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Stellar velocity dispersions and emission line properties of SDSS-III/BOSS galaxies

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ABSTRACT
We perform a spectroscopic analysis of 492 450 galaxy spectra from the first two years of observations of the Sloan Digital Sky Survey (SDSS) III/Baryonic Oscillation Spectroscopic Survey (BOSS) collaboration. This data set has been released in the ninth SDSS data release, the first public data release of BOSS spectra. We show that the typical signal-to-noise ratio of BOSS spectra, despite being low, is sufficient to measure stellar velocity dispersion and emission line fluxes for individual objects. We show that the typical velocity dispersion of a BOSS galaxy is $\sim 240$ km s$^{-1}$. The typical error in the velocity dispersion measurement is 14 per cent, and 93 per cent of BOSS galaxies have velocity dispersions with an accuracy of better than 30 per cent. The distribution in velocity dispersion is redshift independent between redshifts 0.15 and 0.7, which reflects the survey design targeting massive galaxies with an approximately uniform mass distribution in this redshift interval. We show that emission lines can be measured on BOSS spectra. However, the majority of BOSS galaxies lack detectable emission lines, as is to be expected because of the target selection design towards massive galaxies. We analyse the emission line properties and present diagnostic diagrams using the emission lines [O ii], H$\beta$, [O iii], H$\alpha$ and [N ii] (detected in about 4 per cent of the galaxies) to separate star-forming objects and active galactic nuclei (AGN). We show that the emission line properties are strongly redshift dependent and that there is a clear correlation between observed frame colours and emission line properties. Within in the low-$z$ sample (LOWZ) around 0.15 < $z$ < 0.3, half of the emission line galaxies have low-ionization nuclear emission-line region (LINER)-like emission line ratios, followed by Seyfert-AGN-dominated spectra, and only a small fraction of a few per cent are purely star-forming galaxies. AGN and LINER-like objects,
1 INTRODUCTION

Within the framework of hierarchical galaxy formation theory (White & Rees 1978; Frenk et al. 1985), the formation and evolution of galaxies is driven by the interplay between dark matter and baryon physics involving complex processes such as gas accretion, star formation, black hole accretion, chemical enrichment, galactic winds, etc. Progress in our understanding of galaxy formation crucially relies on the observational constraints that can be set on theoretical models. Traditionally, this can be done either through detailed studies of local galaxies (e.g. Kuntschner 2000; Davies et al. 2001; Kormendy & Kennicutt 2004; Thomas et al. 2005; Kormendy et al. 2009, 2010; Kuntschner et al. 2010), or through the analysis of remote galaxies at large distances using the Universe as a time machine (e.g. Genzel et al. 2003; Cimatti et al. 2004; Bundy et al. 2006).

Recent large galaxy surveys have opened a new avenue to approach this problem by providing large data sets that allow statistical studies of large galaxy samples in the nearby Universe. In the last decade an overwhelming number of studies based on data from the Sloan Digital Sky Survey (SDSS; York et al. 2000) have led to significant progress in our understanding of the local galaxy population (e.g. Blanton et al. 2003; Kauffmann et al. 2003a,b; Brinchmann et al. 2004; Tremonti et al. 2004; Wake et al. 2006; Panter et al. 2007; Schawinski et al. 2007; Thomas et al. 2010). The Baryon Oscillation Spectroscopic Survey (BOSS), part of the SDSS III collaboration (Eisenstein et al. 2011, SDSS-III), will now extend this data base to higher redshifts obtaining spectra of 1.5 million luminous galaxies up to redshifts \( z \approx 0.7 \) by 2014. This will allow large-scale statistical studies of the galaxy population at an epoch when the Universe had only half of its current age.

In this paper we present the spectroscopic analysis of 492 450 galaxy spectra observed in the first 1.5 years of BOSS operation covering about one third of the total survey area. We introduce the spectroscopic analysis tools developed for this purpose and present stellar velocity dispersions, emission line fractions and emission line classifications. The aim of this work is to characterize BOSS galaxies and to discuss their basic spectroscopic properties in the line classifications. The main focus here is to provide a powerful colour–colour space to select luminous galaxies up to redshift \( z \approx 0.7 \) in the construction of the SDSS luminous red galaxies (LRG) sample (Eisenstein et al. 2001) and in the 2dF-SDSS LRG and Quasi Stellar Object (QSO) survey (2SLAQ; Cannon et al. 2006). BOSS reaches significantly deeper than the SDSS LRG sample and is significantly wider than 2SLAQ.

The galaxy sample is split in a high-redshift sample called CMASS and a low-redshift sample called LOWZ. The limiting apparent magnitude for galaxy targets is \( 17.5 < i < 19.9 \) mag AB (Oke & Gunn 1983) in the CMASS and \( 16 < r < 19.6 \) mag in the LOWZ samples. While the SDSS MAIN sample is purely magnitude limited, CMASS and LOWZ employ colour cuts in order to target higher-z samples without being overwhelmed by low-z contamination. These cuts are designed to target massive passively evolving galaxies, but also include some star-forming galaxies as explored in the present paper. The \( r - i \) colour serves as a powerful and simple redshift estimator. At redshift \( z \approx 0.4 \) the 4000 Å break moves from the \( g \) into the \( r \) band, which results in a steep rise of \( r - i \) colour as a function of redshift beyond \( z = 0.4 \). The two cuts, LOWZ and CMASS, reflect this dividing line at \( z = 0.4 \). The model trajectory of a passively evolving massive galaxy with \( M \sim 10^{11} M_\odot \) (Maraston et al. 2009b) shows that this galaxy class hits the detection limit of \( i = 19.9 \) mag at a redshift of \( z \approx 0.7 \). As a consequence, the CMASS sample contains massive galaxies in the redshift interval \( 0.4 \leq z \leq 0.7 \). The number density of BOSS galaxies drops sharply beyond \( z = 0.7 \) (Padmanabhan et al. 2010; White et al. 2011). About one third of the LOWZ sample is covered with existing SDSS-II spectroscopy, while most of the CMASS galaxy spectra are obtained for the first time with BOSS observations. Note that we do not include LOWZ or CMASS targets with existing spectra from SDSS-II in the present analysis.

A subsample called SPARSE has been defined within CMASS in order to allow us to study galaxies beyond the nominal CMASS galaxies up to redshifts \( z \approx 0.7 \). A comprehensive overview of the project is presented in Eisenstein et al. (2011) and Dawson et al. (2013). The first public release of BOSS spectra in 2012 July as part of the ninth SDSS data release (DR9) is described in Ahn et al. (2012).

2 DATA

BOSS is one of four surveys of the SDSS-III collaboration using an upgrade of the multi-object spectrograph on the 2.5-m SDSS telescope (Gunn et al. 2006) to collect spectra of galaxies and quasars over 10 000 deg\(^2\) on the sky. BOSS has started operation in Fall 2009 and by 2014 it will have observed about 1.5 million luminous galaxies instead, are less prevalent in the high-z sample (CMASS) around \( 0.4 < z < 0.7 \), where more than half of the emission line objects are star forming. This is a pure selection effect caused by the non-detection of weak H\(\beta\) emission lines in the BOSS spectra. Finally, we show that star-forming, AGN and emission line free galaxies are well separated in the \( g - r \) versus \( r - i \) target selection diagram.

Key words: surveys – galaxies: active – galaxies: evolution – galaxies: general – galaxies: ISM – galaxies: kinematics and dynamics.

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selection cuts. The SPARSE sample contains galaxies with slightly bluer $r-i$ colours for targets with an $i$-band magnitude fainter than 19.5 (for details see Dawson et al. 2013). Furthermore, the BOSS data set includes a sample obtained during commissioning called COMM that is part of the CMASS sample. The current study includes the SPARSE and the COMM samples as part of CMASS.

Galaxy target selection is designed to construct a sample of massive galaxies with constant comoving number density between redshifts 0.1 and 0.7 with a uniform mass distribution at all redshifts. The analyses of number density (Padmanabhan et al. 2010; White et al. 2011) and galaxy masses (Chen et al. 2012; Maraston et al. 2013) from early BOSS data show that this goal has been achieved. Both these constraints are critical for the proper measurement of large-scale structure as a function of redshift and the cosmology science goals of BOSS (Anderson et al. 2012). The uniform mass distribution is crucial for galaxy evolution studies, as it provides a sample that is homogeneous in mass, thus minimizing the mass bias when studying galaxy properties as a function of redshift.

### 2.2 Spectroscopy

BOSS multi-object spectroscopy is being performed with an upgrade of the SDSS fibre-fed spectrograph. The hardware upgrade is introduced in Bhardwaj et al. (2010), Roe et al. (2010) and Smee et al. (2013), while details about the spectroscopic observations, data reduction and the spectroscopic pipeline are provided in Bolton et al. (2012). The most important features of the upgrade include the increase in the number of fibres to 1000 per plate, the decrease in fibre diameter to 2 arcsec and the employment of a new CCD with extended wavelength coverage to span 3600 to 10000 Å and much improved throughput. Large format VPH gratings and thick, fully depleted CCDs are special features of the upgrade (Roe et al. 2010). The SDSS pipeline is used for data reduction and simple measurements. Standard stars are targeted on each plate, so that the BOSS spectra have been flux-calibrated.

The upgrade implies that spectra of reasonable signal-to-noise ratio (S/N) can be obtained in 1-h exposures down to the limiting magnitude in the $i$ band of 19.9 mag. The typical S/N of a BOSS galaxy spectrum are about 5 per Å, which is sufficient for an accurate redshift determination. In fact, the desired redshift efficiency of 95 per cent has been accomplished (Masters et al. 2011; Ross et al. 2011; White et al. 2011). The quality of the spectra is sufficient for the detection of emission lines and the measurement of simple dynamical quantities such as stellar velocity dispersion, which are subject of the present paper. The spectral resolution is $R \sim 2000$, hence high enough for an accurate derivation of these basic quantities.

The typical S/N clearly does not allow for more detailed spectroscopic studies of individual objects. However, very high S/N spectra can be obtained through stacking. This approach is necessary for absorption line measurements and studies of element abundance ratios and other stellar population parameters, which is the subject of future work.

### 2.3 The present sample

BOSS began in 2009 December, and has taken 534,474 galaxy spectra in total by 2011 July, observing 813 plates over 3,275 deg$^2$ on the sky, which corresponds to about one third of the final survey footprint. We use this data set in the present work, which corresponds to the data volume that has been released in DR9, the first public data release of BOSS spectra. We select those objects that are classified as galaxies and for which the ZWARNING_NQSO flag is set zero (reliable redshifts and excluding QSOs) resulting in 492,450 unique objects (excluding repeat observations). This includes all BOSS galaxies from DR9 that have been selected through the LOWZ and CMASS selection cuts. The SPARSE sample is included within the CMASS selection. We do not consider LOWZ or CMASS targets with spectra from SDSS I/II.

### 3 Analysis Tools

Following the approaches of Schawinski et al. (2007) and Thomas et al. (2010), we use the publicly available codes pPXF (Cappellari & Emsellem 2004) and GANDALF v1.5 (Sarzi et al. 2006) to calculate stellar kinematics and to derive emission line properties. We refer to those papers for more information. In brief, GANDALF fits stellar population and Gaussian emission line templates to the galaxy spectrum simultaneously to separate stellar continuum and absorption lines from the ionized gas emission. Stellar kinematics are evaluated by pPXF. The subtraction of the emission line spectrum from the observed one produces a clean absorption line spectrum free from emission line contamination. This spectrum will be used for any further analysis of absorption features. The fits account for the impact of diffuse dust in the galaxy on the spectral shape adopting a Calzetti (2001) obscuration curve. The code further determines the kinematics of the gas (velocity and velocity dispersion) and measures emission line fluxes and equivalent widths (EWs) on the resulting Gaussian emission line template.

To calibrate our analysis tool we present a comparison with low-redshift data from the previous surveys SDSS-I/II. We have selected a subset of ~10,000 SDSS galaxies from 20 randomly selected plates. Quantities published in Data Release 7 (DR7; Abazajian et al. 2009) are adopted for the comparison. This is for calibration purposes only, and the DR7 set of galaxies is not part of the higher-redshift BOSS sample from DR9 analysed in this paper.

#### 3.1 Stellar population templates

The stellar population template is a critical ingredient in this procedure. We adopt the new stellar population models from Maraston & Strömbäck (2011) based on the MILES stellar library (Sánchez-Blázquez et al. 2006). The wavelength range covered by these templates is 3500–7500 Å. As this blue limit corresponds to a relatively red rest-frame wavelength of ~5200 Å around $z \sim 0.5$, Maraston & Strömbäck (2011) have augmented their templates with theoretical spectra at wavelengths $\lambda < 3500$ Å using the model by Maraston et al. (2009a) based on the theoretical library UVBLUE (Rodríguez-Merino et al. 2005). We use this hybrid model in the present study.

A proper stellar population fit requires a large set of templates spanning a wide range in the parameter space of formation ages, star formation histories, metallicities, stellar initial mass functions and dust attenuations (Maraston et al. 2006; Tojeiro et al. 2009; Maraston et al. 2010). Such an analysis is computationally expensive. However, for the purpose of this work, we merely need the stellar population fits to separate the absorption spectrum from the emission spectrum, and to perform a simple analysis of stellar kinematics. To this end it is most critical to obtain a good representation of the absorption spectrum. Hence in this case we can benefit from the age–metallicity degeneracy, and exclude redundant age–metallicity combinations and complex star formation histories from our templates. The final template set we use consists of simple stellar populations with fixed solar metallicity and a Salpeter (1955) initial mass function, but spanning a wide range in ages.
Stellar velocity dispersion

Stellar kinematics are evaluated by pPXF. The line-of-sight velocity distribution is fitted directly in pixel space, which is alternative to but consistent with Fourier methods (e.g. Bender 1990; Rix & White 1992).

A precise knowledge of the spectral resolution of the underlying stellar library is essential for the accurate derivation of stellar velocity dispersion. For this reason, Beifiori et al. (2011) have performed a careful analysis of the spectral resolution of the Maraston & Strömbäck (2011) stellar population models. They have determined resolutions for stellar spectra from the MILES library as well as the Maraston & Strömbäck (2011) stellar population models through template fits with independent, high-resolution empirical and theoretical spectra. The spectral resolution of the MILES library corresponds to a wavelength-independent dispersion $\Delta \lambda$ of 2.54 Å (full width at half-maximum FWHM). This is slightly larger than the $\Delta \lambda = 2.3$ Å indicated in Sánchez-Blázquez et al. (2006) resulting in a lower spectral resolution. This new resolution value has also been found by Falcón-Barroso et al. (2011) and Prugniel, Vauglin & Koleva (2011) in independent re-analyses of the MILES library.

We have used the resolution measurement from Beifiori et al. (2011) to downgrade the stellar population templates to the BOSS resolution. Note that a $\Delta \lambda$ of 2.54 Å corresponds to a resolution of $R \sim 1800$ at 4500 Å (or $\sim 71 \text{ km s}^{-1}$), which is the nominal SDSS and BOSS resolution at these wavelengths. As a result, the Maraston & Strömbäck (2011) templates only require a modest downgrading at longer wavelengths to the correct BOSS resolution.

At wavelengths bluewards $\sim$4500 Å our MILES-based templates have slightly worse spectral resolutions than our data, which can affect the derivation of stellar velocity dispersion. However, we only use the rest-frame wavelength range 4500–6500 Å for the derivation of stellar velocity dispersion, which is the wavelength range most suitable for stellar kinematics analyses because absorption features are most pronounced (Bender 1990; Bender, Saglia & Gerhard 1994). Therefore, the loss of spectral resolution of the MILES library relative to the BOSS resolution at $\lambda \lesssim 4500$ Å is not a concern for the present work.

We found good agreement between our measurements of stellar velocity dispersion and the ones published in DR7. The measurements in DR7 are based on the direct fitting method, the same approach adopted by pPXF. Fig. 1 shows this comparison. The velocity dispersions are in good agreement with a negligible median offset in $\sigma$ of 1 per cent with a dispersion of 11 per cent.

Emission line measurements

Rest-frame emission line fluxes and EWs of all emission lines available in the rest-frame wavelength range covered are measured on the emission line template spectra. Table 1 summarizes the list of emission lines measured, if accessible in the rest-frame spectrum. An emission line measurement is made when the amplitude-over-noise (AoN) ratio is larger than two, which implies that many of these lines are too weak to be detected in BOSS. Reasonable AoN ratios can be obtained in a subsample of BOSS galaxies, however, for some of the stronger lines such as the forbidden lines [O II] $\lambda\lambda 3726 + 3729$, [O III] $\lambda 5007$ and [N II] $\lambda 6583$, as well as the Balmer lines H$\beta$ and H$\alpha$. Line fluxes of the O II doublet [O II] $\lambda\lambda 3726 + 3729$ are calculated as the sum of the individual lines [O II] $\lambda 3726$ and [O II] $\lambda 3729$. EWs are calculated as the ratio between line and continuum fluxes. The continuum flux adopted is the median of the average fluxes in the two blue and red continuum windows at a distance of 200 km s$^{-1}$ from the centre of the line and with a width of 200 km s$^{-1}$.

We note that continuum fluxes as listed in the Portsmouth DR9 catalogue still need to be corrected to rest-frame by multiplication with the factor $(1 + z)$. Consequently, EW provided in the Portsmouth DR9 catalogue need to be divided by the same factor $(1 + z)$ to be translated into rest frame. To be better consistent with the emission line fluxes in the catalogue, that are presented in rest-frame, future data releases (DR10 and onwards) will provide proper rest-frame continuum fluxes and EWs with this correction factor already included.

In case of a relatively low S/N as provided by SDSS and BOSS spectroscopy, it would generally be preferable to tie the kinematics of most emission lines to stronger related lines such as H$\alpha$ at...
the resulting does not affect the emission line measurements, but does imply that foreground extinction before the emission lines analysis. This extinction obtained in this way. Note that we do not correct for Milky Way emission line fluxes provided have been corrected for dust extinction adopting a Calzetti (2001) obscuration curve. The fits and focus on the diffuse dust component that only affects the emission line is barely detected, the inclusion of this second dust component tends to yield unreasonably high values for dust extinction a posteriori.

Thus, we do not consider this second dust component in the measurement generally agree well showing tight correlations with small scatter and only small offsets. Median offsets in emission line flux measurements are below 0.02 dex with a dispersion of ~0.1 dex. Only [O III] λλ3726 + 3729 is slightly more offset by ~0.1 dex with a somewhat larger dispersion of ~0.2 dex. This may not be surprising, as the [O III] λλ3726 + 3729 doublet is barely resolved at SDSS spectral resolution, and the measurement is therefore more uncertain. Similar offsets, even though somewhat larger, are present for the EWs. Median offsets are below 0.04 dex for [O II] λλ3729, Hα and [N II] λ6583, while they increase to 0.1 dex and 0.25 dex for Hβ and [O III] λλ3726 + 3729, respectively, with a larger dispersion of 0.2 dex. These larger discrepancies in the EW measurements will most likely be caused by differences in the treatment of continuum fitting. As for the fluxes, discrepancies in [O II] λλ3726 + 3729 are further caused by uncertainties in the measurement of this line, as the doublet is not resolved.

We note that this same version of the code is being used within the Galaxy and Mass Assembly (GAMA) project (Driver et al. 2011) to derive simple stellar kinematics and emission line fluxes. The GAMA spectroscopy and a comparison of GANDALF–based emission line measurements with other independent methods are presented in Hopkins et al. (2013). In this comparison, particular care has been taken in the homogenization of the treatment of dust reddening. The result reinforces the above conclusion. It is shown that the measurements of emission line fluxes are consistent to better than 5 per cent, with a dispersion consistent with the error measurements on the lines. The line EW estimates are also consistent to better than 5 per cent in the red, and to 10–15 per cent in the blue, again with dispersions consistent with the measured errors.

### 4 VELOCITY DISPERSIONS OF BOSS GALAXIES

In this section we present the measurements of the line-of-sight velocity dispersions for the BOSS galaxy sample. We show their error distributions, compare with independent measurements and discuss their redshift evolution.

#### 4.1 Example spectra in BOSS

Fig. 3 shows two example spectra for BOSS galaxies around z ~ 0.3 with the best-fitting spectrum composed of the stellar population and the emission line templates overplotted. It can be seen that the code is successful at identifying true emission line features over the relatively high noise level. The stellar population fits are good enough to make measurement of stellar kinematics and emission
Figure 2. Emission line fluxes and EWs for $[\text{O II}]\lambda\lambda 3726 + 3729$, H$\beta$, $[\text{O III}]\lambda 5007$, H$\alpha$ and $[\text{N II}]\lambda 6583$ measured in this work for a subset of SDSS-I/II galaxies in comparison with the measurements published in the DR7. $[\text{O II}]\lambda\lambda 3726 + 3729$ has been calculated as the sum of $[\text{O II}]\lambda 3726$ and $[\text{O II}]\lambda 3729$. Colour indicates number of galaxies (scale given by the colour bar on the right-hand side). Observed, non dust-corrected, values are used. Emission line fluxes and EWs are slightly higher in this work by $\sim 0.1$ dex.
Spectroscopic properties of BOSS galaxies

4.2 Velocity dispersions and their errors

The typical S/N in each BOSS galaxy spectrum is about $5 \text{ Å}^{-1}$. This is considerably lower than the average provided by SDSS-I spectroscopy owing to the faintness of the BOSS targets. However, despite this limitation, measurements of stellar velocity dispersion at reasonable accuracy can still be made. The top-left panel in Fig. 4 shows the distribution in formal measurement errors. There is a strong peak at a typical relative error of 14 per cent, and 93 per cent of the objects have a relative error below 30 per cent. Hence, errors are relatively large, as expected from the low S/N, but $\sigma$ measurements are robust as discussed in the following section through comparison with independent measurements. The top-right panel in Fig. 4 shows the distribution of velocity dispersions with error smaller than 30 per cent. The distribution is approximately Gaussian with a well-pronounced peak at $\sigma = 240 \text{ km s}^{-1}$. This relatively high value is consistent with the goal of the BOSS galaxy target selection algorithm designed to target massive galaxies (Padmanabhan et al. 2010; Dawson et al. 2013; Maraston et al. 2013).

4.3 Comparison with independent measurements

To test the reliability of these measurements we compare our velocity dispersions with alternative measurements. In the bottom panels of Fig. 4 we compare our results with two independent measurements, one from Bolton et al. (2012) based on the original SDSS pipeline (used in Shu et al. 2011) and the other from Chen et al. (2012). The velocity dispersions are slightly higher by $\sim 4$ per cent than the ones of Bolton et al. (2012) at a dispersion of 5 per cent and slightly smaller by $\sim 7$ per cent than the ones of Chen et al. (2012) at dispersions of 19 and 16 per cent, respectively. Both these offsets are smaller than the typical measurement error of 14 per cent. This result is encouraging and underlines the reliability of stellar velocity dispersion measurements on the BOSS spectra despite the relatively large error and low S/N.

4.4 Comparison with higher S/N spectra

Additionally to the comparison with independent measurements we investigated the dependence on S/N. To this end we made use of repeated plate observations in the course of the last two years. We constructed a sample of 574 BOSS galaxies mainly from plates 3615 and 3647 with at least six 1-h observations each. We then stacked the spectra from the individual exposures to a high S/N spectrum for each object. The left-hand panel of Fig. 5 shows the individual spectra and the final stack. It can be seen that the resulting spectrum has a significantly higher S/N. The latter increases by about a factor of 4 from $\sim 5$ to $\sim 20$ per resolution element. It is important to note that each stacked spectrum represents the stack for one individual object.

Finally, we measured stellar velocity dispersion on both the individual and the stacked spectra. The result of this exercise is presented in the right-hand panel of Fig. 5, where we plot the ratio between the measurements on individual and stacked spectra as a function of the measurements on individual spectra. The agreement is very good. There is no systematic offset between measurements on individual (low S/N) and stacked (high S/N) spectra. Furthermore, we find no evidence for a systematic trend with S/N. Hence, overall this exercise demonstrates that velocity dispersion measurements on BOSS spectra are reliable (within their errors) in spite of the relatively low S/N.
Figure 4. Top panels: distributions of the relative errors in the velocity dispersion measurements of BOSS galaxies and the distribution of velocity dispersions with error smaller than 30 per cent. Bottom panels: comparison with independent measurements of velocity dispersions based on the original SDSS DR7 pipeline code by Bolton et al. (2012) and the code by Chen et al. (2012). Colour indicates number of galaxies (scale given by the colour bar on the right-hand side). There are small systematic offsets. The measurements of this work are $\sim 4$ per cent higher than in Bolton et al. (2012) and $\sim 7$ per cent lower than in Chen et al. (2012) at dispersions of 19 and 16 per cent, respectively.

Figure 5. Left-hand panel: individual spectra and their stack of a single BOSS galaxy with repeated 1-h observations. The S/N per resolution element is given by the labels. The S/N of the stacked spectrum is higher by about a factor of 4 compared to the individual spectra. Right-hand panel: median velocity dispersion measured on individual BOSS spectra versus the ratio between the median of measurements on individual and stacked spectra. Each stacked spectrum is the sum of individual spectra of the same object from repeated plate observations. The blue symbols are the median in bins of velocity dispersion; error bars indicate Poisson errors. The agreement is very good, hence velocity dispersion measurements are reliable even at typical BOSS S/N.

4.5 Distribution of velocity dispersions as a function of redshift

In Fig. 6 we show the distributions of velocity dispersions with an error less than 30 per cent, corresponding to 93 per cent of the sample in the redshift intervals 0–0.15, 0.15–0.3, 0.3–0.45, 0.45–0.6, 0.6–0.75, and for $z > 0.7$. The red line indicates the mean position of the peak for the four central redshift intervals.

Fig. 6 shows that the distribution in velocity dispersion is largely independent of redshift within 0.15 $< z < 0.75$. The position of the peak of the distribution does not change, while the width becomes somewhat larger at higher redshifts caused by slightly larger measurement errors (see also Shu et al. 2011). At redshifts below $z \sim 0.15$ and above $z \sim 0.75$, the distributions are skewed and slightly offset towards lower and higher velocity dispersions, respectively. This uniformity of the distribution in velocity dispersion as a function of redshift between 0.15 and 0.75 is an important feature of the BOSS target selection, as it establishes a direct link between the galaxy samples at various redshifts, which allows us to accurately probe the redshift evolution of massive galaxies. Target selection in BOSS has been designed to this purpose and, using stellar
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5 EMISSION LINE PROPERTIES

5.1 BPT classification

We use the emission lines Hβ, [O III]λ5007, Hα and [N II]λ6583 to perform the standard classification based on the diagnostic diagram first introduced by Baldwin et al. (1981) and Veilleux & Osterbrock (1987), and widely used in studies of SDSS galaxies (e.g. Hopkins et al. 2003; Kauffmann et al. 2003b; Miller et al. 2003; Brinchmann et al. 2004; Kewley et al. 2006; Schawinski et al. 2007; Wild et al. 2007; Stasińska et al. 2008). In this method the emission line ratios [O III]/Hβ and [N II]/Hα are used as indicators for the ionization source of the interstellar gas in galaxies. The diagram has been proven to be very powerful at separating star-forming galaxies from objects with AGN. The AoN limit of 2 for all four diagnostic emission lines yields a sample of 4887 spectra (3.5 per cent of the total). Note that the fractions of galaxies with significant detections of the emission lines Hα and [N II]λ6583 are considerably higher (around 30 per cent).

It can be seen that, in contrast to the distribution in galaxy masses and stellar velocity dispersion, there is a change of the emission line properties of BOSS galaxies as a function of redshift, mainly because of selection effects. Furthermore, there is a striking difference between the LOWZ and CMASS samples. Besides the fact that the number of galaxies selected decreases with increasing redshift for LOWZ and increases for CMASS owing to the design of the target...
Figure 7. Emission line classification (Baldwin, Phillips & Terlevich 1981) for BOSS galaxies at various redshift bins (redshift increasing from left to right) for CMASS galaxies (top panels) and LOWZ galaxies (bottom panels). Objects at \( z < 0.45 \) are selected to warrant detectability of H\( \alpha \) and [N II]\( \lambda \)6583. The fraction of objects for which all four emission lines are detected (requiring the AoN ratio of all four lines to be larger than two) is given in the bottom-left corner of each panel. The empirical separation between star-forming galaxies and active galactic nuclei (AGN; dashed line) is from Kauffmann et al. (2003b), and the theoretical extreme starburst line from Kewley et al. (2001) to identify pure AGN emission (solid curved line). A dividing line defined by Schawinski et al. (2007) is used to distinguish between LINER and Seyfert emission (solid straight line). The fractions of galaxies in each of the emission line classes are given by the labels in the panels. Overall, the fraction of objects with detected emission lines is small in BOSS. There is a marked difference in the emission line properties between the BOSS galaxy samples at high and low redshift, mainly caused by selection effects. Furthermore, there is a striking difference between the LOWZ and CMASS samples (see text for details).

selection, the overall fraction of galaxies with detected emission lines (see label in bottom-left corner in each panel) is different for LOWZ and CMASS and changes with redshift. In general, the fraction of star-forming galaxies among BOSS galaxies can be expected to be low, independent of redshift, because of the bias towards massive galaxies at all redshifts.

5.1.1 LOWZ

Not surprisingly, the largest fraction of BOSS galaxies with detectable emission lines (15 per cent) is found in the LOWZ sample at redshifts below 0.15. This should be expected as the contamination with lower-mass galaxies is largest (see Fig. 6). The majority of emission line galaxies have some AGN component, the fraction of purely star-forming galaxies only being 20 per cent. The fraction of galaxies with detected emission lines drops dramatically with increasing redshift to only a few per cent. The prevalence of AGN and LINER-like emission increases further with increasing redshift above 0.15.

We have also examined the presence of BOSS emission line galaxies that are likely to be ionized through old stellar populations rather than AGN. Following Cid Fernandes et al. (2011), we assume that such galaxies can be characterized by having H\( \alpha \) EWs below 3 Å. This threshold has been derived from the distribution of H\( \alpha \) EWs in SDSS galaxies, which is strongly bimodal (see also Bamford et al. 2008), with two peaks at 1 and 16 Å and an intermediate minimum in the neighbourhood of 3 Å (Cid Fernandes et al. 2011). We find that these so-called ‘retired’ galaxies typically have LINER emission, but only a minority (about one quarter) of galaxies with LINER emission line characteristics are found to be better described by this object class.

5.1.2 CMASS

Interestingly, there are some CMASS galaxies at low redshifts below 0.15, even though the selection cuts are designed to target galaxies above \( z \sim 0.4 \). Fig. 7 shows that most of these objects are star-forming galaxies that fell into the CMASS colour selection cut despite being at low redshift, most probably due to dust reddening. These galaxies are also relatively low mass with velocity dispersions at the low-end of the distribution. With increasing redshift, this population progressively disappears from the CMASS sample.

At redshifts above 0.3, closer to the actual redshift range targeted by the CMASS selection cuts, the (very few) galaxies with detected emission lines are mostly AGN. Interestingly, the majority of these AGN are Seyfert. It should be emphasized, however, that AGN fractions derived through optical emission line ratios are critically dependent on S/N. In particular LINERs, typically having lower emission line fluxes, tend to drop out of the sample as the S/N decreases. Hence, the relatively low fraction of BOSS galaxies with LINER emission at high redshifts is most likely a selection effect, and the effect of S/N needs to be considered carefully in scientific analyses.

5.2 Emission line properties at higher redshifts

The analysis of star-forming and AGN fractions at redshifts \( z > 0.45 \) requires alternative methods, as the BPT diagnostic lines H\( \alpha \) and
Figure 8. Emission line classification (Lamareille 2010) for CMASS BOSS galaxies at higher redshift bins (redshift increasing from left to right). The fraction of objects for which all three emission lines are detected (requiring the AoN ratio of all three lines to be larger than two) is given in the bottom-left corner of each panel. The fractions of galaxies in each of the emission line classes are given by the labels in the panels. The relative fractions of star forming and AGN in the redshift interval 0.3 ≤ z ≤ 0.45 agree well with the results from the BPT classification in Fig. 7. Beyond those redshifts, the fraction of star-forming CMASS galaxies increases considerably with increasing redshift.

We analyse the emission line properties of CMASS galaxies in the redshift range 0.3 < z < 0.75. In total, there are 373,924 CMASS galaxies at z > 0.3, from 10,238 of which (2.7 per cent) all three blue diagnostic emission lines ([O II]λλ3726 + 3729, Hβ, [O III]λλ5007) could be detected at an AoN larger than 2. Fig. 8 presents the results for the redshift intervals 0.3 < z < 0.45, 0.45 < z < 0.6 and 0.6 < z < 0.75, equivalent to the BPT diagnostic of Fig. 7 at lower redshifts. The fractions of galaxies in each of the emission line classes are given by the labels in the panels.

The relative fractions of star-forming/SF–AGN composite and AGN in the redshift interval 0.3 ≤ z ≤ 0.45 agree well with the results from the BPT classification in Fig. 7. Beyond those redshifts, the fraction of star-forming CMASS galaxies increases considerably with increasing redshift. At redshifts above 0.6, almost two thirds of the CMASS galaxies with detected emission lines are star-forming or SF–AGN composites. This trend is most probably due to the fact that the Hβ emission line is the weakest among those three, so that objects with low Hβ fluxes drop out first with increasing redshift. These are AGN, while star-forming galaxies with stronger Hβ emission stay above the AoN threshold. A scientific analysis aimed at studying relative fractions of star forming and AGN with redshift will need to perform a careful assessment of this selection effect, which goes beyond the scope of this paper. Still, the BOSS sample is certainly useful for the identification and selection of massive star-forming galaxies at redshifts around z ∼ 0.6. A first analysis of this kind has been carried out by Chen et al. (2013) who study the link between radio AGN activity and star formation in CMASS galaxies around z ∼ 0.6.

6 TARGET SELECTION COLOUR–COLOUR SPACE

We have shown that a small but significant fraction of BOSS galaxies contains emission lines, encompassing all ionization classes from star forming to AGN. It is interesting to investigate whether these emission line properties follow some distinct pattern in the colour–colour diagram used for target selection in BOSS. In the following we split in the redshift ranges 0.45 < z < 0.75, so that we can benefit from the full BPT classification where accessible for the separation between emission line free galaxies, star forming and AGN. In Fig. 9 we present the colour–colour plot g − r versus r − i of all DR9 BOSS galaxies. The left-hand panel is for z < 0.45, and the emission line classes are derived form the BPT classification. The right-hand panel shows BOSS galaxies in the redshift range...
0.45 < z < 0.75, and the emission line classification is based on the blue diagnostic diagram of Lamareille (2010).

### 6.1 The \((g - r)\) versus \((r - i)\) diagram

Galactic extinction-corrected \textit{modelmags} are used. The solid line labelled \(d_r\) indicates the major colour selection cut

\[
d_r \equiv (r - i) - (g - r)/8 = 0.55
\]

that has been used to separate the high-redshift CMASS and the low-redshift LOWZ samples (Dawson et al. 2013). The colour \(r - i\) is an excellent redshift indicator around redshifts of \(z = 0.4\), because the 4000 Å break passes from the \(g\) band into the \(r\) band. As a consequence, galaxies become significantly redder in \(r - i\) and slightly bluer in \(g - r\) with increasing redshift beyond a redshift of \(z = 0.4\) (Eisenstein et al. 2001). This pattern is displayed by the BOSS galaxy data in Fig. 9. Galaxies above the solid line \((d_r \geq 0.55)\) define the CMASS sample and typically have redshifts \(z \gtrsim 0.4\), while everything below that line is in the LOWZ sample with typical redshifts of \(z \lesssim 0.4\). The solid lines labelled ‘LRG’ and ‘2SLAQ’ are the selection cuts used by Eisenstein et al. (2001) and Cannon et al. (2006) to define the 2SLAQ LRG sample, respectively. The dashed line is the dividing line between early-type and late-type from Masters et al. (2011). Total galaxy numbers and emission line class fractions are given in Table 2.

### 6.2 Correlations between observed frame colours and emission line properties

The full BOSS sample is plotted as grey symbols, and galaxies for which emission lines have been detected are plotted as coloured symbols. The various emission line classes derived in the present work are shown using the colour-code of Fig. 7 (left-hand panel) and Fig. 8 (right-hand panel).

As is to be expected, there is a large overlap of the various emission line classes for the LOWZ sample at z < 0.45. Still, galaxies with current star formation activity (blue points) are slightly shifted towards bluer \(g - r\) colours by \(\sim 0.1\) mag, while no measurable offset is observed for the AGN populations (green and red symbols). Galaxies with SF–AGN composite spectra can be found in between those two extremes (purple points). This pattern of star-forming galaxies in the ‘blue cloud’ and transition objects in the ‘green valley’ between the blue cloud and the red sequence has previously been seen in colour–magnitude diagrams of SDSS-II galaxies (Graves et al. 2007; Schawinski et al. 2007; Salim et al. 2007).

For the CMASS sample at redshifts above \(z \sim 0.4\), the separation of the various emission line classes is far more pronounced. There are clear correlations between the observed frame colours and the emission line properties of CMASS galaxies. There is a strong bias such that CMASS galaxies without emission lines are predominantly found in the classical LRG section towards the right-hand side of the diagram at red \(g - r\) colours (most evident in the right-hand panel). CMASS galaxies with emission lines, instead, are more likely to be found at blue \(g - r\) colour, and galaxies with star formation activity (blue points), in particular, populate the blue end of the \(g - r\) colour space, typically having \((g - r) \lesssim 1.0\). AGN, both Seyfert and LINER, preferentially occupy intermediate \(g - r\) colour in between those two extremes. This pattern can be observed in both the low-z and the high-z versions of the diagram. It should be noted that a large fraction of the star-forming galaxies in CMASS/BLUE at blue \(g - r\) colours at \(z < 0.45\) (left-hand diagram) are low-redshift \((z \sim 0.1)\) interlopers that fell into the
CMASS colour cut region most likely because of dust reddening as discussed in Section 5 (see Fig. 7).

Table 2 gives the counts of emission line galaxies and the various emission line classes as well as the total number of objects for the four sections in Fig. 9 defined by the solid lines: CMASS/LRG (above $d_z$, right of ‘LRG’), CMASS/M11 (above $d_z$, between ‘LRG’ and ‘M11’), CMASS/2SLAQ (above $d_z$, between ‘M11’ and ‘2SLAQ’), CMASS/BLUE (above $d_z$, left of ‘2SLAQ’), LOWZ (below $d_z$), CMASS/BLUE is most abundant in emission line objects (23 per cent at $z < 0.45$ and 7 per cent at $z > 0.45$) and star-forming galaxies (around half of emission line spectra). The classical LRG section (CMASS/LRG), instead, is devoid of emission line objects (less than per cent). CMASS/2SLAQ, instead, contains the largest fraction of galaxies with Seyfert-like AGN emission lines (60 per cent).

### 6.3 Star formation histories and morphologies

The dependence of star formation activity on observed $g-r$ colour for the CMASS galaxies as found in the present work is not surprising. As discussed above, it was to be expected that the blue $g-r$ colour is driven by the presence of young stellar populations caused by recent or current star formation episodes. Tojeiro et al. (2012) analyse the star formation histories of CMASS galaxies through Spectral Energy Distribution (SED) fitting and find extended star formation in blue CMASS galaxies (see also Chen et al. 2012). The present results confirm this finding.

If the CMASS galaxies with blue $g-r$ are dominated by young stellar populations and have a fraction of star-forming galaxies, one would expect to find mostly late-type galaxies. This is indeed the case. Masters et al. (2011) analyse the morphologies of BOSS galaxies through Hubble Space Telescope (HST)/COSMOS imaging and find that most CMASS galaxies with blue $g-r$ colour are in fact late-type systems. Their morphology-driven dividing line between early-type and late-type at $g-i = 2.55$ (dashed line in Fig. 9) separates quite well between star-forming and passive galaxies.

### 7 CONCLUSIONS

BOSS is one of four surveys of the SDSS-III collaboration using an upgrade of the multi-object spectrograph on the 2.5-m SDSS telescope to collect spectra of galaxies and quasars over 10 000 deg$^2$ on the sky (Eisenstein et al. 2011). BOSS has started operation in autumn 2009 and by 2014 it will have observed about 1.5 million luminous galaxies up to redshifts $z \sim 0.7$. Targets are selected from SDSS imaging split in a high-redshift sample called CMASS and a low-redshift sample called LOWZ. BOSS multi-object spectroscopy is being performed with an upgrade of the SDSS fibre-fed spectrograph providing spectra of reasonable S/N in 1-h exposures down to the limiting magnitude in the $i$-band of 19.9 mag.

We perform a spectroscopic analysis of 492 450 galaxy spectra that are part of the ninth SDSS data release in 2012 July, the first public data release of BOSS spectra (Ahn et al. 2012). We use the publicly available codes pPXF (Cappellari & Emsellem 2004) and GANDALF v1.5 (Salari et al. 2006) to calculate stellar velocity dispersions and to derive emission line fluxes and EWs. The new stellar population models from Maraston & Str¨omb¨ack (2011) based on the MILES stellar library (Sánchez-Blázquez et al. 2006) are adopted. To calibrate the procedure, we have used our technique to derive stellar velocity dispersions and emission line properties for a sub-set of SDSS galaxies from DR7 (Abazajian et al. 2009) and found satisfying agreement. The velocity dispersions are in good agreement with a small median offset in $\sigma$ of 2 km s$^{-1}$ at a dispersion of 30 km s$^{-1}$. Also the emission line measurements generally agree reasonably well showing tight correlations with small scatter and only small offsets. Our measurements of emission line fluxes and EWs tend to be slightly larger than in DR7 by ~0.1 dex with a dispersion of ~0.2 dex. Still, the comparison is satisfying overall, and residual discrepancies will most likely be caused by differences in the treatments of reddening, absorption line correction and continuum fitting.

We show that the typical S/N of BOSS spectra, despite being low, is sufficient to measure simple dynamical quantities such as stellar velocity dispersion for individual objects. We verify the reliability of our measurements on individual BOSS spectra through comparison with high S/N spectra from repeat-plate observations in BOSS using a subsample of 574 BOSS galaxies mainly from plates 3615 and 3647 with at least six 1-h observations each. The agreement is very good. There is no systematic offset between measurements on individual (low S/N) and stacked (high S/N) spectra. We also do not find any systematic trend with S/N. Finally, we compare our measurements with independent measurements within the BOSS collaboration by Bolton et al. (2012) and Chen et al. (2012), and find good agreement. The typical error in the velocity dispersion measurement is 14 per cent, and 93 per cent of BOSS galaxies have velocity dispersions with an accuracy better than 30 per cent. We show that the typical velocity dispersion of a BOSS galaxy is ~240 km s$^{-1}$. The distribution in velocity dispersion is nearly Gaussian and is redshift independent between redshifts 0.15 and 0.7. At redshifts below $z \sim 0.15$ and above $z \sim 0.75$, the distributions are skewed and slightly offset towards lower and higher velocity dispersions, respectively. This reflects the survey design targeting massive galaxies with an approximately uniform mass distribution in the redshift interval 0.15 to $z < 0.75$.

We show that emission lines can be measured on BOSS spectra, but the majority of BOSS galaxies lack detectable emission lines, as is to be expected because of the target selection design towards massive galaxies.

We analyse the emission line properties for a subsample of 140 596 galaxies below $z = 0.45$, so that the full set of key diagnostic emission lines H$\beta$, [O III]5007, Hr and [N II]6583 is accessible in the rest-frame spectra. All four diagnostic lines are detected at an AoN ratio above two for 4887 spectra (3.5 per cent).
For these, we present the classical diagnostic diagrams (Baldwin et al. 1981) to divide star-forming objects from AGN separately for the high-z sample CMASS and the low-z sample LOWZ. We find that the emission line properties are strongly redshift dependent. Furthermore, there is a clear correlation between observed frame colours and emission line properties. In general, the fraction of star-forming galaxies decreases and the fraction of AGN increases with increasing redshift, mostly owing to selection effects. Within in the LOWZ sample, the majority of emission line galaxies have some AGN component, the fraction of purely star forming galaxies only.

To assess the emission line properties of BOSS galaxies at higher redshifts, we additionally study the 373 924 CMASS galaxies in the redshift range 0.3 < z < 0.75, containing 10 238 objects (2.7 per cent) with significant emission line detections. For this purpose we use the blue diagnostic diagram of Lamareille (2010) based on the emission lines [O ii]λ3726 + 3729, Hβ and [O iii]λ5007. For this sample, the fraction of star-forming galaxies is considerably higher, which is most probably due to the fact that the Hβ emission line is the weakest among the three diagnostic lines, so that objects with low Hβ fluxes, hence AGN, drop out first with increasing redshift. Therefore, the BOSS sample turns out to be instrumental for the identification and selection of massive star-forming galaxies at redshifts around z ~ 0.6.

Finally, we show that CMASS galaxies whose emission lines are produced by star formation activity have blue observed g − r colours and are well separated in the g − r versus r − i target selection diagram.

To conclude, BOSS offers spectra of a large sample of galaxies up to redshifts ~0.8. The quality of BOSS spectroscopy, even though designed for redshift determination, allows the measurement of simple quantities on individual BOSS spectra for a wealth of galaxy evolution studies on dynamical, gas and stellar population properties.

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