialized, in a simple self-similar

<table>
<thead>
<tr>
<th>Cluster</th>
<th>Slope</th>
<th>Zero Point</th>
<th>Target Magnitude</th>
<th>Completeness</th>
</tr>
</thead>
<tbody>
<tr>
<td>RX J1633.6</td>
<td>-0.041</td>
<td>3.17 ± 0.35</td>
<td>21.08</td>
<td>23.6</td>
</tr>
<tr>
<td>RX J0333.0</td>
<td>-0.041</td>
<td>3.19 ± 0.35</td>
<td>21.15</td>
<td>23.7</td>
</tr>
<tr>
<td>RX J0210.4</td>
<td>-0.041</td>
<td>3.28 ± 0.35</td>
<td>21.20</td>
<td>23.5</td>
</tr>
<tr>
<td>RX J0054.0</td>
<td>-0.041</td>
<td>3.33 ± 0.35</td>
<td>21.67</td>
<td>23.4</td>
</tr>
<tr>
<td>RX J1606.7</td>
<td>-0.041</td>
<td>3.37 ± 0.35</td>
<td>21.84</td>
<td>23.4</td>
</tr>
<tr>
<td>RX J2237.0</td>
<td>-0.015</td>
<td>2.82 ± 0.26</td>
<td>21.73</td>
<td>23.3</td>
</tr>
<tr>
<td>MS 0407.2</td>
<td>-0.037</td>
<td>3.04 ± 0.43</td>
<td>20.96</td>
<td>22.9</td>
</tr>
<tr>
<td>RX J1418.5</td>
<td>-0.010</td>
<td>2.76 ± 0.26</td>
<td>21.68</td>
<td>23.3</td>
</tr>
<tr>
<td>RX J0256.5</td>
<td>-0.056</td>
<td>3.74 ± 0.32</td>
<td>22.31</td>
<td>23.7</td>
</tr>
<tr>
<td>MS 0353.6</td>
<td>-0.022</td>
<td>2.95 ± 0.22</td>
<td>21.94</td>
<td>23.3</td>
</tr>
<tr>
<td>MS 1455.0</td>
<td>-0.048</td>
<td>3.34 ± 0.33</td>
<td>21.30</td>
<td>22.7</td>
</tr>
<tr>
<td>MS 2137.3</td>
<td>-0.075</td>
<td>4.01 ± 0.67</td>
<td>21.87</td>
<td>23.3</td>
</tr>
</tbody>
</table>

**Note.**—The median $B - R$ CMR slope and zero points calculated from the biweight fits to the 100 realizations of the background subtraction with the errors given as the rms of these fits and the $R$-band completeness limit estimated from the NMR.
model (Bryan & Norman 1998; Eke et al. 1998) the virial radius, $R_V$, is given by

$$R_V = 3.80 \beta_T^{-1/2} \Delta_z^{-1/2} (1 + z)^{-3/2} \left( \frac{kT}{10 \text{ keV}} \right)^{1/2} h_{50}^{-1},$$  \hspace{1cm} (1)$$

with

$$\Delta_z = \frac{\Delta_c(\Omega_c, \Lambda) \Omega_0}{18 n^2 \Omega_z}$$  \hspace{1cm} (2)$$
taken from Arnaud et al. (2002), where $\Delta_c(\Omega_c, \Lambda)$ is the density contrast and $\beta_T$ is the normalization of the virial relation $GM_V/2R_V = \beta_T kT$. A value of $\beta_T = 1.05$ (Evrard et al. 1996) is used here. An analytic approximation for $\Delta_c(\Omega_c, \Lambda)$ is given in Bryan & Norman (1998).

Only three clusters in our sample have measured temperatures to use in the above relation: MS 0353.6, MS 1455.0 (Mushotzky & Scharf 1997), and MS 2137.3 (Ettori & Fabian 1999). For the rest of the sample, it was necessary to convert the measured $L_X$ to temperature. This was done using the redshift-dependent $L_{X-T}$ relation,

$$T = \left[ \frac{L_{bol}}{B(1 + z)^3} \right]^{1/\alpha},$$  \hspace{1cm} (3)$$

where $B = (3.11 \pm 0.27) \times 10^{44} h^{-2} \text{ ergs s}^{-1}$, $A = 1.5 \pm 0.3$, $\alpha = 2.64 \pm 0.27$ (Markovitch 1998; Vikhlinin et al. 2002), and $L_{bol}$ is the bolometric luminosity.

A conversion from the ROSAT $L_X$ to $L_{bol}$ was required before the above $L_{X-T}$ relation could be used. This conversion was calculated using a model X-ray spectrum. The shape of the spectrum is dependent on the temperature, and hence so is the conversion. The two steps were therefore combined iteratively, with an initial estimate of temperature used to calculate $L_{bol}$, which was in turn used in the $L_{X-T}$ relation to estimate the temperature, which was again fed into the $L_{bol}$ conversion and so on until convergence. This procedure converged rapidly within three to five iterations.

The complexity of the above method, combined with the existence of significant scatter in the $L_{X-T}$ relation and the requirement of a virialized cluster core, calls into question the reliability of $R_V$ and its superiority over $R_{50}$. Since all of these clusters show reasonably strong X-ray emission, the likelihood of the cores being virialized is high. To estimate how large an error both this conversion and the $L_{X-T}$ scatter may have introduced, the same method was applied to the data of Mushotzky & Scharf (1997). They measured the temperatures of 38 clusters between a redshift of 0.143 and 0.541 using ASCA. A typical error of 20% was found between the measured temperatures and those calculated with the $L_{X-T}$ relation, which leads to only a 10% error in $R_V$. This error and the previously mentioned uncertainties seem acceptable considering the particular advantages this method has in the removal of the fairly arbitrary decision on the position of the cluster edge and its independence on the heavily fluctuating field density. The calculated values of $L_{bol}$, $T$, and $R_V$ are shown in Table 5.

Another advantage of X-ray data is revealed when determining the cluster center. The centroid of the X-ray emission yields the deepest point in the cluster potential well. This often coincides with a bright elliptical galaxy. When this occurred, the center of this galaxy was used as the cluster center. Otherwise,

TABLE 5

<table>
<thead>
<tr>
<th>Cluster</th>
<th>Redshift</th>
<th>$L_X$ ROSAT (10^{44} \text{ ergs s}^{-1})</th>
<th>$L_{bol}$ (10^{44} \text{ ergs s}^{-1})</th>
<th>$kT$ keV</th>
<th>$R_V$ (Mpc)</th>
<th>$R_V$ (arcmin)</th>
</tr>
</thead>
<tbody>
<tr>
<td>RX J1633.6...</td>
<td>0.239</td>
<td>0.10 ± 0.02</td>
<td>0.24 ± 0.05</td>
<td>1.53 ± 0.27</td>
<td>1.17 ± 0.10</td>
<td>5.16 ± 0.44</td>
</tr>
<tr>
<td>RX J0333.0...</td>
<td>0.245</td>
<td>0.12 ± 0.02</td>
<td>0.30 ± 0.06</td>
<td>1.67 ± 0.27</td>
<td>1.22 ± 0.11</td>
<td>5.27 ± 0.43</td>
</tr>
<tr>
<td>RX J0210.4...</td>
<td>0.273</td>
<td>0.16 ± 0.02</td>
<td>0.41 ± 0.06</td>
<td>1.86 ± 0.28</td>
<td>1.26 ± 0.10</td>
<td>5.02 ± 0.40</td>
</tr>
<tr>
<td>RX J0054.0...</td>
<td>0.293</td>
<td>0.24 ± 0.03</td>
<td>0.66 ± 0.10</td>
<td>2.19 ± 0.31</td>
<td>1.34 ± 0.10</td>
<td>5.10 ± 0.38</td>
</tr>
<tr>
<td>RX J1606.7...</td>
<td>0.310</td>
<td>0.69 ± 0.06</td>
<td>2.24 ± 0.24</td>
<td>3.47 ± 0.33</td>
<td>1.66 ± 0.08</td>
<td>6.08 ± 0.29</td>
</tr>
<tr>
<td>RX J2237.0...</td>
<td>0.299</td>
<td>1.09 ± 0.08</td>
<td>3.85 ± 0.35</td>
<td>4.28 ± 0.31</td>
<td>1.86 ± 0.07</td>
<td>6.98 ± 0.26</td>
</tr>
<tr>
<td>MS 0407.2...</td>
<td>0.229</td>
<td>1.87 ± 0.41</td>
<td>3.63 ± 0.95</td>
<td>4.32 ± 0.52</td>
<td>1.98 ± 0.12</td>
<td>9.03 ± 0.54</td>
</tr>
<tr>
<td>RX J1418.5...</td>
<td>0.294</td>
<td>2.96 ± 0.20</td>
<td>12.47 ± 1.10</td>
<td>6.69 ± 0.45</td>
<td>2.34 ± 0.08</td>
<td>8.87 ± 0.30</td>
</tr>
<tr>
<td>RX J0256.5...</td>
<td>0.360</td>
<td>3.44 ± 0.17</td>
<td>14.71 ± 1.01</td>
<td>6.93 ± 0.48</td>
<td>2.25 ± 0.08</td>
<td>7.46 ± 0.27</td>
</tr>
<tr>
<td>MS 0536.6...</td>
<td>0.320</td>
<td>7.05 ± 1.38</td>
<td>17.53 ± 4.31</td>
<td>8.13 ± 0.36</td>
<td>2.52 ± 0.06</td>
<td>9.03 ± 0.22</td>
</tr>
<tr>
<td>MS 1455.0...</td>
<td>0.259</td>
<td>12.81 ± 0.40</td>
<td>36.74 ± 1.69</td>
<td>5.60 ± 0.29</td>
<td>2.20 ± 0.06</td>
<td>9.15 ± 0.25</td>
</tr>
<tr>
<td>MS 2137.3...</td>
<td>0.313</td>
<td>15.48 ± 2.11</td>
<td>45.65 ± 8.42</td>
<td>5.00 ± 1.10</td>
<td>1.99 ± 0.22</td>
<td>7.23 ± 0.80</td>
</tr>
</tbody>
</table>

Notes.—The calculated bolometric luminosities, temperatures, and virial radii for all clusters using the $L_{X-T}$ relation of Vikhlinin et al. (2002). For MS 0353.6, MS 1455.0, and MS 2137.3 the temperatures quoted are those taken from Mushotzky & Scharf (1997) and Ettori & Fabian (1999). The errors in $R_V$ are calculated from the $L_X$ error along with the errors on the $L_{X-T}$ relation.
the X-ray centroid was used. When only optical imaging data are present, the cluster center is often determined by the position of the brightest cluster galaxy. It has been demonstrated (Lynam et al. 2000) that this can often lead to an incorrect choice, potentially affecting the measurement of cluster properties.

3.2. Statistical Field Correction

In order to study the cluster galaxy population, it was first necessary to correct for the presence of foreground and background field galaxies along the cluster line of sight. A field region was defined for each cluster as the area outside a radius of 3 Mpc. Having a large field of view allowed a field sample to be constructed for each cluster, which should better take into account variations in large-scale structure along the different lines of sight.

Following the method of Pimbblet et al. (2002), the probability of each galaxy being a cluster member was determined in a color-magnitude grid of size 0.5 in magnitude and 0.1 in color by comparing the numbers of galaxies in the cluster and field regions. One hundred realizations of the cluster membership were then determined using this probability grid.

3.3. Fitting the Color-Magnitude Relation

Although the color-magnitude distribution is dominated by the red galaxies defining the relation to be fitted, there is still significant contamination from bluer galaxies. To overcome this contamination, a robust biweight fit was made to the data, which assigns increasingly lower weights to outlying points. Beers et al. (1990) give scale ($S_B$) and location estimators ($C_B$) based on the biweight method. Using these estimators, the slope ($M$) and normalization ($C$) of the CMR are determined in turn. The CMR residual was defined as res = $(M \times \text{magnitude} + C) - \text{color}$. First, the residual was minimized in $S_B$ with $C = 0$. This yielded the slope of the relation $M$. Then the residual was minimized in $C_B$ with $M$ fixed, giving the normalization of the relation. The procedure was carried out for all clusters in each realization of the CMR that would then be used for all of these clusters individually. To construct the composite, it was first necessary to K-correct the galaxy colors and magnitudes to account for the differences in redshift, and hence filter bandpass, between the individual clusters. This was done using the K-corrections of Fukugita et al. (1995) with mean corrections of amplitude 0.08, 0.06, and 0.03 in $B$, $V$, and $R$, respectively. Figure 5 shows 1 of the 100 composite color-magnitude diagrams before and after K-corrections were applied, with the resultant biweight fit.

Figure 6 shows $B - R$ versus $R$ color-magnitude diagrams for the 12 clusters. This filter combination was chosen because it approximates $U - V$ versus $m_B$ at rest, thus spanning the 4000 Å break and providing a sensitive measure of the age of an old stellar population (Dressler & Shectman 1987; Bruzual 1983). The filled circles show galaxies selected as being in the cluster, and the dots show those in the field for this statistical realization. In all plots, the median biweight fits of all of the statistical realizations are shown by solid lines and the 3σ errors on the fits by the shaded regions. Details of these fits are given in Table 4. For the low-$L_X$ clusters fitted as a composite, the zero points have been K-corrected back to the redshift of the individual clusters. We note that fits were also made to CMRs generated with the other filter combinations and that adding these to the analysis below does not change our results.

By inspecting the color-magnitude plots, it can be seen that most of the clusters show clear CMRs. Those that do not, such as RX J0333.0 and RX J1633.6, are of low richness as might be expected from their very low X-ray luminosities and thus have very few galaxies with which to define a relation. When these clusters are combined together (Fig. 5), a relation does become apparent. On plotting the fit from this composite cluster on the individual color-magnitude diagrams, a concentration of galaxies about the fit is then visible.

3.4. The Dependence of the Color-Magnitude Relation on Cluster Mass

As discussed in §1, the uniformity of CMR provides tight constraints on any variation in the star formation history of early-type galaxies. This section investigates whether or not the CMR is universal over the large range in cluster X-ray luminosity, and hence mass, present in the sample of clusters studied here.

The properties of the CMR considered here are the slope and zero point, represented as the color at a fiducial magnitude. In order to investigate how these properties vary with cluster $L_X$, it is necessary to first correct for any dependence on redshift. Figure 7 shows the slope and zero point as a function of redshift for the clusters. The low-$L_X$ clusters, whose CMRs were fitted together in a composite, are shown as one point in these plots. Also shown on these plots are model predictions for the CMR using the PEGASE2 stellar population synthesis models (Fioc & Rocca-Volmerange 1997) normalized to the Coma CMR at a redshift of 0.023 (Bower et al. 1992b). Clearly there is some discrepancy between the models and the fits. Considering first the evolution of the slope, a large scatter is immediately noticeable, as well as systematically shallower slopes than the models predict. One possibility for the steeper model slopes is the large apertures used to determine the colors. The Coma data, used to normalize the models, used a much smaller aperture to calculate the colors. Since there are radial color gradients in elliptical galaxies, with redder colors nearer the centers, this has the effect of increasing the slope as the inner regions are sampled in the brightest galaxies. Figure 7 also shows the zero point of the CMR of each cluster, defined as the color of a galaxy lying on the fitted CMR that would have an absolute $V$-band magnitude of $-21.2$ at a redshift of zero. Again, there is a discrepancy between the models and the fitted CMRs, with the cluster fits appearing...
Fig. 6.—$B - R$ CMRs for all 12 clusters. All galaxies to half a virial radius and to a limiting magnitude of $M_{\text{lim}} = -20$ are shown. The filled circles are galaxies designated as cluster members and the dots as field members in one iteration of the statistical background subtraction. The solid near-horizontal line shows the median biweight fit to the relation and the shaded area the 3σ error on that fit from the background correction. For the five lowest $L_X$ clusters the fit shown is that to the composite cluster $k$-corrected back to the individual cluster redshift. The dashed vertical line shows the color-dependent magnitude cut (see § 3.6).
redder than the models. The photometric checks discussed in § 2.5 suggest that the photometry is much more accurate than the 0.1–0.2 mag offset visible here. Allied to the consistent offset over both independent data sets, it appears that there may be a problem with the model $B$ magnitudes. This may not be too surprising; Eisenstein et al. (2001) found that the PEGASE models were unable to reproduce the color evolution of luminous red galaxies in the SDSS, particularly in $g - r$, predicting either too red colors at low redshift or too blue at intermediate redshift. We have tied the models to the colors of the low-$z$ red galaxies in the Coma Cluster, which has made the models too blue at the intermediate redshift of the galaxies studied here.

Although the model slopes are offset from the measured slopes, the evolution with redshift appears to be consistent in form. This is seen in the bottom left panels of Figure 7, where no gradient with redshift is apparent. Therefore, it is still possible to use the models to remove the redshift evolution of the slope in order to investigate any dependence on $L_X$, and this is plotted in Figure 8.

For the zero points, the models are clearly inadequate. Unlike the slopes, a tight relationship between zero point and redshift is visible. This enables an empirical determination of the relationship to be made and subtracted in order to investigate the $L_X$ dependence. It is safe to do this, as there is no dependence of $L_X$ on redshift within this sample.

Figure 9 shows the fits and residuals to the zero-point–redshift relations. The fits are simple, linear least-squares fits and provide good representations of the data. Figure 10 shows the residuals to the fits as a function of X-ray luminosity.

Inspecting Figures 8 and 10, the CMR shows no dependence on cluster X-ray luminosity in either its slope or zero point over a factor of 100 in X-ray luminosity. This is confirmed by Spearman rank tests, with correlation probabilities of 82% and 61% for the slope and zero point, respectively, consistent with no trend. The scatter in both the slope and zero-point $L_X$ relations is consistent with being driven by the measurement errors.

Even though the range in X-ray luminosity is large, the number of clusters considered is quite small, and the errors and scatter in these plots are quite large. It is therefore worth considering how much of a trend would still be consistent with these plots. To calculate this, a simple least-squares fit weighted by the errors was made to the relations in Figures 8 and 10. A maximum variation of 0.091 in the slope and 0.090 in the zero point was
allowed by the 2σ error to the fits over the entire $L_X$ range of the clusters. The change in the slopes allowed is quite large; however, the maximum zero-point change is well constrained.

If the change in zero point is considered to be due to an age change, the maximum age change allowed can then be estimated. Using the PEGASE2 models, an age change of 1 Gyr corresponds to a color change of $\sim 0.05$ in $B - R$ at $z \sim 0.3$. This means that an age difference of greater than $\sim 2$ Gyr is ruled out at the 2σ level. It therefore appears that the global environment does not have a strong effect on the ages of early-type galaxies in clusters.

### 3.5. The Dependence of the Color-Magnitude Relation on Cluster Radius

In the previous section we investigated how the CMR depends on the global environment of a galaxy cluster, as measured by its X-ray luminosity. Another environmental change we can probe is the variation of local galaxy density as measured by cluster radius. One approach to investigating the CMR as a function of radius would be to try and fit the CMR in radial bins for each cluster. However, rapidly decreasing cluster galaxy densities, and thus increasing field subtraction errors, make this unfeasible. Instead, all of the clusters are combined together using a method similar to that described in Pimbblet et al. (2002). Since we have already shown that the properties of red sequence galaxies are independent of the X-ray luminosity of the cluster in which they reside, we can be confident that no significant biases due to the large range in $L_X$ have been introduced when the entire cluster sample is combined together. The lowest $L_X$ clusters, while contributing many fewer galaxies than the highest $L_X$ clusters, do make a significant contribution, with the five lowest $L_X$ clusters together adding a similar number of cluster galaxies as one of the richest.

Figure 11 shows the surface density of the galaxies lying close...
to the CMR for each cluster. The clusters are generally centrally concentrated with approximately circular density contours, and any irregularities should be smoothed out when the clusters are combined.

Before combining, the CMR fits were subtracted from the galaxy colors of each cluster; i.e., for each galaxy the color difference $[\Delta(B - R)]$ from the fitted CMR was calculated. This was repeated for every galaxy in the cluster area (within $2R_v$) and for every galaxy in a combined field sample. The combined field sample was constructed by including all of the galaxies in the cluster fields at a radius greater than $2.5 R_v$ from the cluster center. A combined sample is used here, rather then a field sample for the 12 clusters. The solid histogram shows the fitted Gaussian, and the dashed line shows the position of the Gaussian peak.

Figure 12 shows the combined histograms, in four radial bins, for the 12 clusters. The solid histogram shows the field-corrected data, and the dotted histogram shows all data prior to the field correction. Each panel shows the histogram in the radial bins of $0.25R_v$, except the final panel, which shows the histogram in a larger bin, between $0.75R_v$ and $1.25R_v$, in an attempt to increase the signal caused by the low cluster density at these radii. The central bin (top left panel) shows the clear peak of the cluster CMR. This gets smaller with increasing radii and disappears in the final bin (bottom right panel) at $\sim R_v$.

To investigate any change in the color of the CMR with cluster radius, we wished to determine if and how the cluster peak color and width change. To do this, a Gaussian was fitted iteratively to the histogram data around the peak between $-0.4$ and $0.4$ in $\Delta(B - R)$, thus ignoring the very bluest galaxies, which become more significant at larger radii. The results of these fits are given in Table 6 and are shown in Figure 12 by the dot-dashed curves, with the center of the Gaussian fit shown by a dashed line. To generate errors on the fits, random Gaussian noise scaled to each bin’s Poisson error was added to each histogram bin, and then the fit was recalculated. This was repeated 10,000 times with the final fits and errors calculated as the mean and rms. A Gaussian fit was used to define the peak instead of other location estimators such as the biweight, as it could be fitted to data including negative bins, whereas the biweight cannot.

The peak of the Gaussian fits shows a clear trend of becoming bluer with increasing radius in the first three bins, with the fourth bin being very noisy with a large error on the fit. A total shift blueward of $0.10 \pm 0.036$ mag was observed over $0.75R_v$. The fact that the first bin shows a positive peak is reassuring, since the subtracted CMR was fitted within $0.5R_v$, and so would lie between the first two radial bins considered here. The width of the CMR shows no evidence of any significant change with radius. However, the errors on the width are large, so definite conclusions regarding the CMR width are difficult.

The color difference from the fitted CMR, the equivalent of a $k$- and evolutionary correction has been applied based on the empirical colors of the galaxies lying on the CMR of each cluster. This “correction” is likely to be more accurate than any determined by models, as it has been determined using the data on which it was to be applied. Its only limitation is that the equivalent of one correction was applied to all galaxies regardless of how close their color lies to that of the CMR. However, as the galaxies of interest here are those lying close to the CMR and the redshift range is small, any systematic errors would be much smaller than those introduced by using model $K$-corrections.

Figure 12 shows the combined histograms, in four radial bins, for the 12 clusters. The solid histogram shows the field-corrected data, and the dotted histogram shows all data prior to the field correction. Each panel shows the histogram in the radial bins of $0.25R_v$, except the final panel, which shows the histogram in a larger bin, between $0.75R_v$ and $1.25R_v$, in an attempt to increase the signal caused by the low cluster density at these radii. The central bin (top left panel) shows the clear peak of the cluster CMR. This gets smaller with increasing radii and disappears in the final bin (bottom right panel) at $\sim R_v$.

To investigate any change in the color of the CMR with cluster radius, we wished to determine if and how the cluster peak color and width change. To do this, a Gaussian was fitted iteratively to the histogram data around the peak between $-0.4$ and $0.4$ in $\Delta(B - R)$, thus ignoring the very bluest galaxies, which become more significant at larger radii. The results of these fits are given in Table 6 and are shown in Figure 12 by the dot-dashed curves, with the center of the Gaussian fit shown by a dashed line. To generate errors on the fits, random Gaussian noise scaled to each bin’s Poisson error was added to each histogram bin, and then the fit was recalculated. This was repeated 10,000 times with the final fits and errors calculated as the mean and rms. A Gaussian fit was used to define the peak instead of other location estimators such as the biweight, as it could be fitted to data including negative bins, whereas the biweight cannot.

The peak of the Gaussian fits shows a clear trend of becoming bluer with increasing radius in the first three bins, with the fourth bin being very noisy with a large error on the fit. A total shift blueward of $0.10 \pm 0.036$ mag was observed over $0.75R_v$. The fact that the first bin shows a positive peak is reassuring, since the subtracted CMR was fitted within $0.5R_v$, and so would lie between the first two radial bins considered here. The width of the CMR shows no evidence of any significant change with radius. However, the errors on the width are large, so definite conclusions regarding the CMR width are difficult.

The peak of the Gaussian fits shows a clear trend of becoming bluer with increasing radius in the first three bins, with the fourth bin being very noisy with a large error on the fit. A total shift blueward of $0.10 \pm 0.036$ mag was observed over $0.75R_v$. The fact that the first bin shows a positive peak is reassuring, since the subtracted CMR was fitted within $0.5R_v$, and so would lie between the first two radial bins considered here. The width of the CMR shows no evidence of any significant change with radius. However, the errors on the width are large, so definite conclusions regarding the CMR width are difficult.

A clear variation in the color of the CMR with radius is seen for a combined sample of 12 intermediate-redshift clusters. Removing the slope of the CMR before the radial comparison is made ensures that any color change is independent of the magnitude distribution of the galaxies in a radial bin. This is important, as the magnitude distribution will change, with the most massive, brightest, and hence reddest galaxies being located in the cluster center. Pimbblet et al. (2002) measured the change in
of the galaxies and thus the larger fractional age gradient with radius. Turning to the width of the fitted Gaussian, there is little
evidence of any trend in the data presented here, contrary to that
found by Pimbblet et al. (2002), although the large errors make
definite conclusions difficult (see also Balogh et al. 2004).

Several other authors have reported similar radial color changes
of the CMR. Abraham et al. (1996) studied a single cluster, A2390,
at a redshift of 0.23, with both photometry and spectroscopy,
over a wide area. They found that the colors of galaxies on the
CMR became bluer with radius with a gradient of \( \frac{d(g-r)}{d \log r} = -0.079 \) out to 3.7 Mpc, equivalent to \( \sim 1.15R_v \) calculated
from the X-ray temperature measurement of Allen et al. (2001). Terlevich et al. (2001) reported a blueing of the \( U-V \)
CMR in Coma as a function of cluster radius. Converting to the
\( g-r \) color used by Abraham et al. (1996), they report a change
of \( \frac{d(g-r)}{d \log r} = -0.024 \pm 0.005 \). Pimbblet et al. (2002) similarly
converted their \( B-R \) color to \( g-r \) and find \( \frac{d(g-r)}{d \log r} = -0.061 \pm 0.011 \), which is intermediate between the
other two studies.

Converting the \( B-R \) color difference of the cluster sample
presented here to \( g-r \) produces \( \frac{d(g-r)}{d \log r} = -0.081 \pm
0.019 \), consistent with the trend of Abraham et al. (1996) at the
same redshift. Using simple evolutionary models presented in
\( \S \) 3.4, the age change corresponding to these color changes is
calculated, assuming that the galaxies are formed at a redshift
\( >2 \). This enables the rate of age change per \( \log r \) to be determined.
The results of these calculations are shown in Table 7.

All four studies produce very consistent results with a luminosity-
weighted age change of \( \sim 2.5 \) Gyr per \( \log r \), accounting for the
radial color change. Both Abraham et al. (1996) and Pimbblet
et al. (2002) explain this change as a result of an increase in youn-
ger S0 galaxies contaminating the CMR at larger radii. Dressler
et al. (1997) show that the fraction of S0 galaxies in clusters
declines with increasing redshift, suggesting that S0 galaxies in
clusters have been formed relatively recently. They further sug-
uggest that infalling spiral galaxies in the field are transformed into
S0 galaxies by the truncation of their star formation. This may
result in a gradient of younger S0 galaxies with cluster radius.
Pimbblet et al. (2002) suggest that the increasing width of the
CMR histogram they observe supports this, with a larger range of
galaxy colors expected from the spread in age of the recently
formed S0 galaxies. Unfortunately, due to the large errors, it is
difficult to distinguish between no trend and that of Pimbblet
et al. (2002) here. Recently Hogg et al. (2004) have conducted a
similar study of bulge-dominated galaxies in the SDSS. They
find evidence of a small shift in the peak color (<0.02 mag \( g-r \))
and a broadening of the blue wing of galaxy color distribution
with density, further supporting this hypothesis.

### 3.6. The Blue Fraction

In the previous sections we have investigated the properties of the
red cluster galaxies as a function of cluster environment. We

### TABLE 7

<table>
<thead>
<tr>
<th>Study</th>
<th>Number</th>
<th>( z )</th>
<th>( \Delta(g-r)/\log r )</th>
<th>( \Delta(g-r)/\text{Gyr} )</th>
<th>( \Delta(\text{age})/\log r )</th>
</tr>
</thead>
<tbody>
<tr>
<td>Terlevich et al. (2001)</td>
<td>1</td>
<td>0.023</td>
<td>-0.024 ± 0.005</td>
<td>0.0083</td>
<td>-2.9 ± 0.6</td>
</tr>
<tr>
<td>Pimbblet et al. (2002)</td>
<td>11</td>
<td>0.12</td>
<td>-0.061 ± 0.011</td>
<td>0.0151</td>
<td>-2.5 ± 0.7</td>
</tr>
<tr>
<td>Abraham et al. (1996)</td>
<td>1</td>
<td>0.23</td>
<td>-0.079 ± 0.02</td>
<td>0.0283</td>
<td>-2.8 ± 0.7</td>
</tr>
<tr>
<td>This paper</td>
<td>12</td>
<td>0.28</td>
<td>-0.081 ± 0.019</td>
<td>0.0323</td>
<td>-2.5 ± 0.6</td>
</tr>
</tbody>
</table>

Note.—Rate of change of \( g-r \) peak color as a function of \( \log \) projected radius, the calculated change in color per Gyr of an old
stellar population, and the resulting rate of change of age as a function of projected radius from four photometric studies of clusters.
now turn to the blue cluster galaxy population and calculate the fraction of blue galaxies ($f_b$) following the method of Butcher & Oemler (1984). Butcher & Oemler defined the blue galaxies as those 0.2 mag bluer than the CMR in rest-frame $B - V$. One approach to calculating $f_b$ would therefore be to $k$-correct all of the data to the rest-frame $B - V$. However, a simpler approach suggested by Kodama & Bower (2001) is to $k$-correct the blue galaxy criteria to the cluster redshift. A $B - V$ color 0.2 mag bluer than an elliptical galaxy falls between the colors of an Sab and Sbc at a redshift of zero. The blue fraction cut was thus defined as the color at the same position between an Sab and an Sbc at the cluster redshift, using the colors and $K$-corrections of Fukugita et al. (1995). The blue fraction cuts are listed in Table 8.

Butcher and Oemler also defined $f_b$ to be measured to a limiting $M_V$ of $-20$ at $z = 0$. At higher redshifts, this limiting magnitude depends on spectral type. Again, the Fukugita et al. (1995) colors and $K$-corrections were used to determine the limiting magnitude for each cluster, which are shown by the triple-dot-dashed lines in Figure 6. These lines are close to vertical in most cases, due to the clusters being chosen at redshifts where the measurement filters map approximately onto rest $UBV$. The limiting magnitude for each cluster at the color of an elliptical galaxy is given in Table 8.

On calculating the blue fraction, a field correction was again required. However, since $f_b$ is a simple measure that splits all of the galaxies into just two groups, the complicated grid method was not necessary. Again, the background was determined for each cluster at radii $>3$ Mpc. The galaxies in both the cluster and field areas were then split into blue and red galaxies in the same manner. These numbers were then scaled by the relative corrected areas, which are calculated in the same manner as in §3.3. The field numbers were then subtracted from the cluster numbers to give $f_b$ simply as residual blue galaxies divided by the residual total galaxy population. The error in $f_b$ was determined using the Poisson errors on the numbers of galaxies in the blue and red, cluster and field samples using the equations of Gehrels (1986).

When determining the field errors, it was important to consider the clustering of galaxies. To estimate this effect, the variance in the field region on the size of the cluster area was determined for each image. This was done by splitting the field into a grid, with each grid square having the same area as the cluster within which $f_b$ is measured. The number of blue and red galaxies was calculated in the manner described above, and the mean and rms of this distribution determined. The rms was then used as the error in the field numbers as it represents how the field beneath the cluster is typically varying, based on the local galaxy distribution. This rms error was always larger than the Poisson error on the whole background by a factor of $\sim 8$, resulting in an increased error in $f_b$ of $\sim 50\%$.

In order to investigate any dependence of the blue fraction on redshift and X-ray luminosity in a manner consistent with Butcher and Oemler, $f_b$ was first calculated within a radius of $R_{\text{v}}/3$ approximating $R_{50}$. Table 8 shows the resultant values of $f_b$ in observed $V - R$ in the range of $0.25$ to $1.0$. Errors are given for purely Poisson variations on the number counts and for the rms background variations. Figure 14 shows these data plotted as a function of both redshift and X-ray luminosity. It is clear that no obvious correlations exist and that there is a large scatter. Spearman rank correlation tests confirm this. The large scatter and small range in redshift mean that it would be very difficult to draw any conclusions on the evolution of $f_b$ with redshift from these data alone.

This is not the case for the lack of a correlation of $f_b$ with $L_X$. This cluster sample covers a factor of $\sim 100$ in X-ray luminosity with an even distribution of clusters throughout this range. The lack of any trend suggests that the blue fraction is independent of the global properties of the cluster and that the distribution of galaxy types is the same in all cluster cores regardless of mass. This is in agreement with the work of Balogh et al. (2002), who show that the distributions of star formation rates in low-$L_X$ clusters at $z \sim 0.25$ are indistinguishable from those of X-ray-luminous clusters at similar redshifts, De Propris et al. (2004), who show that $f_b$ is independent of the velocity dispersion of local clusters in the 2df Galaxy Redshift Survey, and Lea & Henry (1988), who show little dependence of $f_b$ on $L_X$ in 14 of the original BO clusters. However, Marston et al. (2001) and Goto et al. (2003) both find a trend of increasing $f_b$ with decreasing cluster richness. It should be noted that both studies use a fixed physical aperture within which they measure $f_b$. This would correspond to a larger fraction of the virial radius, or $R_{50}$, for the poor clusters and could be driving this effect.

It is worth briefly considering the implications of an independence of $f_b$ from $L_X$ on the transformation mechanisms discussed in §1. The most likely explanation for the Butcher-Oemler effect is that as time goes on there is a declining rate of accretion of field galaxies onto clusters, combined with a declining star formation rate in these field galaxies, along with a mechanism to truncate star formation within the cluster environment (Kodama &

### Table 8: Blue Fractions

<table>
<thead>
<tr>
<th>Cluster</th>
<th>$m_R$ (mag)</th>
<th>$f_b$ Cut (mag)</th>
<th>$f_b$</th>
<th>$R_{50}$ (Mpc)</th>
</tr>
</thead>
<tbody>
<tr>
<td>RX J1633.6</td>
<td>20.076</td>
<td>0.182</td>
<td>0.06</td>
<td>0.390 (0.29)</td>
</tr>
<tr>
<td>RX J0333.0</td>
<td>20.145</td>
<td>0.188</td>
<td>0.06</td>
<td>0.290 (0.15)</td>
</tr>
<tr>
<td>RX J0210.4</td>
<td>20.201</td>
<td>0.072</td>
<td>0.22</td>
<td>0.160 (0.13)</td>
</tr>
<tr>
<td>RX J0054.0</td>
<td>20.667</td>
<td>0.093</td>
<td>0.06</td>
<td>0.190 (0.17)</td>
</tr>
<tr>
<td>RX J1606.7</td>
<td>20.839</td>
<td>0.255</td>
<td>0.01</td>
<td>0.250 (0.20)</td>
</tr>
<tr>
<td>RX J2237.0</td>
<td>20.729</td>
<td>0.240</td>
<td>0.16</td>
<td>0.240 (0.18)</td>
</tr>
<tr>
<td>MS 0407.2</td>
<td>19.959</td>
<td>0.172</td>
<td>0.06</td>
<td>0.130 (0.11)</td>
</tr>
<tr>
<td>RX J1418.5</td>
<td>20.678</td>
<td>0.234</td>
<td>0.10</td>
<td>0.100 (0.06)</td>
</tr>
<tr>
<td>RX J0256.5</td>
<td>21.314</td>
<td>0.303</td>
<td>0.02</td>
<td>0.070 (0.06)</td>
</tr>
<tr>
<td>MS 0353.6</td>
<td>20.937</td>
<td>0.269</td>
<td>0.04</td>
<td>0.090 (0.07)</td>
</tr>
<tr>
<td>MS 1455.0</td>
<td>20.300</td>
<td>0.200</td>
<td>0.07</td>
<td>0.170 (0.09)</td>
</tr>
<tr>
<td>MS 2137.3</td>
<td>20.869</td>
<td>0.259</td>
<td>0.02</td>
<td>0.130 (0.10)</td>
</tr>
</tbody>
</table>

Notes: Blue fractions for all clusters. The first error on each number is that calculated using the rms background variation, and the second assuming a Poisson error in the background.
Bower 2001). If that truncation mechanism depends on the cluster mass, then we might expect to see a correlation between $f_b$ and $L_X$. For instance, if the truncation mechanism becomes ineffective for some mass threshold, all of the accreted star-forming galaxies would remain blue, resulting in a higher blue fraction. For ram pressure stripping we are able to directly determine the ram pressure efficiency from the cluster $L_X$.

Figure 15 shows the rest-frame $B - V$ blue fraction as a function of relative ram pressure for all of the clusters. The relative ram pressure is calculated using the relations $P_{\text{ram}} = \rho_{\text{ICM}} V_{\text{gal}}^2$, $V_{\text{gal}} \propto kT_{\text{CL}}^{0.55}$, and $\rho_{\text{ICM}} \propto L_X / kT_{\text{CL}}^2$, where $\rho_{\text{ICM}}$ is the density of the intracluster medium, $V_{\text{gal}}$ is the mean velocity of a galaxy through the cluster, and $T_{\text{CL}}$ and $L_X$ are intracluster medium temperature and X-ray luminosity, respectively. The ram pressure is normalized to give the lowest $L_X$ cluster (RX J0210.4) a value of 1. Figure 15 shows that the average ram pressure varies by a factor of almost 40 in this sample, and yet no dependence with $f_b$ is observed. Further detailed numerical simulations (Stevens et al. 1999) and more sophisticated analytical models (Fujita & Nagashima 1999) show that galaxies in the lowest $L_X$ clusters observed here would not be expected to experience any ram pressure stripping, even in the very central regions of the clusters where both their velocities and the cluster gas density are highest. Therefore, it seems unlikely that ram pressure stripping, or other mechanisms that depend on the global cluster properties such as tidal stripping or harassment, is the sole mechanism determining the blue fraction.

Figure 16 shows the rest $B - V$ blue fractions along with three X-ray–selected cluster samples (Kodama & Bower 2001; Smail et al. 1998; Pimbblet et al. 2002). This illustrates the extension in the range of $L_X$ sampled by this study and demonstrates the lack of a correlation between $f_b$ and $L_X$ over all of these studies.

A number of authors have reported that most clusters show increasing blue fractions with radius (Butcher & Oemler 1984; Abraham et al. 1996; Fairley et al. 2002; Kodama & Bower 2001). This is consistent with the morphology-density relation (Dressler et al. 1994; Dressler 1980) and the observed increase in the average star formation rate with cluster radius (Balogh et al. 1999; Abraham et al. 1996; Gómez et al. 2003; Lewis et al. 2002).

Figure 17 shows the average blue fraction calculated within a series of radii for the whole cluster sample. Values of $f_b$ within each radius are also calculated for three magnitude limits: the standard BO limit, and 1 mag either side of this. The trend of increasing $f_b$ with radius is confirmed in this cluster sample with the main increase seeming to occur within $R_{\text{vir}}/2$, with a near-constant fraction beyond. The brightest galaxies show the largest trend, but the errors preclude making any quantitative conclusion. This is not surprising, as the cluster core is expected to be dominated by bright elliptical galaxies.

4. CONCLUSIONS

We have analyzed the colors of bright galaxies in a sample of 12 X-ray–selected clusters of galaxies at $z \sim 0.3$. The clusters cover a large range in X-ray luminosity ($10^{44}$–$10^{45}$ ergs s$^{-1}$) and hence mass, with the lowest $L_X$ clusters representing some of the least massive studied at this redshift. Furthermore, the wide field of our imaging has allowed us to study the galaxy colors out to the virial radius of each cluster as determined by its X-ray luminosity, well beyond the core region typical of previous studies at this redshift.
We have shown that the red galaxies in our clusters form a tight CMR and measure its slope and zero point. After removing the redshift evolution, we found that neither the slope nor the zero point depends strongly on cluster X-ray luminosity and hence mass. However, these constraints were limited by both the small number of clusters and the accuracy of the CMR fitting caused by the statistical field correction required in purely photometric studies of galaxy clusters. By combining all of the clusters together, we were able to measure the change in the zero point of the CMR as a function of cluster radius. We found that the CMR became bluer by $0.1 \pm 0.036$ in $B - R$ out to $0.75R_p$. If this was driven purely by an age change, it corresponds to a difference of $\sim 2.5$ Gyr.

We also measure the fraction of blue star-forming galaxies as defined by Butcher and Oemler in our clusters. Again we find that there is no dependence of $f_b$ on cluster X-ray luminosity and hence mass. However, we do again find a dependence on radius, particularly for the brightest galaxies.

Overall, we can find no dependence of cluster galaxy population on the global cluster environment, i.e., cluster mass, but we do find a dependence on local environment, i.e., galaxy density. The lack of any trends with cluster mass suggests that mechanisms like ram pressure stripping, tidal stripping, or harassment, which depend strongly on cluster mass, are unlikely to be solely responsible for changing the galaxy population from the blue star-forming galaxies that dominate low-density environments to the red passive galaxies that dominate clusters.

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REFERENCES

Beers, T. C., Flynn, K., & Gebhardt, K. 1990, AJ, 100, 32
Quilis, V., Moore, B., & Bower, R. 2000, Science, 288, 1617